# **Windham School District**



# Math K-8 Curriculum

Approved by the Windham School Board on 7/12/2022

# WINDHAM SCHOOL DISTRICT Math

## **TEAM**

All of the math teachers, K-12, participated in the mathematics curriculum by reading, writing, offering input, and editing the mathematics curriculum. This collaboration was extremely valuable.

A special thank you to the following teachers who also took time out of their summer vacation to help lead the mathematics curriculum review:

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### **Mission Statement**

The Windham School District K-12 Mathematics Curriculum has undergone a formal review and revision during the 2021-2022 school year. Previously, the mathematics curriculum was approved in April 2018. Mathematics teachers, representing all grade levels, worked together to revise the math curriculum to ensure that it is a comprehensive math curriculum incorporating both the Common Core State Standards as well as Local Windham School District Standards. There was also a vertical review of core mastery standards to ensure that teachers are emphasizing the same key concepts through a spiral review format. This will help ensure that students are prepared for both state assessments as well as the following grade level or course.

There are three versions of the Windham K-12 Math Curriculum. By grade level or course, there is a summary overview section followed by a more detailed version of the curriculum. The summary overview section gives both parents and teachers a quick list of the concepts to be taught, which includes both vocabulary and skills that will be learned. The second detailed version of the curriculum also includes essential questions and the formal list of Common Core Standards. At the end of this document, there is also a mastery overview document. This document shows the concepts and skills, per grade level or course, that will be emphasized, reviewed, and assessed multiple times throughout the school year.

## <u>Title of Curriculum</u>: Kindergarten Mathematics

| Unit Name  | What (content, vocab)  | Why (enduring understandings)  | How (skills)  |
|--|--|--|---|
| Place Value:<br>Numbers and Operations<br>in Base 10                 | <ul> <li>Numbers 11 to 19</li> <li>Vocabulary: how many more?</li> <li>Tens and ones</li> <li>Relationship between whole and parts</li> <li>Counting on</li> <li>10 can be added to another digit to make a whole number.</li> </ul>   | <ul> <li>Numbers from 11-19 can be represented as the sum of 10 and some more.</li> <li>A pattern is a repetition of shapes, numbers, or any item selected. These patterns can be used to help solve problems.</li> </ul>  | <ul> <li>Identify the value of a digit in a 2 digit number (11-19)</li> <li>Use ten frames to understand base ten</li> <li>Identify symbols +, -, and = in equations</li> <li>Count on from a number to find how many in all.</li> <li>Put parts together to find a whole and taking a whole apart to find parts.</li> </ul>                            |
| Operations and Algebraic<br>Thinking:<br>Addition and<br>Subtraction | <ul> <li>Vocabulary: in all, join, addition sentence, add, equal, equation, sum, left, separate, subtraction sentence, take away, subtract, difference.</li> <li>Symbols: Plus sign (+), equal sign (=)minus sign (-)</li> <li>Adding is joining 2 numbers or groups, subtracting is taking apart</li> <li>The addition symbol can be read as "plus" or "and."</li> <li>The minus sign can be read as "take away."</li> <li>The equal sign symbol can be read as "equals" or "is" or "same as".</li> <li>Equations can be written with addends before the sum or the sum before the addends.</li> <li>Fact families</li> </ul> | <ul> <li>Addition and subtraction can be shown in many different ways. These include putting together, taking apart, separating, and pattern building.</li> <li>Subtraction equations using and = can be used to show subtraction situations.</li> <li>Equations using plus signs and equal signs can be used to show parts of a whole.</li> <li>The ability to solve problems is the heart of mathematics.</li> </ul> | <ul> <li>Demonstrate fluency of addition and subtraction facts (0 to 5).</li> <li>Represent addition and subtraction (6 to 10) with objects, fingers, mental images, and drawings.</li> <li>Solve addition and subtraction word problems.</li> <li>Decompose numbers (0 to 10) into pairs in more than one way by using objects or drawings.</li> </ul> |
| Counting and Cardinality:<br>Counting and Ordering<br>Numbers        | <ul> <li>Numbers and counting 0 to 100</li> <li>The name and formation for each number 0 to 10.</li> <li>Counting begins with zero.</li> </ul>   | <ul> <li>There is a unique symbol that goes with each number word.</li> <li>There is more than one way to show a number.</li> </ul>  | <ul> <li>Count to find how many objects and write the number 0 to 20.</li> <li>Count to 100 by ones and tens.</li> <li>Counting forward from any given number to 100.</li> </ul>  |

|                      | <ul> <li>Meaning of greater than, less than, and equal groups</li> <li>1:1 correspondence when counting</li> </ul>  | <ul> <li>There is a specific order to the set of whole numbers.</li> <li>Zero is a number that tells how many objects there are when there are none.</li> <li>Counting tells the total number in a group no matter which order the objects are counted.</li> <li>Two groups of objects are equal if they can be directly matched, one-to-one, with no extras in either group.</li> </ul> |   |
|----------------------|---|--|---|
| Geometry             | <ul> <li>Two-dimensional shapes (squares, circles, triangles, rectangles, and hexagons)</li> <li>Three-dimensional shapes (cubes, cones, cylinders, and spheres)</li> <li>Describe position of objects using above, below, beside, in front of, behind, next to.</li> <li>Objects can be described, classified, analyzed, compared, and created by their attributes.</li> </ul> | <ul> <li>Shapes are everywhere in our world.</li> <li>Objects can be classified into two categories, based on whether they have or do not have particular attributes.</li> </ul>   | <ul> <li>Describe objects using names of shapes.</li> <li>Identify two and three-dimensional shapes.</li> <li>Name shapes using attributes.</li> <li>Analyze and compare two- and three-dimensional shapes, in different sizes and orientations, using informal language to describe their similarities, differences, parts (e.g. number of sides and vertices) and other attributes (e.g. having sides of equal length).</li> <li>Construct shapes using various materials.</li> <li>Describe relative position of objects using positional words.</li> <li>Name shapes regardless of their overall size or orientation.</li> <li>Compose simple shapes to form larger shapes (e.g join two triangles to make a rectangle).</li> </ul> |
| Measurement and Data | Vocabulary: category, classify, chart,<br>tally mark  | <ul> <li>Measuring identifies how long<br/>things are, how much things<br/>are, how much they weigh,</li> </ul>  | <ul> <li>Describe measurable attributes of objects, such as length or weight.</li> <li>Describe several measurable attributes of</li> </ul>   |

| • | objects have measurable attributes,   |
|---|---------------------------------------|
|   | such as length or weight, that can be |
|   | recognized and described.             |

- objects can have similar measurable attributes.
- objects can be sorted and classified by attribute
- objects in a group can be counted, sorted and compared

and how much they hold.

 Objects can be classified into two categories, based on whether they have or do not have particular attributes. a single object.

- Compare two objects with a measurable attribute in common to see which object has more of / less of a given attribute and describe the difference.
- Classify objects into categories.
- Sort and classify objects by attribute.
- Count the number of objects in each category and sort the categories by how many objects (0 to 10) are in each category (e.g. 2 circles, 1 triangle, 3 rectangles).
- Use tally marks to count.
- Chart data

# Windham School District Curriculum Mathematics - Kindergarten Unit #1: Place Value: Numbers and Operations in Base 10

#### ESTABLISHED GOALS:

Students will begin their formal study of mathematics. In this unit, students will build a foundation for understanding place value by focusing on composing and decomposing numbers 11 - 19 into a group of 10 ones and some additional ones. To help visualize this, students will use objects, drawings and equations.

#### Content Standards:

 K.NBT.A.1 Compose and decompose numbers from 11 to 19 into ten ones and some further ones, e.g., by using objects or drawings, and record each composition or decomposition by a drawing or equation (such as 18 = 10 + 8); understand that these numbers are composed of ten ones and one, two, three, four, five, six, seven, eight, or nine ones

## **Stage 1 Desired Results**

#### Students will be able to independently use their learning to...

- correctly form and identify numbers in mathematics.
- use base 10 when counting and composing higher numbers to 100.
- use 1:1 correspondence, understanding of base 10, and number naming fluency to build skills of addition, subtraction, story problem comprehension, etc.

#### ENDURING UNDERSTANDINGS

- Numbers from 11-19 can be represented as the sum of 10 and some more.
- A pattern is a repetition of shapes, numbers, or any items selected. These patterns can be used to help solve problems.

## Meaning ESSENTIAL QUESTIONS

Transfer

- How does knowing that teen numbers are made of ten and more help me to know the number?
- Why can I start with any number and continue counting?
- Why do we count in increasing order?
- Where have I seen these numbers in my life?
- Why do I need to count how many?
- How can I show ways to make 11, 12, 13, 14, 15, 16, 17, 18, 19, or 20?
- Why do you need to count in order?
- How can one problem help me to solve another?

#### **Acquisition**

#### Students will understand...

- Numbers 11-19
- Vocabulary: how many more?
- Tens and ones
- Relationship between whole and parts
- Counting on

- Identifying the value of a digit in a 2 digit number (11-19)
- Adding 10 and another digit to make a whole number.
- Using ten frames to understand base ten
- Being mindful of symbols in equations
- Counting on from 10
- Finding parts of a whole

| 10 can be added to another digit to make a whole number. |  |
|--|--|
| Used in Content Area Standards                           | 21st Century Skills  |
| not applicable   | <ul><li>Problem solving</li><li>Communication</li><li>Perseverance</li></ul> |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | Other Evidence: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Kindergarten

## **Unit 2: Operations & Algebraic Thinking - Addition & Subtraction**

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|---|----|---|---|---|---|---|---|---|---|--------|---|-----|--|
|   |    |   |   |   |   |   |   |   |   |        |   |     |  |

Students will continue their study of mathematics. In this unit, Students will gain an understanding that addition is "putting together" and subtraction is "taking apart". Students will learn to represent and solve addition and subtraction word problems, decompose numbers, and fluently add and subtract within 5.

#### Content Standards:

- K.OA.A.1 Represent addition and subtraction with objects, fingers, mental images, drawings1, sounds (e.g., claps), acting out situations, verbal explanations, expressions, or equations.
- K.OA.A.2 Solve addition and subtraction word problems, and add and subtract within 10, e.g., by using objects or drawings to represent the problem.
- K.OA.A.3 Decompose numbers less than or equal to 10 into pairs in more than one way, e.g., by using objects or drawings, and record each decomposition by a drawing or equation (e.g., 5 = 2 + 3 and 5 = 4 + 1).
- K.OA.A.4 For any number from 1 to 9, find the number that makes 10 when added to the given number, e.g., by using objects or drawings, and record the answer with a drawing or equation.
- K.OA.A.5 Fluently add and subtract within 5.

## Stage 1 Desired Results

#### Students will be able to independently use their learning to...

- add and subtract to solve more complex equations.
- add and subtract to find differences in daily life.
- add and subtract to complete fact families.

#### Meaning

Transfer

#### **ENDURING UNDERSTANDINGS**

- Addition and subtraction can be shown in many different ways. These include putting together, taking apart, separating, and pattern building.
- Subtraction equations using and = can be used to show subtraction situations.
- Equations using plus signs and equal signs can be used to show parts of a whole.
- The ability to solve problems is the heart of mathematics.

#### **ESSENTIAL QUESTIONS**

- Why doesn't the order numbers in an addition number sentence matter?
- Why does the order of numbers in a subtraction number sentence matter?
- Why does the number sentence show equal groups?
- When do you need to put things together?
- When do you need to take groups apart?
- Do math symbols help you understand equations?
- Why do growing patterns help us solve addition and subtraction problems?
- How can math tools help me solve equations?
- How can I use objects to show subtraction?
- What are ways to separate 10, 9, 8, 7, 6, 5, 4, 3, 2 or 1?
- What are ways to take away from 10, 9, 8,7, 6, 5, 4, 3, 2 or 1?

|                                 | Acquisition  |
|---------------------------------|--|
|                                 | Students will understand Students will be skilled at   |
|                                 | <ul> <li>Vocabulary: in all, join, addition sentence, add, equal, equation, sum, left, separate, subtraction sentence, take away, subtract, difference.</li> <li>Symbols: Plus sign (+), equal sign (=)minus sign (-)</li> <li>Adding is joining 2 numbers or groups, subtracting is taking apart</li> <li>The addition symbol can be read as "plus" or "and."</li> <li>The minus sign can be read as "take away."</li> <li>The equal sign symbol can be read as "equals" or "is" or "same as".</li> <li>Equations can be written with addends before the sum or the sum before the addends.</li> <li>Identifying the value of a digit in a 2 digit number (11-19).</li> <li>Using ten frames to understand base ten. Identifying symbols +, -, = in equations.</li> <li>Counting on from to find how many in all.</li> <li>Putting parts together to make a whole and taking a whole apart to find parts.</li> <li>Using patterns to develop fluency</li> <li>Demonstrating fluency of addition and subtraction with objects (6 - 10) fingers, mental images, drawings, and sounds.</li> <li>Solving addition and subtraction word problems.</li> <li>Decomposing numbers 0 -10 into pairs in more than one way by using objects and</li> </ul> |
|                                 | • Fact families drawings and equations   |
| Used in Content Area Standards  | 21st Century Skills  |
| Joeu III Content Area Standards | Problem solving  |
| at annlicable                   | Communication  |
| not applicable                  |  |
|                                 | Perseverance   |

| Stage 2 - Evidence  |  |  |  |
|---------------------|--|--|--|
| Evaluative Criteria | Assessment Evidence  |  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Mathematics - Kindergarten

# **Unit 3: Counting & Cardinality - Counting & Ordering Numbers**

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|---|--|---|
|   | Stage 1 Desired Results  |   |
| ESTABLISHED GOALS:  | Trai   | nsfer   |
| Students will continue their study of mathematics. In       | Students will be able to independently use their lea             | rning to  |
| this unit, students will learn to write, identify and count | • correctly form and identify numbers in mathem                  | atics.  |
| objects in a variety of arrangements, and understand        | • build skills of addition, subtraction, story proble            | m comprehension, etc. by using 1:1 correspondence,          |
| the quantity of a group in order to compare groups to       | comparing numbers, and number names.                             |   |
| find greater than, less than and equal to.                  | Med  | ning  |
| E   | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS   |
| Content Standards:  | • There is a unique symbol that goes with each                   | • Why do I need to count how many?                          |
| • K.CC.A.1 Count to 100 by ones and by tens.                | number word.   | • Why do you need to count in order?                        |
| K.CC.A.2 Count forward beginning from a given               | • There is more than one way to show a number.                   | <ul> <li>Can we count how many objects no matter</li> </ul> |
| number within the known sequence (instead of                | • There is a specific order to the set of whole                  | how we set them up?   |
| having to begin at 1).                                      | numbers.   | Where have I seen numbers in my life?                       |
| • K.CC.A.3 Write numbers from 0 to 20. Represent a          | <ul> <li>Zero is a number that tells how many objects</li> </ul> | • Why do we need to know the numbers?                       |
| number of objects with a written numeral 0-20               | there are when there are none.                                   | • How can I show ways to make 0,1,2,3,4,5,6, 7,             |
| (with 0 representing a count of no objects)                 | • Counting tells the total number in a group no                  | 8, 9, or 10?  |
| K.CC.B.4 Understand the relationship between                | matter which order the objects are counted.                      | • How is zero different from the other numbers?             |
| numbers and quantities; connect counting to                 | • Two groups of objects are equal if they can be                 | <ul><li>Why are the groups equal or not equal?</li></ul>    |
| cardinality   | directly matched, one-to-one, with no extras in                  |   |
| K.CC.B.5 Count to answer "how many?" questions              | either group.  |   |
| about as many as 20 things arranged in a line, a            | • Counting helps us solve problems in our lives.                 |   |
| rectangular array, or a circle, or as many as 10            |  | isition   |
| things in a scattered configuration; given a number         | Students will understand   | Students will be skilled at                                 |
| from 1-20, count out that many objects.                     | • The name and formation for each number from                    | <ul> <li>Counting to find how many objects and</li> </ul>   |
| K.CC.C.6 Identify whether the number of objects             | 0-10   | writing the number 0-20.                                    |
| in one group is greater than, less than, or equal to        | <ul> <li>Counting begins with zero</li> </ul>                    | <ul> <li>Counting to 100 by ones and tens.</li> </ul>       |

| <ul> <li>the number of objects in another group, e.g., by using matching and counting strategies.1</li> <li>K.CC.C.7 Compare two numbers between 1 and 10 presented as written numerals.</li> </ul> | <ul> <li>Meaning of greater than, less than, and equal groups</li> <li>Vocabulary: total, zero, number, part, whole, group order, compare, equal/equal to, greater than, less than, same number as, not</li> <li>1:1 correspondence</li> </ul> | <ul> <li>Counting forward from any given number to 100.</li> <li>Identifying and comparing numbers, between 1 and 10, in terms of greater than, less than or equal to.</li> </ul> |
|---|--|---|
| Used in Content Area Standards  |  | 21st Century Skills   |
| not applicable  |  | <ul><li>Problem solving</li><li>Communication</li><li>Perseverance</li></ul>  |

| Stage 2 - Evidence  |  |  |  |
|---------------------|--|--|--|
| Evaluative Criteria | Assessment Evidence  |  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Mathematics - Kindergarten Unit 4: Geometry

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|----|-----|-------|------|-----|
|    |     |       |      |     |

Students will continue their study of mathematics. In this unit, students will identify two and three dimensional shapes as well as analyze and compare various shapes by their attributes.

#### Content Standards:

- CCSS.MATH.CONTENT.K.G.A.1 Describe objects in the environment using names of shapes, and describe the relative positions of these objects using terms such as above, below, beside, in front of, behind, and next to.
- CCSS.MATH.CONTENT.K.G.A.2 Correctly name shapes regardless of their orientations or overall size.
- CCSS.MATH.CONTENT.K.G.A.3 Identify shapes as two-dimensional (lying in a plane, "flat") or threedimensional ("solid").
- CCSS.MATH.CONTENT.K.G.B.4 Analyze and compare two- and three-dimensional shapes, in different sizes and orientations, using informal language to describe their similarities, differences, parts (e.g., number of sides and vertices/"corners") and other attributes (e.g., having sides of equal length).

## **Stage 1 Desired Results**

#### Transfer

#### Students will be able to independently use their learning to...

- name and recognize shapes in their authentic forms and within their environment
- compare and sort shapes by kind

#### Meaning

#### ENDURING UNDERSTANDINGS

- Shapes are everywhere in our world.
- Objects can be classified into two categories, based on whether they have or do not have particular attributes.

#### ESSENTIAL QUESTIONS

• How do shapes make up our world?

#### **Acquisition**

#### Students will understand...

- Two-dimensional shapes (squares, circles, triangles, rectangles, hexagons)
- Three-dimensional shapes (cubes, cones, cylinders, spheres)
- Positional words such as above, below, beside, in front of, behind, next to, to describe an object's location.
- objects can be described, classified, analyzed, compared, and created by their attributes.

- describing objects in the environment using names of shapes.
- identifying two-dimensional and three-dimensional shapes.
- naming shapes using attributes.
- analyzing and comparing two- and threedimensional shapes, in different sizes and orientations, using informal language to describe their similarities, differences, parts (e.g. number of sides and vertices) and other attributes (e.g., having sides of equal length).
- constructing shapes using various materials (e.g. sticks and clay balls), and draw shapes.

| Used in Content Area Standards not applicable  | <ul> <li>21st Century Skills</li> <li>Problem solving</li> <li>Communication</li> <li>Perseverance</li> </ul>  |
|--|--|
| <ul> <li>the world by building shapes from components (e.g., sticks and clay balls) and drawing shapes.</li> <li>CCSS.MATH.CONTENT.K.G.B.6 Compose simple shapes to form larger shapes. For example, "Can you join these two triangles with full sides touching to make a rectangle?"</li> </ul> | using positional words. <ul> <li>naming shapes regardless of their orientations or overall size.</li> <li>composing simple shapes to form larger shapes. (For example, "Can you join these two triangles with full sides touching to make a rectangle?").</li> </ul> |
| CCSS.MATH.CONTENT.K.G.B.5 Model shapes in  | describing the relative position of objects  |

| Stage 2 - Evidence   |  |  |  |
|--|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |  |

# Windham School District Curriculum Mathematics - Kindergarten Unit 5: Measurement & Data

| Onit J. Wiedstrient & Data                              |   |   |  |  |
|---|---|---|--|--|
|   | Stage 1 Desired Results   |   |  |  |
| ESTABLISHED GOALS:                                      | Transfer  |   |  |  |
| Students will continue their study of mathematics. In   | Students will be able to independently use their lea                | rning to  |  |  |
| this unit, students will be able to measure an object's | <ul> <li>understand differences in objects based on size</li> </ul> |   |  |  |
| length, width, height and volume and compare these      | <ul> <li>use charts to understand data (how many more</li> </ul>    | , how many fewer, which is the most? which is the                 |  |  |
| attributes to those of other objects.                   | least? etc.)  |   |  |  |
|   | Med   | ning  |  |  |
| Content Standards:                                      | ENDURING UNDERSTANDINGS   | ESSENTIAL QUESTIONS   |  |  |
| K.MD.A.1 Describe measurable attributes of              | <ul> <li>Measuring identifies how long things are, how</li> </ul>   | <ul><li>Can all things be measured?</li></ul>                     |  |  |
| objects, such as length or weight. Describe several     | much they weigh, and how much they hold.                            | <ul> <li>How do we use measurement every day?</li> </ul>          |  |  |
| measurable attributes of a single object.               | <ul> <li>Objects can be classified into two categories,</li> </ul>  | Why do we measure things?   |  |  |
| K.MD.A.2 Directly compare two objects with a            | based on whether they have or do not have                           | How many ways can you sort a group of                             |  |  |
| measurable attribute in common, to see which            | particular attributes.  | objects?  |  |  |
| object has "more of"/"less of" the attribute, and       |   | <ul> <li>How can classifying data help to answer</li> </ul>       |  |  |
| describe the difference. For example, directly          |   | questions?  |  |  |
| compare the heights of two children and describe        |   | Why do we chart our data?   |  |  |
| one child as taller/shorter.                            | Acquisition   |   |  |  |
| K.MD.B.3 Classify objects into given categories;        |   | Students will be skilled at                                       |  |  |
| count the numbers of objects in each category and       | Vocabulary: category, classify, chart, tally mark                   |   |  |  |
| sort the categories by count.                           | <ul> <li>objects have measurable attributes, such as</li> </ul>     | such as length or weight.   |  |  |
|   | length or weight, that can be recognized and                        | <ul> <li>describing several measurable attributes of a</li> </ul> |  |  |
|   | described.  | single object.  |  |  |
|   | • objects can have similar measurable attributes.                   | <ul> <li>comparing two objects with a measurable</li> </ul>       |  |  |
|   | <ul> <li>objects can be sorted and classified by</li> </ul>         | attribute in common to see which object has                       |  |  |
|   | attribute.  | more of/less of a given attribute and describe                    |  |  |
|   | <ul> <li>objects in a group can be counted, sorted and</li> </ul>   | the difference.   |  |  |

compared.

• classifying objects into categories.

|                                | • | sorting and classifying objects by attribute. counting the number of objects in each category and sorting the categories by how many objects (0 to 10) are in each category (e.g. 2 circles, 1 triangle, 3 rectangles). using tally marks to count. charting data using real life objects and pictographs. |
|--------------------------------|---|--|
| Used in Content Area Standards |   | 21 <sup>st</sup> Century Skills  |
| not applicable                 | • | Problem solving<br>Communication<br>Perseverance   |

| Stage 2 - Evidence   |  |  |  |
|--|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |  |

### <u>Title of Curriculum</u>: Grade 1 Mathematics

| Unit Name   | What (content, vocab)  | Why (enduring understandings)  | How (skills)  |
|-------------|--|--|---|
| Counting    | <ul> <li>Counting follows a sequence</li> <li>Numbers represent an object (1:1 correspondence)</li> <li>Numbers 1-120</li> <li>Numbers can be expressed in pictures, objects and numerals</li> </ul> | Counting helps us solve problems in our lives.   | <ul> <li>Identify the value of a whole number (0 to 120)</li> <li>Count by 1s, 2s, 5s, 10s</li> <li>Order whole number from 0-120</li> <li>Write whole numbers from 0 -120</li> <li>Recognize visual representations of numbers (0-120)</li> <li>Create visual representations using models and written numbers.</li> <li>Represent a quantity of objects with a numeral</li> </ul>   |
| Place Value | <ul> <li>Tens and ones</li> <li>Symbols &lt;, &gt;, and =</li> <li>2-digit numbers</li> <li>Multiples of 10 (10, 20, 30, 40, 50, 60, 70, 80, 90)</li> </ul>  | <ul> <li>Numbers can be organized by ones and tens.</li> <li>Place value can help to solve math problems more efficiently.</li> <li>Place value can be used to compare numbers using symbols.</li> </ul> | <ul> <li>ordering whole numbers (0-120).</li> <li>Represent ten ones as a bundle called "ten".</li> <li>Identify the digit in the tens and ones places in a given two digit number.</li> <li>Identify the value of each digit within a 2-digit number</li> <li>Use mental math to add groups of 10 to a number</li> <li>Compare two-digit numbers using &lt;, &gt;, =</li> <li>add within 100, including adding a two-digit number and a one digit number (23+7=30), and adding a two-digit number and a multiple of 10 (23+20=43).</li> <li>understand that in adding two-digit numbers, one adds tens and tens, ones and ones; and sometimes it is necessary to compose a ten.</li> <li>mentally finding ten more and ten less than a given two-digit number without having to count and explain reasoning.</li> <li>subtracting multiples of 10 in the range of 10-90 from multiples of 10 in the range 10-90 (positive or zero differences).</li> </ul> |

| Addition and Subtraction | <ul> <li>Addition and subtraction</li> <li>Drawings, symbols, equations</li> <li>Numbers 1- 20</li> <li>Properties of addition and subtraction</li> </ul> | Addition and subtraction can be shown in many different ways, including putting together, taking apart and separating.      So w 20 FI D St  | elating strategies used to add or subtract two wo-digit numbers to a written method and xplain reasoning used lse addition and subtraction within 20 to solve roblems, including word problems (adding to, aking from, putting together, taking apart, omparing) by using objects, drawings, and quations with a symbol for the unknown number or represent the problem.  olve word problems using addition of three whole numbers whose sum is less than or equal to 0.  luently add and subtract facts within 10 retermine the unknown number in an addition or subtraction equation relating to three whole umbers (8+?=10). |
|--------------------------|---|--|---|
| Geometry                 | <ul> <li>2-D and 3-D shapes</li> <li>Equal shares of a whole</li> </ul>   | <ul> <li>Shapes are everywhere in our world.</li> <li>A whole can be divided into equal shares.</li> <li>Addition and subtraction can be represented by models &amp; equal equations.</li> <li>Compare the comparent of the comparent of</li></ul> | vistinguish between defining and non-defining ttributes uild and draw shapes with defining attributes omposing (making) two-dimensional shapes to reate a composite shape (e.g. two trapezoids to reate a hexagon). Compose three-dimensional shapes (e.g. 6 quares to create a cube) compare new shapes made from composite shapes artition circles and rectangles into two and four qual shares describing two and four equal shares using the cords halves, fourths, and quarters, and use the hrases half of, fourth of, and quarter of.  |
| Measurement and Data     | <ul><li>Length</li><li>Tools for measurement</li><li>Data</li></ul>   | Measuring objects allows us to compare the size of us  | neasuring and recording the length of an object sing same size units that span the object with no aps or overlaps. expressing the length of an  |

| <ul> <li>Graphs, charts, pictures</li> <li>Graphing categories</li> <li>Analog clock</li> <li>Digital clock</li> <li>Hour hand</li> <li>Minute hand</li> </ul> | <ul> <li>Data and graphs are used to make decisions and solve problems.</li> <li>Time can be measured in a variety of forms including to the nearest hour and half hour.</li> <li>Comparing the lengths of two objects indirectly by using a third object (a pencil, a shoe, a cube).</li> <li>measuring the length of an object using same size units that span the object with no gaps or overlaps.</li> <li>ordering three objects by length.</li> <li>organizing and representing data with up to three categories (Pets: dog, cat, bird).</li> <li>interpreting data with up to three categories.</li> <li>asking and answering questions about the total number of data points: How many in each category? How many more or less are in one category than in another?</li> <li>telling and writing time to the hour and half-hour using analog and digital clocks.</li> </ul> |
|--|---|
|--|---|

# Windham School District Curriculum Mathematics - Grade 1 Unit 1: Counting

|  | Stage 1 Desired Result   | CS CONTRACTOR CONTRACT |  |  |
|--|--|--|--|--|
| ESTABLISHED GOALS:                       |  | Transfer   |  |  |
| Students will continue their study of    | Students will be able to independently use their lear                | rning to   |  |  |
| mathematics. In this unit, students will | <ul> <li>Recognize the value and order of numbers</li> </ul>         |  |  |  |
| be able to count sequentially, read and  | <ul> <li>Create and recognize visual representations of r</li> </ul> | e visual representations of numbers  |  |  |
| write numbers correctly, and recognize   |  | Meaning  |  |  |
| visual representations of numbers.       | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS  |  |  |
|  | <ul> <li>Counting helps us solve problems in our lives.</li> </ul>   | What can numbers represent?  |  |  |
| Content Standards:                       |  | How can numbers be represented using symbols, words and  |  |  |
| • CCSS.1.NBT.A. 1. Count to 120,         |  | tools?   |  |  |
| starting at any number less than         |  | Why do we need numbers?  |  |  |
| 120. In this range, read and write       |  |  |  |  |
| numerals and represent a number          | Acquisition  |  |  |  |
| of objects with a written numeral.       | Students will understand   | Students will be skilled at  |  |  |
| CCSS.MP.4 Model with                     | <ul> <li>counting follows a sequence.</li> </ul>                     | • identifying the value of a whole number (0 to 120).  |  |  |
| mathematics.                             | • numbers represent an object (1:1                                   | • counting forward by 1, 2, 5, 10s (0 to 120).   |  |  |
| • CCSS.MP.6 Attend to precision.         | correspondence).   | writing whole numbers (0 to 120).  |  |  |
| CCSS.MP7 Look for and make use of        |  | <ul> <li>recognizing visual representations of numbers (0 to 120).</li> </ul>  |  |  |
| structure.                               | understand numbers can be expressed in                               | creating visual representation using models and written  |  |  |
| CCSS.MP8 Look for and express            | pictures, objects and numerals.                                      | numbers (0 to 120).  |  |  |
| regularity in repeated reasoning         |  | ordering whole numbers (0 to 120).   |  |  |
|  |  | Representing a quantity of objects with a number.  |  |  |
| Used in Content Area Standards           |  | 21 <sup>st</sup> Century Skills  |  |  |
|  |  | Problem Solving  |  |  |
| not applicable                           |  | Communication  |  |  |
|  |  | Perseverance   |  |  |
|  |  |  |  |  |

| Stage 2 - Evidence   |  |  |  |
|--|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |  |

# Windham School District Curriculum Mathematics - Grade 1 Unit 2: Place Value

### Stage 1 Desired Results

#### ESTABLISHED GOALS:

Students will continue their study of mathematics. In this unit, students will learn to organize numbers based on ones and tens. They will be able to compare numbers using symbols. Students' understanding of place value will help them to solve math problems more efficiently.

#### Content Standards:

- CCSS.1.NBT.B. 2. Understand that the two digits of a two-digit number represent amounts of tens and ones. Understand the following as special cases: 10 can be thought of as a bundle of ten ones called a "ten". The numbers from 11 to 19 are composed of a ten and one, two, three, four, five, six, seven, eight, or nine ones. The numbers 10, 20, 30, 40, 50, 60, 70, 80, 90 refer to one, two, three, four, five, six, seven, eight, or nine tens (and 0 ones).
- CCSS.1.NBT.B.3. Compare two two-digit numbers based on meanings of the tens and ones digits, recording the results of comparisons with the symbols >, =, and <. Use place value understanding and properties of operations to add and subtract.
- CCSS.1.NBT.C.4. Add within 100, including adding a two-digit number and a one-digit number, and adding a two-digit number and a multiple of 10 using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and

## Transfer

### Students will be able to independently use their learning to...

- Make sense of and solve various math problems and real life problems
- Recognize the value and order of numbers
- Use appropriate tools strategically
- Create and recognize visual representations of numbers

#### Meaning

#### ENDURING UNDERSTANDINGS

- Numbers can be organized by ones and tens
- Place value can help to solve math problems more efficiently.
- Place value can be used to compare numbers using symbols.

#### **ESSENTIAL QUESTIONS**

- How does understanding place value help us to compare and order numbers?
- How can knowing the value of a number help us to make decisions?
- Why are zero and ten important?

### Students will understand...

- two digits of a 2-digit number represents amounts of tens and ones.
- symbols <, >, and = can be used to compare numbers
- value of zero in a multiple of 10 (10, 20, 30, 40, etc).
- meaning of base-ten and its use for solving number and real life

#### Acquisition

- representing ten ones as a bundle called "ten".
- identifying the digit in the tens and one places in a given two-digit number.
- identifying the value of each digit within a 2digit number.
- Using mental math to add groups of 10 to a number.
- comparing two two-digit numbers using <, >, and =.

| <ul> <li>subtraction; relate the strategy to a written method and explain the reasoning used.</li> <li>CCSS.1.NBT.C. 5. Given a two-digit number, mentally find 10 more or 10 less than the number, without having to count; explain the reasoning used.</li> <li>CCSS.1.NBTC. 6. Subtract multiples of 10 in the range 10 to 90 from multiples of 10 in the range 10 to 90 (positive or zero differences), using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used. CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Look for and make use of structure.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul> | problems (addition, subtraction, comparison). | • | adding within 100, including adding a two-digit number and a one digit number (23+7=30), and adding a two-digit number and a multiple of 10 (23+20=43). understanding that in adding two-digit numbers, one adds tens and tens, ones and ones; and sometimes it is necessary to compose a ten. mentally finding ten more and ten less than a given two-digit number without having to count and explain reasoning. subtracting multiples of 10 in the range of 10 to 90 from multiples of 10 in the range 10 to 90 (positive or zero differences). relating strategies used to add or subtract two two-digit numbers to a written method and explain reasoning used |
|---|---|---|---|
| Used in Content Area Standards  |   |   | 21 <sup>st</sup> Century Skills   |
|   |   |   | Problem Solving   |
| not applicable  |   |   | Communication   |
|   |   | • | Perseverance  |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Mathematics - Grade 1 Unit 3: Addition & Subtraction

#### ESTABLISHED GOALS:

Students will continue their study of mathematics. In this unit, students will be able to use multiple strategies to solve addition and subtraction word problems. Students will demonstrate fluency in addition and subtraction problems within 10.

#### Content Standards:

- CCSS.1.OA A.1. Use addition and subtraction within 20 to solve word problems involving situations of adding to taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.
- CCSS.1.OA.A.2. Solve word problems that call for addition of three whole numbers whose sum is less than or equal to 20, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem. Understand and apply properties of operations and the relationship between addition and subtraction.
- CCSS.1.OA.B.3. Apply properties of operations as strategies to add and subtract. 3 Examples: If 8+3 =11 is known, then 3+8 =11 is also known. (Commutative property of addition.) To add 2+6+4, the second two numbers can be added to make a ten, so 2+6+4=2+10=12. (Associative property of addition.)
- CCSS.1.OA.B. 4. Understand subtraction as an unknown-addend problem. For example, subtract 10-8 by finding the number that makes 10 when added to 8.
- CCSS.1.OA.C.5. Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).

## Transfer

Students will be able to independently use their learning to...

Apply addition and subtraction strategies to solve problems

 Apply addition and subtraction strategies to solve problems in everyday life.

Meaning

#### ENDURING UNDERSTANDINGS

- Addition and subtraction can be shown in many different ways including putting together, taking apart, and separating.
- Addition and subtraction can be represented by models and equations.

#### **ESSENTIAL QUESTIONS**

- How do addition and subtraction help me function in my world?
- How does comparing numbers help us solve problems?

#### Acquisition

#### Students will understand...

- multiple ways to solve addition and subtraction equations with whole numbers.
- addition and subtraction procedures have real world application.
- commutative and associative properties of addition and subtraction.

- using addition and subtraction within 20 to solve problems, including word problems (adding to, taking from, putting together, taking apart, comparing) by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.
- solving word problems that call for addition of three whole numbers

- CCSS.1.OA.C. 6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as counting on; making ten (e.g., 8+6=8+2+4=10+4=14); decomposing a number leading to a ten (e.g., 13-4=13-3-1=10-1=9); using the relationship between addition and subtraction (e.g., knowing that 8+4=12, one knows 12-8=4); and creating equivalent but easier or known sums (e.g., adding 6+7 by creating the known equivalent 6+6+1=12+1=13).
- CCSS.1. OA.D.7. Understand the meaning of the equal sign, and determine if
  equations involving addition and subtraction are true or false. For example,
  which of the following equations are true and which are false? 6=6, 7=8-1,
  4+1=5+2. CCSS.
- 1.OA.D. 8. Determine the unknown whole number in an addition or subtraction equation relating to three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations 8+? =11, 5=? +3, 6+6=?
- CCSS.MP1 Make sense of problems and persevere in solving them.
- CCSS.MP2 Reason abstractly and quantitatively.
- CCSS.MP3 Construct viable arguments and critique the reasoning of others.
- CCSS.MP4 Model with mathematics.
- CCSS.MP6 Attend to precision.
- CCSS.MP7 Look for and make use of structure.

- number models, objects and drawings are various ways to solve problems.
- meaning of the symbols and the equal sign within equations.
- an unknown number in an equation can be determined by demonstrating the relationship between addition and subtraction

- whose sum is less than or equal to 20.
- fluently adding and subtracting facts within ten.
- determining the unknown number in an addition or subtraction equation relating to three whole numbers (8+? =10).

| Used in Content Area Standards |   | 21 <sup>st</sup> Century Skills |
|--------------------------------|---|---------------------------------|
|                                | • | Problem Solving                 |
| not applicable                 | • | Communication                   |
|                                | • | Perseverance                    |
|                                |   |                                 |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Mathematics - Grade Unit 4: Geometry

|  | Stage 1 Desired Results  |  |
|--|--|--|
| ESTABLISHED GOALS:   | Tro  | ansfer   |
| Students will continue their study of mathematics. In  | Students will be able to independently use their le                          | arning to  |
| this unit, students will identify two-dimensional and  | Divide shapes into equal shares and identify th                              | ose shares   |
| three-dimensional shapes according to defining   | Recognize shapes in their environment  |  |
| attributes. Students will be able to partition circles,  | Me   | eaning   |
| squares, and rectangles into two and four equal parts,   | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS  |
| describing those parts as halves, fourths, or quarters.  | Shapes are everywhere in our world.  | How do shapes make up our world? How is the  |
|  | <ul> <li>A whole can be divided into equal shares.</li> </ul>                | world of geometry connected to the world of  |
| Content Standards:   |  | numbers?   |
| CCSS.1.G.A. 1. Distinguish between defining  |  |  |
| attributes (e.g., triangles are closed and three-  |  | uisition   |
| sided) versus non-defining attributes (e.g. color,   | Students will understand   | Students will be skilled at  |
| orientation, overall size); build and draw shapes to   |  | distinguishing between defining (triangles have  |
| possess defining attributes.   | described, classified and analyzed by their                                  | three sides) and non-defining attributes (color,   |
| CCSS.1.G.A.2. Compose two-dimensional shapes   | attributes.  | orientation, overall size).  |
| (rectangles, squares, trapezoids, triangles, half-   | The names of two and three-dimensional shapes are based on their attributes. | <ul> <li>building and drawing shapes with defining attributes.</li> </ul>                        |
| circles, and quarter-circles) or three-dimensional   | shapes are based on their attributes.  |  |
| shapes (cubes, right rectangular prisms, right   | • shapes can be partitioned in equal shares.                                 | composing (making) two-dimensional shapes to     screet a composite shape (o.g. two transposide) |
| circular cones, and right circular cylinders) to   |  | create a composite shape (e.g. two trapezoids to create a hexagon).                              |
| create a composite shape, and compose new  |  |  |
| shapes from the composite shape.   |  | • composing (making) three-dimensional shapes (e.g. 6 squares to create a cube).                 |
| CCSS.1.G.A. 3. Partition circles and rectangles into two and four equal shares, describe the shares. |  | <ul> <li>comparing new shapes made from composite</li> </ul>                                     |
| two and four equal shares, describe the shares   |  | shapes.  |
| using the words halves, fourths, and quarters, and   |  | <ul> <li>partitioning circles and rectangles into two and</li> </ul>                             |
| use the phrases half of, fourth of, and quarter of.  |  | four equal shares  |
| Describe the whole as two of, or four of the   |  | Tour equal strates   |

| not applicable  | • | Problem Solving Communication Perseverance   |
|---|---|--|
| Used in Content Area Standards  |   | 21st Century Skills  |
| shares. Understand for these examples that decomposing into more equal shares creates smaller shares.  CCSS.MP1 Make sense of problems and persevere in solving them.  CCSS.MP4 Model with mathematics.  CCSS.MP5 Use appropriate tools strategically.  CCSS.MP6 Attend to precision.  CCSS.MP7 Look for and make use of structure. | • | describing two and four equal shares using the words halves, fourths, and quarters, and use the phrases half of, fourth of, and quarter of. describing a whole as two of, or four of the shares. (Ex. A whole circle is made of two halves). demonstrating an understanding that decomposing (taking apart) an object into more equal shares creates smaller shares. |

| Stage 2 - Evidence   |  |  |  |
|--|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |  |

# Windham School District Curriculum Mathematics - Grade 1 Unit 5: Measurement & Data

### **Stage 1 Desired Results**

#### ESTABLISHED GOALS:

Students will continue their study of mathematics. In this unit, students will make accurate measurements using non-standard units. They will be able to read, create, and ask and answer questions using different types of graphs. Students will also write and tell time to the hour and half hour.

#### Content Standards:

- CCSS.1.MD.A. 1. Order three objects by length; compare the lengths of two objects indirectly by using a third object.
- CCSS.1.MD.A. 2. Express the length of an object as a whole number of length units, by laying multiple copies of a shorter object (the length unit) end to end; understand that the length measurement of an object is the number of same-size length units that span it with no gaps or overlaps. Limit to contexts where the object being measured is spanned by a whole number of length units with no gaps or overlaps.
- CCSS.1.MD.B. 3. Tell and write time in hours and half-hours using analog and digital clocks.
- CCSS.1.MD.C. 4. Organize, represent, and interpret data with up to three categories; ask and answer questions about the total number of data points,

#### Transfer

#### Students will be able to independently use their learning to...

- make accurate measurements
- order objects from longest to shortest or shortest to longest based on measurement
- read different types of graphs in different situations and use the information to make accurate decisions in their lives.
- display data in a variety of ways.
- look at graphs and charts and explain their meaning and make sense of the data to apply to their everyday lives.
- accurately tell and write time to help make decisions.

#### Meaning

#### ENDURING UNDERSTANDINGS

- Measuring objects allow us to compare the size of objects,
- Data and graphs are used to make decisions and solve problems.
- Time can be measured in a variety of forms including to the nearest hour and half hour.

#### **ESSENTIAL QUESTIONS**

- Can all things be measured?
- Why is measuring important?
- How can data help us to make decisions and solve problems?
- How can time affect the decisions we make?

#### Acquisition

#### Students will understand...

- attributes (e.g. length, height) of objects are measurable and can be quantified using unit amounts.
- time can be determined using an analog or a digital clock.

#### Students will be skilled at...

 measuring and recording the length of an object using same size units that span the object with no gaps or overlaps. expressing the length of an object by stating the length as a whole number of units (5 same size pencils) by

| <ul> <li>how many in each category, and how many more or less are in one category than in another.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul> | <ul> <li>the different features of a clock such as hour hand and minute hand.</li> <li>questions can be answered by collecting and analyzing data.</li> <li>data represents real world objects and ideas.</li> <li>data can be represented in different forms (chart, graph, picture).</li> </ul> | <ul> <li>laying multiple copies of a shorter object end to end.</li> <li>comparing the lengths of two objects indirectly by using a third object (a pencil, a shoe, a cube).</li> <li>measuring the length of an object using same size units that span the object with no gaps or overlaps.</li> <li>ordering three objects by length.</li> <li>organizing and representing data with up to three categories (Pets: dog, cat, bird).</li> <li>interpreting data with up to three categories.</li> <li>asking and answering questions about the total number of data points: How many in each category? How many more or less are in one category than in another?</li> <li>telling and writing time to the hour and half-hour using analog and digital clocks.</li> </ul> |
|---|---|--|
| Used in Content Area Standards  |   | 21 <sup>st</sup> Century Skills  |
|   |   | Problem Solving  |
| not applicable  |   | Communication  |
|   |   | Perseverance   |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |

### <u>Title of Curriculum</u>: Grade 2 Mathematics

| Unit Name                                 | What (content, vocab)  | Why (enduring understandings)   | How (skills)   |
|---|--|---|--|
| Time and Money                            | <ul> <li>Analog and digital clocks</li> <li>Hour and minute hand</li> <li>Coins and bills</li> <li>\$ and cent symbols</li> </ul>  | <ul> <li>Time can be given in many forms including to the nearest 5 minutes.</li> <li>When counting money, it is usually easier to start with the coin with the greater value.</li> <li>The same amount of money can be represented using different combinations of coins and bills.</li> </ul> | Writing time from analog and digital clock to the nearest five minutes, using a.m. and p.m.  |
| Addition and Subtraction within 20        | <ul> <li>Addition &amp; subtraction drawings, symbols, equations, properties</li> <li>Sum, difference</li> <li>Fact Families</li> <li>Equal Groups / Arrays</li> <li>Odd and even</li> </ul> | There are strategies for learning addition and subtraction facts within 20 that will help with fluency. This includes counting on, making ten, and decomposing.   | <ul> <li>Solving one- and two- step problems using addition and subtraction within 20 with unknowns in all positions.</li> <li>demonstrating fluency of addition and subtraction facts within 20., using mental math strategies.</li> <li>writing fact families that consist of 2 addition and 2 subtraction equations using 3 numerals.</li> <li>arranging objects in rectangular arrays with up to 5 rows and 5 columns and writing an equation to express the total as a sum of equal addends.</li> </ul> |
| Addition and Subtraction for Larger Units | <ul> <li>Addition and subtraction equations</li> <li>Regrouping</li> <li>Composing and decomposing three digit numbers</li> </ul>  | <ul> <li>Students will use place value understanding and properties of operations to solve two-digit three-digit addition and subtraction equations.</li> <li>Two digit numbers can be broken apart using tens and ones and added in different ways.</li> </ul>                                 | <ul> <li>adding and subtracting numbers within 100 using place value strategies.</li> <li>breaking apart numbers into tens and ones to find their sums and differences.</li> <li>explaining their mathematical thinking.</li> <li>adding up to four 2-digit numbers</li> <li>understanding addends can be added in any order.</li> <li>adding 10 or 100 mentally using place value</li> </ul>  |

|                                    |  | <ul> <li>Three-digit numbers can be<br/>broken apart using hundreds,<br/>tens, and ones and added in<br/>different ways.</li> </ul>                      | <ul> <li>adding 3 digit numbers using a variety of strategies<br/>such as adding partial sums, compensation,<br/>traditional algorithms and mental math.</li> </ul>   |
|------------------------------------|--|--|---|
| Representing and Interpreting Data | <ul> <li>Bar graphs, picture graphs and line plots</li> <li>Data</li> </ul>  | <ul> <li>Some questions can be answered by collecting and analyzing data.</li> <li>Data can be represented visually using charts &amp; graphs</li> </ul> | <ul> <li>drawing a picture graph and a bar graph (with single-unit scale) to represent a data set with up to four categories. (Fall, Winter, Spring, Summer).</li> <li>solving simple addition, subtraction, and comparing word problems using information presented in a bar graph and a picture graph.</li> <li>collecting measurement data by measuring lengths of several objects to the nearest whole unit and showing the measurements by making a line plot, where the horizontal scale is marked off in wholenumber units.</li> </ul>   |
| Geometry                           | <ul> <li>2D and 3D shapes</li> <li>Equal shares of a whole</li> <li>Fraction</li> <li>Halves</li> <li>Thirds</li> <li>Fourths</li> <li>Quarters</li> <li>Attributes</li> </ul> | <ul> <li>Two-and-three dimensional objects have unique attributes.</li> <li>A shape can be divided into equal parts.</li> </ul>                          | <ul> <li>recognizing the specified attributes of shapes, such as a given number of angles or a given number of equal faces.</li> <li>drawing shapes with specified attributes, such as a given number of angles or a given number of equal faces.</li> <li>identifying triangles, quadrilaterals, pentagons, hexagons, cubes, pyramids, cones, and cylinders.</li> <li>dividing a rectangle into rows and columns of same-size squares.</li> <li>counting the same-size squares within the rows and columns to find the total number of squares.</li> <li>dividing circles and rectangles into two, three or four equal shares and describing the equal shares as halves, thirds, fourths respectively.</li> <li>describing the whole as two halves, three thirds, four fourths, etc.</li> <li>recognizing that equal shares of identical wholes need not have the same shape.</li> </ul> |

| Measurement | <ul> <li>Rulers, yard and meter sticks, tape measures</li> <li>Number lines</li> <li>Units of measure: inches, feet, yards, centimeters and meters</li> <li>Length</li> </ul>                      | <ul> <li>Some attributes of objects are measurable and can be quantified using unit amounts.</li> <li>Objects can be measured using multiple units of measurement.</li> </ul> | different units of measure, and describing how the two measurements relate to the size of the unit chosen. estimating lengths using units of inches, feet, centimeters, and meters.  Estimating the length of an object using appropriate units for that object.  measuring to determine how much longer one object is than another.  expressing the differences in length in terms of a standard length unit.  using addition and subtraction within 100 to solve word problems involving lengths that are given in the same unit by using drawings and equations with a symbol for the unknown number to represent the problem.  representing whole numbers as lengths from 0 on a number line with equally spaced points corresponding to the numbers 0, 1, 2 and represent whole number sums and differences within 100 on a number line.  generating measurement data by measuring lengths of several objects to the nearest whole unit or by making repeated measurements of the same object. |
|-------------|--|---|---|
| Place Value | <ul> <li>Base 10 blocks</li> <li>Hundreds charts</li> <li>&lt;,&gt;, = symbols</li> <li>2, 3, 4 digit numbers</li> <li>Greater than</li> <li>Less than</li> <li>Equal to</li> <li>Value</li> </ul> | <ul> <li>The value of a number can be determined by the place value of the number.</li> <li>Place value can be used to compare and order numbers.</li> </ul>                  | <ul> <li>Representing 3 digit numbers using models, words, and numbers.</li> <li>Identifying and understanding the value of digits in the hundreds, tens, and ones places</li> <li>Skip-counting by 5s, 10s and 100s to 1000.</li> <li>Identifying the hundreds, tens and ones place in a 3 digit number</li> <li>Comparing the value of two three-digit numbers</li> </ul>   |

# Windham School District Curriculum Mathematics - Grade 2 Unit 1: Time & Money

|  |  | - <b>1</b>  |  |
|--|--|---|--|
|  | Stage 1 Desired Results  |   |  |
| ESTABLISHED GOALS:                               | Transfer   |   |  |
| Students will continue their study of            | Students will be able to independently use their learning to     |   |  |
| mathematics. In this unit, students will be able | • tell and write time to the nearest 5 minutes.                  |   |  |
| to tell and write time to the nearest 5 minutes. | show an amount using dollars and/or coins.                       |   |  |
| Students will be able to show an amount using    | Meaning  |   |  |
| dollars and/or coins.                            | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS   |  |
|  | Time can be given in many forms including o                      | How would life be different if we couldn't measure                    |  |
| Content Standards:                               | the nearest 5 minutes.   | time?   |  |
| CCSS.2.MD 7. Tell and write time from            | <ul> <li>When counting money, it is usually easier to</li> </ul> | What would the world be like without money?                           |  |
| analog and digital clocks to the nearest five    | 8  | <ul> <li>How can time affect the decisions we make?</li> </ul>        |  |
| minutes using a.m. and p.m.                      | The same account of money can be                                 |   |  |
| CCSS.2.MD 8. Solve word problems                 | represented using different combinations of                      |   |  |
| involving dollar bills, quarters, dimes,         | coins and bills.   |   |  |
| nickels, and pennies, using dollar and cent      |  |   |  |
| symbols appropriately. Example: If you           | Acquisition  |   |  |
| have two dimes and three pennies, how            |  | Students will be skilled at   |  |
| many cents do you have?                          | analog and digital clocks  | • telling time from analog and digital clock to the nearest           |  |
|  | <ul> <li>time to the nearest five minutes</li> </ul>             | five minutes, using a.m. and p.m.                                     |  |
|  | am. and pm.  | <ul> <li>writing time from analog and digital clock to the</li> </ul> |  |
|  | • names and value of quarters, nickels, pennies,                 | nearest five minutes, using a.m. and p.m.                             |  |
|  | dimes, dollar bills  | Determining the total amount of a collection of various               |  |
|  | dollar and cent symbols  | coins (half dollars, quarters, dimes, nickels, pennies).              |  |
|  |  | showing an amount several different ways using                        |  |
|  |  | quarters, dimes, nickels and pennies.                                 |  |
|  |  | solving word problems involving dollar bills and coins.               |  |
| Used in Content Area Standards                   |  | 21 <sup>st</sup> Century Skills                                       |  |

|                | • | Problem Solving |
|----------------|---|-----------------|
| not applicable | • | Communication   |
|                | • | Perseverance    |
|                |   |                 |

| Stage 2 - Evidence                      |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence |  |  |
|   | ASSESSMENT: Written Assessments or Projects                                  |  |
|   | Other Evidence: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 2 Unit 2: Addition & Subtraction Within 20

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|---------|--------|------|------|
| E.3 I A | опоп   | こいけい | ALD. |
|         |        |      |      |

Students will continue their study of mathematics. In this unit, students will use addition and subtraction strategies to solve problems in everyday life.

#### Content Standards:

- 2.OA.A.1. Use addition and subtraction within 100 to solve one- and two-step word problems involving situations of adding to, taking from, putting together, taking apart, and comparing with unknowns in all positions; e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.
- 2.OA.B.2. Fluently add and subtract within 20 using mental strategies. By the end of Grade 2, know from memory all sums of two one-digit numbers.
- 2.OA.C.3 Determine whether a group of objects (up to 20) has an odd or even number of members, e.g., by pairing objects or counting them by 2s; write an equation to express an even number as a sum of two equal addends.
- 2.OA.C.4 Use addition to find the total number of objects arranged in rectangular arrays with up to 5 rows and up to 5 columns; write an

## **Stage 1 Desired Results**

#### Transfer

Students will be able to independently use their learning to...

use addition and subtraction strategies to solve problems in everyday life.

#### Meaning

#### ENDURING UNDERSTANDINGS

 There are strategies for learning addition and subtraction facts within 20 that will help with fluency. This includes counting on, making ten, and decomposing.

#### ESSENTIAL QUESTIONS

- How would life be different if we couldn't add or subtract?
- Why is being able to add and subtract important?
- What would happen if you could only add, and not subtract?

#### **Acquisition**

#### Students will understand...

- how to identify the sum and difference in addition and subtraction equations.
- fact families are a group of four facts using the same three numbers.
- whether a number is odd or even
- how to arrange objects into arrays and write equations that represent the array

- Solving one- and two- step problems using addition and subtraction within 20 with unknowns in all positions.
- demonstrating fluency of addition and subtraction facts within 20., using mental math strategies.
- writing fact families that consist of 2 addition and 2 subtraction equations using 3 numerals.
- arranging objects in rectangular arrays with up to 5 rows and 5 columns and writing an equation to express the total as a sum of equal addends.

| equation to express the total as a sum of equal addends. |                                 |
|--|---------------------------------|
| Used in Content Area Standards                           | 21 <sup>st</sup> Century Skills |
|  | Problem solving                 |
| not applicable   | Communication                   |
|  | Perseverance                    |
|  |                                 |

| Stage 2 - Evidence  |  |
|---------------------|--|
| Evaluative Criteria | Assessment Evidence  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |

### Windham School District Curriculum Mathematics - Grade 2 Unit 3: Addition & Subtraction For Larger units

| רכז | - A D | 110 | וור | - | ۸۱۲۰ |
|-----|-------|-----|-----|---|------|
|     |       |     |     |   |      |

Students will continue their study of mathematics. In this unit, students will add and subtract within 100, and 1000 using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.

### Content Standards:

- CCSS.2 NBT.B.5. Fluently add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.
- CCSS.2 NBT.B.6. Add up to four two-digit numbers using strategies based on place value and properties of operations.
- CCSS.2.NBT.B.7 Add and subtract within 1000, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method. Understand that in adding or subtracting three-digit numbers, one adds or subtracts hundreds and hundreds, tens and tens, ones and ones; and sometimes it is necessary to compose or decompose tens or hundreds.

### **Stage 1 Desired Results**

### Students will be able to independently use their learning to...

add and subtract within 100, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction

Transfer

 add and subtract 3-digit numbers using a variety of strategies such as the standard algorithm, mental math or partial sums.

### Meaning

### ENDURING UNDERSTANDINGS

- Two digit numbers can be broken apart using tens and ones and added in different ways.
- Three-digit numbers can be broken apart using hundreds, tens, and ones and added in different ways.

### **ESSENTIAL QUESTIONS**

- How do we understand place value and use properties of operations to add and subtract?
- How does the position of a digit in a number affect its value?

### Acquisition

### Students will understand...

- a variety of strategies to add and subtract.
- how to compose and decompose 2 and 3-digit numbers to add and subtract.
- place value
- properties of operations of addition and subtraction

- adding and subtracting numbers within 100 using place value strategies.
- breaking apart numbers into tens and ones to find their sums and differences.
- explaining their mathematical thinking.
- adding up to four 2-digit numbers
- understanding addends can be added in any order.
- adding 10 or 100 mentally using place value

| <ul> <li>CCSS.2.NBT.B.8 Mentally add 10 or 100 to a given number 100-900 and mentally subtract 10 or 100 from a given number 100-900.</li> <li>CCSS.2.NBT.B.9 Explain why addition and subtraction strategies work, using place value and the properties of operations.</li> </ul> | <ul> <li>adding 3 digit numbers using a variety of<br/>strategies such as adding partial sums,<br/>compensation, traditional algorithms and<br/>mental math.</li> </ul> |
|--|---|
| Used in Content Area Standards   | 21st Century Skills   |
| not applicable   | <ul><li>Problem Solving</li><li>Communication</li><li>Perseverance</li></ul>  |

| Stage 2 - Evidence                      |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence |  |  |
|   | ASSESSMENT: Written Assessments or Projects                                  |  |
|   | Other Evidence: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 2 Unit 4: Representing & Interpreting Data

|   | Stage 1 Desired Resul                                      | ts  |  |
|---|--|---|--|
| ESTABLISHED GOALS:                                | Transfer   |   |  |
| Students will continue their study of             | Students will be able to independently use                 | their learning to   |  |
| mathematics. In this unit, students will use data | <ul> <li>use data and graphs to make decisions</li> </ul>  | and solve problems.   |  |
| and graphs to make decisions and solve            |  | Meaning   |  |
| problems.   | ENDURING UNDERSTANDINGS                                    | ESSENTIAL QUESTIONS   |  |
| Content Standards:                                | <ul> <li>Some questions can be answered by</li> </ul>      | Why is graphing important?  |  |
| • CCSS.2. MD 9. Generate measurement data         | collecting and analyzing data.                             | <ul><li>Is one graph better than another?</li></ul>               |  |
| by measuring lengths of several objects to        | <ul> <li>Data can be represented visually using</li> </ul> | <ul> <li>How do graphs help us learn about our world?</li> </ul>  |  |
| the nearest whole unit, or by making              | charts and graphs.   |   |  |
| repeated measurements of the same object.         |  |   |  |
| Show the measurements by making a line            | Acquisition  |   |  |
|   | Students will understand                                   | Students will be skilled at                                       |  |
| off in whole-number units.                        | <ul> <li>Data represents real world objects and</li> </ul> | Drawing a picture graph and a bar graph (with single-unit)        |  |
| • CCSS.2. MD 10. Draw a picture graph and a       | ideas.   | scale) to represent a data set with up to four categories. (Fall, |  |
| bar graph (with single-unit scale) to             |  | Winter, Spring, Summer).  |  |
| represent a data set with up to four              |  | Solving simple addition, subtraction, and comparing word          |  |
| categories. Solve simple put-together, take-      |  | problems using information presented in a bar graph and a         |  |
| apart, and compare problems using                 |  | picture graph.  |  |
| information presented in a bar graph.             |  | Collecting measurement data by measuring lengths of several       |  |
|   |  | objects to the nearest whole unit and showing the                 |  |
|   |  | measurements by making a line plot, where the horizontal          |  |
|   |  | scale is marked off in whole-number units.                        |  |
| Used in Content Area Standards                    |  | 21 <sup>st</sup> Century Skills                                   |  |
|   |  | Problem solving   |  |
| not applicable                                    |  | Communication   |  |
|   |  | Perseverance  |  |

| Stage 2 - Evidence                      |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence |  |  |
|   | ASSESSMENT: Written Assessments or Projects                                  |  |
|   | Other Evidence: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 2 Unit 5: Geometry

|   | Stage 1 Desired Results   |   |
|---|---|---|
| ESTABLISHED GOALS:  | Trai  | nsfer   |
| Students will continue their study of mathematics. In   | Students will be able to independently use their lea  | rning to  |
| this unit, students will be able to identify shapes in the  | <ul> <li>identify shapes in the world around them based</li> </ul>  | d on their attributes .   |
| world around them based on their attributes and also  | <ul> <li>divide wholes into equal shares.</li> </ul>  |   |
| be able to divide wholes into equal shares.   | Med   | aning   |
|   | ENDURING UNDERSTANDINGS   | ESSENTIAL QUESTIONS   |
| Content Standards:  | Two-and-three-dimensional objects have  | <ul> <li>How can geometry be used to solve problems?</li> </ul>   |
| CCSS.2.G.1. Recognize and draw shapes having  | unique attributes.  | <ul> <li>How does understanding shapes help you to</li> </ul>   |
| specified attributes, such as a given number of   | <ul> <li>A shape can be divided into equal sized parts.</li> </ul>  | build?  |
| angles or a given number of equal faces. Identify   |   | How can you prove that something is divided   |
| triangles, quadrilaterals, pentagons, hexagons, and   |   | equally?  |
| cubes.  | Acqu  | isition   |
| <ul> <li>CCSS.2.G.2. Partition a rectangle into rows and columns of same-size squares and count to find the total number of them</li> <li>CCSS.2.G.3. Partition circles and rectangles into two, three, or four equal shares, describe the shares using the words halves, thirds, half of, a third of, etc., and describe the whole as two halves, three thirds, four fourths. Recognize that equal shares of identical wholes need not have the same shape.</li> </ul> | <ul> <li>Students will understand</li> <li>attributes of 2-D shapes (angles, sides, and vertices)</li> <li>attributes of 3-D shapes (angles, vertices, faces)</li> <li>2-D shapes can be divided into equal shares (halves, thirds, fourths).</li> <li>The names of shapes are based on their attributes</li> </ul> | <ul> <li>Students will be skilled at</li> <li>recognizing the specified attributes of shapes, such as a given number of angles or a given number of equal faces.</li> <li>drawing shapes with specified attributes, such as a given number of angles or a given number of equal faces.</li> <li>identifying triangles, quadrilaterals, pentagons, hexagons, cubes, pyramids, cones, and cylinders.</li> <li>dividing a rectangle into rows and columns of same-size squares.</li> </ul> |
|   |   |   |

|                                | <ul> <li>counting the same-size squares within the rows and columns to find the total number of squares.</li> <li>dividing circles and rectangles into two, three or four equal shares and describing the equal shares as halves, thirds, fourths respectively.</li> <li>describing the whole as two halves, three thirds, four fourths, etc.</li> <li>recognizing that equal shares of identical wholes need not have the same shape.</li> </ul> |
|--------------------------------|---|
| Used in Content Area Standards | 21 <sup>st</sup> Century Skills   |
| not applicable                 | <ul> <li>Problem Solving</li> <li>Communication</li> </ul>  |
| пос аррпсавіс                  | Perseverance  |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | Other Evidence: independent practice, classroom observations and discussions |  |

### Windham School District Curriculum Mathematics - Grade 2 Unit 6: Measurement

|   | offic of Micasar Cilicit   |  |
|---|--|--|
|   | Stage 1 Desired Results  |  |
| ESTABLISHED GOALS:                                    | Tran   | nsfer  |
| Students will continue their study of mathematics. In | Students will be able to independently use their learning to         |  |
| this unit, students will be able to use their         | <ul> <li>use their understanding of measuring tools to n</li> </ul>  | neasure objects.   |
| understanding of measuring tools to measure objects.  | Mea  | ning   |
|   | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS  |
| Content Standards:                                    | Some attributes of objects are measurable and                        | What would life be like if standard units of                       |
| CCSS.2.MD. 1 Measure the length of an object by       | can be quantified using unit amounts.                                | measurement did not exist?   |
| selecting and using appropriate tools such as         | Objects can be measured using multiple units                         | <ul> <li>How does what we measure affect what we use</li> </ul>    |
| rulers, yardsticks, meter sticks, and measuring       | of measurements.   | to measure?  |
| tapes.  |  |  |
| CCSS.2.MD. 2. Measure the length of an object         | Acquisition  |  |
|   | Students will understand   | Students will be skilled at  |
| the two measurements; describe how the two            | Use the appropriate tool for measuring objects                       | <ul> <li>measuring the length of an object twice, using</li> </ul> |
| measurements relate to the size of the unit           | is important for accuracy.   | two different units of measure, and describing                     |
| chosen.   | Measurements can be compared.  | how the two measurements relate to the size                        |
| CCSS.2.MD. 3 Estimate lengths using units of          | <ul> <li>similarity between a measuring tool and a</li> </ul>        | of the unit chosen. estimating lengths using                       |
| inches, feet, centimeters, and meters.                | number line.   | units of inches, feet, centimeters, and meters.                    |
| CCSS.2.MD. 4. Measure to determine how much           | <ul> <li>how to use rulers, yardsticks, meter sticks, and</li> </ul> | <ul> <li>Estimating the length of an object using</li> </ul>       |
| longer one object is than another, expressing the     | measuring tapes to measure objects.                                  | appropriate units for that object.                                 |
| length difference in terms of a standard-length       |  | measuring to determine how much longer one                         |
| unit.   |  | object is than another.  |
| CCSS.2.MD.B5 Use addition and subtraction within      |  | expressing the differences in length in terms of                   |
| 100 to solve word problems involving lengths that     |  | a standard length unit.  |
| are given in the same units, e.g., by using drawings  |  | <ul> <li>using addition and subtraction within 100 to</li> </ul>   |
| (such as drawings of rulers) and equations with a     |  | solve word problems involving lengths that are                     |
|   |  | given in the same unit by using drawings and                       |

| <ul> <li>CCSS.2.MD.B6 Represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the numbers 0, 1, 2, and represent whole-number sums and differences within 100 on a number line diagram.</li> </ul> | <ul> <li>number to represent the problem.</li> <li>representing whole numbers as lengths from 0 on a number line with equally spaced points corresponding to the numbers 0, 1, 2 and represent whole number sums and differences within 100 on a number line.</li> <li>generating measurement data by measuring lengths of several objects to the nearest whole unit or by making repeated measurements of the same object.</li> </ul> |
|---|--|
| Used in Content Area Standards  | 21st Century Skills  |
| not applicable  | <ul><li>Problem solving</li><li>Communication</li><li>Perseverance</li></ul>   |

| Stage 2 - Evidence  |  |
|---------------------|--|
| Evaluative Criteria | Assessment Evidence  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |
|                     | Other Evidence: independent practice, classroom observations and discussions |

### Windham School District Curriculum Mathematics - Grade 2 Unit 7: Place Value

| ESTABLISHED GOALS: | : |
|--------------------|---|
|--------------------|---|

Students will continue their study of mathematics. In this unit, students will understand the significance of ordering numbers in ones, tens, hundreds and thousands. Students will use place value to solve problems more efficiently.

### Content Standards:

- 2.NBT.A.1. Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones; e.g., 706 equals 7 hundreds, 0 tens, and 6 ones. Understand the following as special cases:
- 100 can be thought of as a bundle of ten tens called a "hundred".
- The numbers 100, 200, 300, 400, 500, 600 700, 800, 900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones).
- 2.NBT.A.2. Count within 1000; skip-count by 5s, 10s, and 100s.
- 2.NBT.A.3. Read and write numbers to 1000 using base-ten numerals, number names, and expanded form.
- 2.NBT.A.4. Compare two three-digit numbers based on meanings of the hundreds, tens, and

### **Stage 1 Desired Results**

### Students will be able to independently use their learning to...

- understand the significance of ordering numbers in ones, tens, hundreds and thousands.
- use place value to solve problems more efficiently.

### Meaning

Transfer

### ENDURING UNDERSTANDINGS

- The value of a number can be determined by the place value of the number.
- Place value can be used to compare and order numbers.

### **ESSENTIAL QUESTIONS**

- How does the value of a digit change when it is moved from one place value to another?
- Why is the number zero important in place value?

### **Acauisition**

### Students will understand...

- value of a digit based on its position in a multidigit number
- Numbers can be represented using number names, base ten blocks, expanded form and numerals.
- Numbers can be compared using symbols
- The number 100 can be thought of as a bundle of ten 10s.

- Representing 3 digit numbers using models, words, and numbers.
- Identifying and understanding the value of digits in the hundreds, tens, and ones places
- Skip-counting to 1000 by 5s, 10s and 100s.
- Identify the hundreds, tens and ones place in a 3 digit number.
- Writing a 3-digit number using expanded notation.
- Comparing the value of two three-digit numbers.

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |

### <u>Title of Curriculum</u>: Grade 3 Mathematics

| Multiplication and Division  Pequal groups Relationship between multiplication and division Equal groups Array Commutative Property Associative Property Identity Property Identity Products Products Products Unknown Equation Poperation  Multiplication & Division Math Fact Fluency  Multiplication is the number of objects in a number of equal groups.  Multiplication is the number of objects in a number of equal groups and patterns for modelling.  Author and division can be regresented by fair share or equal groups situations. Unknowns can be used in all positions when solving problems. Multiplication and division have an inverse relationship and can be used to solve problems and check answers.  Author and division have an inverse relationship and can be used to solve problems and check answers.  Author and division have an inverse relationship and can be used to solve problems and check answers.  Author and division have an inverse relationship and can be used to solve problems and check answers.  Author and division have an inverse relationship and can be used to solve problems and check answers.  Author and division have an inverse relationship and can be used to solve problems and check answers.  Author and division have an inverse relationship and can be used to solve problems and check answers.  Author and division have an inverse relationship and can be used to solve problems and check answers.  Author and division have an inverse relationship and can be used to solve problems and check answers.  Author and division have an inverse relationship and can be used to solve problems and check answers.  Author and division have an inverse relationship and can be used to solve problems and check answers.  Author and division have an inverse relationship and can be used to solve problems and check answers.  Author and division facts of the unknown whole number in a multiplication facts to solve division facts of the unknown whole number in a multiplication facts of the unknown whole number in a multiplication facts  | Unit Name            | What (content, vocab)                    | Why (enduring understandings)         | How (skills)  |
|--|----------------------|--|---------------------------------------|---|
| Relationship between multiplication and division  Equal groups Array Commutative Property Associative Property Identity Property Identity Property Products Unknown Equation Products Unknown Equation Products Unknown Equation Properts Operation  Multiplication & Division Math Fact Fluency  Multiplication is repeated addition.  multiplication is repeated addition. multiplication is the number of objects in a number of equal groups.  Place Value  Relationship between multiplication and division patterns for modeling. Division can be represented by fair share or equal groups situations. Division can be represented by fair share or equal groups situations. Division can be represented by fair share or equal groups situations. Unknowns can be used in all positions have an inverse relationship and can be used to solve problems.  Multiplication and division have an inverse relationship and can be used to solve problems and check answers.  Multiplication and division have an inverse relationship and can be used to solve problems and check answers.  Multiplication facts to solve division facts of to 10 with accuracy and fluency Use multiplication facts to solve division facts Solve one and two-step word problems using all four operations  Automaticity of multiplication facts O-10 is beneficial when learning other computations in mathematics.  Apply properties of operations as strategies to multiply (e.g. manipulatives, pictures, other facts they know).  Apply properties of operations and division on division have an inverse relationship and can be used to solve problems.  Apply properties of operations of operations of operations of on multiplication facts of to multiplication facts of possible multiplication facts of possible multiplication facts of possible multiplication facts of operations of opera | Multiplication and   | Multiplication                           | There are many strategies for         | Use repeated addition of equal groups to                            |
| multiplication and division  | Division             | <ul> <li>Repeated addition</li> </ul>    | multiplication including repeated     | multiply.   |
| Equal groups     Array     Commutative Property     Associative Property     Distributive Property     Identity Properties of operations as strategies to multiplication for builtiplication on the unknown whole number in a multiplication of acts or solve division facts or solve divisio      |                      | <ul> <li>Relationship between</li> </ul> | addition of equal groups, arrays and  | Use patterns to multiply with different                             |
| Array     Commutative Property     Associative Property     Distributive Property     Identity Property     Identity Property     Zero Property     Patterns     Factors     Products     Unknown     Equation     Operation  Multiplication & Division Math Fact Fluency  Place Value  Place Value  Array  Share or equal groups situations.  Unknowns can be used in all positions when solving problems and langorithms and division have an inverse relationship and can be used to solve problems and check answers.  Multiplication and division have an inverse relationship and can be used to solve problems and check answers.  Multiplication & Division Math Fact Fluency  Place Value  Array  Share or equal groups situations.  Unknowns can be used in all positions when solving problems.  Multiplication and division have an inverse relationship and can be used to solve problems and check answers.  Multiplication and division and division facts of the position of acts      |                      | multiplication and division              | patterns for modeling                 | factors.  |
| Commutative Property     Associative Property     Distributive Property     Identity Property     Identity Property     Patterns     Products     Products     Unknown     Equation     Operation  Multiplication & Division Math Fact Fluency  Place Value  Place Value  Place Value  Positions when solving problems.  Multiplication and division have an inverse relationship and can be used to solve problems and check answers.  Multiplication and division have an inverse relationship and can be used to solve problems and check answers.  Multiplication and check answers.  Automaticity of multiplication facts O-10 is beneficial when learning other computations in mathematics.  Multiplication is the number of objects in a number of equal groups.  Place Value  Place Value  Positions when solving problems.  Multiplication have an inverse relationship and can be used to solve groblems.  Multiplication and division have an inverse relationship and can be used to solve problems and check answers.  Multiplication and division or division equation Show mastery of all multiplication facts on the learning of all four operations  Patterns  Automaticity of multiplication facts O-10 is beneficial when learning other computations in mathematics.  Automaticity of multiplication facts O-10 is beneficial when learning other computations in mathematics.  Automaticity of multiplication facts O-10 is beneficial when learning other computations in mathematics.  Use multiplication facts to solve division facts.  Solve one and two-step word problems using all four operations  Use multiplication facts to solve division facts.  Solve one and two-step word problems using all four operations  Use multiplication facts to solve division facts.  Solve one and two-step word problems using all four operations  Use multiplication facts to solve division facts.  Solve one and two-step word problems using all four operations  Use multiplication facts to solve division facts.  Understanding for the fact of the multiplication facts of the multiplicatio      |                      | <ul><li>Equal groups</li></ul>           | · · · · · · · · · · · · · · · · · · · | <ul> <li>Use strategies to multiply (e.g. manipulatives,</li> </ul> |
| Associative Property Distributive Property Identity Property Patterns Products Unknown Equation Operation Multiplication & Division Math Fact Fluency  Place Value  Place Value  Associative Property Distributive and Associative, Property). Multiplication when solving problems. Multiplication and division have an inverse relationship and can be used to solve problems and check answers.  Multiplication and division have an inverse relationship and can be used to solve problems and check answers.  Automaticity of multiplication facts of to 10 with accuracy and fluency Use multiplication facts to solve division facts of to 10 with accuracy and fluency Use multiplication facts to solve division facts of the solve division facts of the solve division facts of the computations in mathematics.  Automaticity of multiplication facts of mathematics.  Automaticity of multiplication facts of the computations in mathematics.  Automaticity of multiplication facts of mathematics.  Automaticity of multiplication facts of the computations in mathematics.  Automaticity of multiplication facts of mathematics.  Automaticity of multi |                      | •  | , , ,                                 | 1 ' ' '   |
| Distributive Property Identity Identity of Multiplication and check answers Identity Identit  |                      | . ,                                      |                                       |   |
| <ul> <li>Identity Property         <ul> <li>Zero Property</li> <li>Patterns</li> <li>Factors</li> <li>Products</li> <li>Unknown</li> <li>Equation</li> <li>Operation</li> </ul> </li> <li>Multiplication &amp; Division Math Fact Fluency</li> <li>Products of multiplication: commutative, associative, and distributive.</li> <li>relationship between multiplication is the number of objects in a number of equal groups.</li> <li>Place Value</li> <li>Identity Property         <ul> <li>Zero Property</li> <li>used to solve problems and can be used to solve problems and check answers.</li> <li>Inverse relationship and can be used to solve problems and check answers.</li> </ul> </li> <li>Determine the unknown whole number in a multiplication of division equation</li> <li>Show mastery of all multiplication facts to solve division facts</li> <li>Solve one and two-step word problems using all four operations</li> <li>Use multiplication facts to solve division facts.</li> <li>Show a mastery of all multiplication facts to solve division facts.</li> <li>Show a mastery of all multiplication facts of the properties of multiplication facts.</li> </ul> <li>Place Value</li> <li>Identity Property         <ul> <li>Automaticity of multiplication facts</li> <li>O-10 is beneficial when learning other computations in mathematics.</li> <li>Show a mastery of all multiplication facts of the properties of multiplication facts of multi</li></ul></li>  |                      | • •                                      | •                                     | , ,   |
| Zero Property     Patterns     Patterns     Products     Unknown     Equation     Operation      Multiplication & Division Math Fact Fluency  Products     relationship between multiplication and division.     multiplication is the number of objects in a number of equal groups.  Place Value  Patterns  Products  Automaticity of multiplication facts of multiplication facts of to solve division equation Show mastery of all multiplication facts of to 10 with accuracy and fluency  Use multiplication or division equation Show mastery of all multiplication facts of solve division facts of multiplication facts of multiplicatio      |                      | • • •                                    |                                       | , ,,  |
| Patterns Factors Products Division Math Fact Fluency  Multiplication and division. In multiplication is repeated addition. In multiplication is the number of objects in a number of equal groups.  Place Value  Products Parallelier Products Push rectancy of all multiplication facts 0 to 10 with accuracy and fluency Place Value Place Val |                      | · · · ·                                  |                                       |   |
| Factors Products Duknown Equation Operation  Multiplication & Division Math Fact Fluency  Multiplication and division. In multiplication is repeated addition.  Multiplication is the number of objects in a number of equal groups.  Place Value  Place Value  Products Duk multiplication facts to solve division facts Solve one and two-step word problems using all four operations  Automaticity of multiplication facts O-10 is beneficial when learning other computations in mathematics.  Automaticity of multiplication facts of outliplication facts of understanding place value is an important strategy for developing  10 with accuracy and fluency  Use multiplication facts to solve division facts of understanding place value is an important strategy for developing  10 with accuracy and fluency  Use multiplication facts to solve division facts of understanding place value is an important strategy for developing  Place Value  10 with accuracy and fluency  Use multiplication facts to solve division facts of understanding place value is an important strategy for developing  Nutriciplication facts to solve division facts of understanding place value is an important strategy for developing  Place Value  Place Value  Nutriciplication facts to solve division facts of understanding place value is an important strategy for developing  |                      | · ,                                      | -                                     | · ·   |
| <ul> <li>Products</li> <li>Unknown</li> <li>Equation</li> <li>Operation</li> <li>Multiplication &amp; Division Math Fact Fluency</li> <li>Prelationship between multiplication and division.</li> <li>multiplication is repeated addition.</li> <li>multiplication is repeated addition.</li> <li>multiplication is the number of objects in a number of equal groups.</li> <li>Place Value</li> <li>Products</li> <li>Understanding place value is an important strategy for developing</li> <li>Use multiplication facts to solve division facts on the solve division facts.</li> <li>Solve one and two-step word problems using all four operations</li> <li>Use multiplication facts to solve division facts.</li> <li>Show a mastery of all multiplication facts 0 to 10 with accuracy and fluency</li> <li>Negund numbers to nearest ten or hundred.</li> <li>Use rounding in estimating sums and</li> </ul>  |                      |  | answers.                              | ·   |
| <ul> <li>Unknown         <ul> <li>Equation</li> <li>Operation</li> </ul> </li> <li>Multiplication &amp; Division Math Fact Fluency</li> <li>Prelationship between multiplication is repeated addition.</li> <li>multiplication is the number of objects in a number of equal groups.</li> <li>Place Value</li> <li>Unknown         <ul> <li>Equation</li> <li>Automaticity of multiplication facts 0-10 is beneficial when learning other computations in mathematics.</li> <li>Use multiplication facts to solve division facts.</li> <li>Show a mastery of all multiplication facts 0 to 10 with accuracy and fluency</li> </ul> </li> <li>Place Value</li> <li>Ones, tens, hundreds, thousands</li> <li>Round</li> <li>Understanding place value is an important strategy for developing</li> <li>Round numbers to nearest ten or hundred.</li> <li>Use rounding in estimating sums and</li> </ul> <li>Solve one and two-step word problems using all four operations</li> <li>Use multiplication facts</li> <li>Use multiplication facts 0 to 10 with accuracy and fluency</li> <li>Now a mastery of all multiplication facts 0 to 10 with accuracy and fluency</li>   |                      |  |                                       | · · · · · · · · · · · · · · · · · · ·                               |
| <ul> <li>Equation         <ul> <li>Operation</li> </ul> </li> <li>Multiplication &amp; Division</li></ul>  |                      |  |                                       | · · · · · · · · · · · · · · · · · · ·                               |
| Multiplication & Division Math Fact Fluency  Math Fact Fluency  Image: Place Value  Operation  Multiplication & Division Math Fact Fluency  Operation  Automaticity of multiplication facts 0-10 is beneficial when learning other computations in mathematics.  O-10 is beneficial when learning other computations in mathematics.  O-10 is beneficial when learning other computations in mathematics.  Show a mastery of all multiplication facts 0 to 10 with accuracy and fluency  10 with accuracy and fluency  Nome: Place Value  Ones, tens, hundreds, thousands Round  Ones, tens, hundreds, thousands Round  Operation  Automaticity of multiplication facts  O-10 is beneficial when learning other computations in mathematics.  Show a mastery of all multiplication facts 0 to 10 with accuracy and fluency  10 with accuracy and fluency  Nome: Place Value  Ones, tens, hundreds, thousands Important strategy for developing  Round numbers to nearest ten or hundred.  Use rounding in estimating sums and  |                      |  |                                       |   |
| Multiplication & Division Math Fact Fluency  • properties of multiplication: commutative, associative, and distributive. • relationship between multiplication and division. • multiplication is repeated addition. • multiplication is the number of objects in a number of equal groups.  Place Value  • Automaticity of multiplication facts of computations in mathematics. • Automaticity of multiplication facts of computation facts. • Show a mastery of all multiplication facts of to number of addition. • Multiplication is the number of objects in a number of equal groups. • Understanding place value is an important strategy for developing • Round numbers to nearest ten or hundred. • Use rounding in estimating sums and  |                      | •  |                                       | all four operations   |
| Math Fact Fluency  commutative, associative, and distributive.  relationship between multiplication and division.  multiplication is repeated addition.  multiplication is the number of objects in a number of equal groups.  Place Value  commutative, associative, and distributive.  other computations in mathematics.  o | 20 14 11 41 0 21 1 1 |  |                                       |   |
| distributive.  relationship between multiplication and division.  multiplication is repeated addition.  multiplication is the number of objects in a number of equal groups.  Place Value  distributive.  other computations in mathematics.  other computations in mathematics.  10 with accuracy and fluency  nultiplication facts 0 to 10 with accuracy and fluency  10 with accuracy and fluency  No with accuracy and fluency  10 with accuracy and fluency  No with accuracy and fluency  10 with accuracy and fluency  10 with accuracy and fluency  No with accuracy and fluency  10 with accuracy and fluency   | •                    |  | , ,                                   | ·   |
| <ul> <li>relationship between multiplication and division.</li> <li>multiplication is repeated addition.</li> <li>multiplication is the number of objects in a number of equal groups.</li> <li>Place Value</li> <li>Ones, tens, hundreds, thousands</li> <li>Round</li> <li>mathematics.</li> <li>10 with accuracy and fluency</li> <li>Bound number of equal san important strategy for developing</li> <li>Round numbers to nearest ten or hundred.</li> <li>Use rounding in estimating sums and</li> </ul>   | Math Fact Fluency    |  | 9                                     |   |
| multiplication and division.  multiplication is repeated addition.  multiplication is the number of objects in a number of equal groups.  Place Value  Ones, tens, hundreds, thousands Round  Nound  Multiplication is repeated addition.  Multiplication is the number of objects in a number of equal groups.  Multiplication is the number of objects in a number of equal groups.  Multiplication is the number of objects in a number of equal groups.  Multiplication is the number of objects in a number of equal groups.  Multiplication is repeated addition.  Multiplication is repeated addition.  Multiplication is repeated addition.  Multiplication is the number of objects in a number of equal groups.  Multiplication is the number of objects in a number of equal groups.  Multiplication is the number of objects in a number of equal groups.  Multiplication is the number of objects in a number of equal groups.  Multiplication is the number of objects in a number  |                      |  | · ·                                   | , ,   |
| <ul> <li>multiplication is repeated addition.</li> <li>multiplication is the number of objects in a number of equal groups.</li> <li>Place Value</li> <li>Ones, tens, hundreds, thousands</li> <li>Round</li> <li>Understanding place value is an important strategy for developing</li> <li>Round numbers to nearest ten or hundred.</li> <li>Use rounding in estimating sums and</li> </ul>  |                      | •  | matnematics.                          | 10 with accuracy and fluency  |
| addition.  • multiplication is the number of objects in a number of equal groups.  • Ones, tens, hundreds, thousands Round  • Round  • Round numbers to nearest ten or hundred.  • Understanding place value is an important strategy for developing  • Use rounding in estimating sums and  |                      |  |                                       |   |
| <ul> <li>multiplication is the number of objects in a number of equal groups.</li> <li>Place Value</li> <li>Ones, tens, hundreds, thousands Round</li> <li>Round</li> <li>Understanding place value is an important strategy for developing</li> <li>Round numbers to nearest ten or hundred.</li> <li>Use rounding in estimating sums and</li> </ul>  |                      |  |                                       |   |
| objects in a number of equal groups.  Place Value  Ones, tens, hundreds, thousands Round  Nound  Ones, tens, hundreds, thousands important strategy for developing  Output  Description  Round  Output  Description  Round  Output  Description  Round  Output  Description  Output  Description  Output  Description  Output  Description  Description  Output  Description  Output  Description  Description  Output  Description  Output  Description  Output  Description  Description  Output  Description  Output  Description  Description  Description  Output  Description  Description  Description  Output  Description  Desc |                      |  |                                       |   |
| groups.  Place Value  Ones, tens, hundreds, thousands Round  Round  Nones, tens, hundreds, thousands important strategy for developing  Broups.  Understanding place value is an important strategy for developing  Use rounding in estimating sums and  |                      | •  |                                       |   |
| Place Value  Ones, tens, hundreds, thousands Round  Ones, tens, hundreds, thousands important strategy for developing  Round  Round numbers to nearest ten or hundred. Use rounding in estimating sums and   |                      | ,  |                                       |   |
| ● Round important strategy for developing ● Use rounding in estimating sums and  | Place Value          |  | Inderstanding place value is an       | Round numbers to nearest ten or hundred                             |
|  | i lace value         |  | <u> </u>                              |   |
|  |                      |  |                                       | <u> </u>  |
| Multiples subtraction.   |                      |  | ·                                     | ac. c.roco.   |

| Fractions                     | <ul> <li>Numerator and denominator</li> <li>Equal parts</li> <li>Unit Fraction</li> <li>Fraction tiles/ fraction strips</li> <li>Number lines</li> <li>Equivalent fractions</li> <li>Same numerator</li> <li>Same denominator</li> <li>Whole numbers</li> <li>half inch</li> <li>Quarter inch</li> <li>Line plot</li> </ul> | A fraction describes the division of a whole into equal parts. The denominator tells how many equal parts the whole is divided into. The numerator tells how many equal parts are indicated.     | <ul> <li>Draw a number line from 0 to 1, partition it into equal parts and label each part with a fraction.</li> <li>Compare fractions that have the same numerator or fractions that have the same denominator and use &lt;, &gt;, or = by reasoning about their size and using a visual model</li> <li>Generate simple equivalent fractions using a line plot or visual fraction model.</li> <li>Express same numerator and denominator as one whole</li> <li>Represent a unit fraction on a number line</li> <li>Recognize fractions as parts to the whole with an understanding of the numerator and denominator parts.</li> <li>Students will understand how to use a ruler to measure lengths to the nearest half and quarter inch.</li> </ul> |
|-------------------------------|---|--|--|
| Measurement and Data:<br>Time | <ul> <li>Minute hand</li> <li>Hour hand</li> <li>AM and PM</li> <li>5 minute intervals</li> <li>Half past</li> <li>Quarter past</li> <li>Quarter of</li> <li>1 minute intervals</li> </ul>  | <ul> <li>Time can be measured using different units that are related to one another.</li> <li>The minute hand takes 5 minutes to move from one number to the next on a typical clock.</li> </ul> | <ul> <li>Tell time to the nearest minute.</li> <li>Solve problems using addition and subtraction of time intervals in minutes on a number line</li> </ul>  |

|   | Elapsed time (shown on numbe line, clock, or paper)   | r   |  |
|---|---|---|--|
| Measurement and Data:<br>Area and Perimeter | <ul> <li>Area</li> <li>Unit square</li> <li>Perimeter</li> <li>Square units</li> <li>Units</li> <li>Length x Width</li> <li>Distributive Property</li> </ul>  | <ul> <li>Perimeter and area are attributes of plane figures.</li> <li>Area is application of multiplication</li> <li>Perimeter is an application of addition</li> <li>There is a distinct difference between area and perimeter and how they are measured.</li> </ul> | Find area of a rectangle by using  |
| Measurement and Data:<br>Mass and Volume    | <ul> <li>Liquid volume/ capacity</li> <li>Mass</li> <li>Grams and kilograms</li> <li>Milliliters and liters</li> </ul>  | <ul> <li>Capacity is a measure of the amount of liquid a container can hold.</li> <li>Mass is a measure of the quantity of matter in an object. Weight and mass are different.</li> </ul>   | <ul> <li>Measure and estimate liquid volumes and masses of objects using standard units.</li> <li>Solve one-step word problems involving any operation using mass and volume given in the same units.</li> </ul> |
| Geometry: Shapes and<br>Attributes          | <ul> <li>Polygon (closed shapes)</li> <li>Attributes</li> <li>Side</li> <li>Angle, vertex</li> <li>Parallel sides</li> <li>Quadrilateral</li> <li>Rectangle, square, rhombus, parallelogram, trapezoid</li> <li>Category/ Categorize</li> </ul> | <ul> <li>There are many types of<br/>quadrilaterals including rhombuses,<br/>rectangles, and squares.</li> <li>Shapes are categorized based on<br/>attributes they share.</li> </ul>  | <ul> <li>Identify types of quadrilaterals by their attributes (rhombuses, rectangles, and squares as examples of quadrilaterals.)</li> <li>Categorize shapes based on attributes they share.</li> </ul>          |

| Measurement and Data:  | Bar graph                | <ul> <li>Some problems can be solved by</li> </ul> | • Use bar graphs and picture graphs, to answer             |
|------------------------|--------------------------|--|--|
| Picture Graphs and Bar | Picture Graph            | making, reading, and analyzing a                   | questions and solve problems.                              |
| Graphs                 | Data                     | graph.   | Draw a bar graph or picture graph, with given              |
|                        | Scale                    |  | data.  |
|                        | • Key                    |  | <ul> <li>Generate measurement data by measuring</li> </ul> |
|                        | <ul><li>Survey</li></ul> |  | lengths using rulers marked with halves and                |
|                        | Tally marks              |  | fourths of an inch.  |

### Windham School District Curriculum Mathematics - Grade 3 Unit 1: Multiplication & Division

### Stage 1 Desired Results

### ESTABLISHED GOALS:

Students will continue their study of mathematics. In this unit, students will represent and solve problems involving multiplication and division.

### Content Standards:

- CCSS.MATH.CONTENT.3.OA.A.1: Interpret products of whole numbers, e.g., interpret 5 × 7 as the total number of objects in 5 groups of 7 objects each.
- CCSS.MATH.CONTENT.3.OA.A.2: Interpret whole-number quotients of whole numbers, e.g., interpret 56 ÷ 8 as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each.
- CCSS.MATH.CONTENT.3.OA.A.3: Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.1
- CCSS.MATH.CONTENT.3.OA.A.4: Determine the unknown whole number in a multiplication or division equation relating three whole numbers.
- CCSS.MATH.CONTENT.3.OA.B.5: Apply properties of operations as strategies to multiply and divide.

### Transfer

### Students will be able to independently use their learning to...

- understand what multiplication is and how to represent it.
- understand what division is and how to represent it.
- solve multiplication and division facts using the strategies and properties.

### Meaning

### ENDURING UNDERSTANDINGS

- There are many strategies for multiplication including repeated addition of equal groups, arrays and patterns for modeling..
- Division can be represented by fair share or equal groups situations.
- Unknowns can be used in all positions when solving problems.
- Multiplication and division have an inverse relationship and can be used to solve problems and check answers.

### **ESSENTIAL QUESTIONS**

- What are different meanings of multiplication?
- What patterns can be found in multiplication?
- What are different meanings of division?
- How is division related to other operations?

### Acquisition

### Students will understand...

- properties of multiplication: commutative, associative, and distributive.
- relationship between multiplication and division.
- multiplication is repeated addition.

- Use repeated addition of equal groups to multiply.
- Use patterns to multiply with different factors.

| not applicable   |   |  | • | Problem solving Communication Perseverance  |
|--|---|--|---|---|
| <ul> <li>Grade 3, know from memory all products of two one-digit numbers.</li> <li>CCSS.MATH.CONTENT.3.OA.D.8: Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.</li> <li>CCSS.MATH.CONTENT.3.OA.D.9: Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations.</li> </ul> |   |  | • | Associative Property).  Determine the unknown whole number in a multiplication or division equation Show mastery of all multiplication facts 0 to 10 with accuracy and fluency Use multiplication facts to solve division facts  Solve one and two-step word problems using all four operations |
| <ul> <li>CCSS.MATH.CONTENT.3.OA.B.6: Understand division as an unknown-factor problem.</li> <li>CCSS.MATH.CONTENT.3.OA.C.7: Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that 8 × 5 = 40, one knows 40 ÷ 5 = 8) or properties of operations. By the end of</li> </ul>   | • | multiplication is the number of objects in a number of equal groups. | • | Use strategies to multiply (e.g. manipulatives, pictures, other facts they know).  Apply properties of operations as strategies to multiply and divide (Commutative, Distributive and   |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Mathematics - Grade 3 Unit 2: Multiplication & Division Math Fact Fluency

|   | Stage 1 Desired Results  |   |  |
|---|--|---|--|
| ESTABLISHED GOALS:  | Transfer   |   |  |
| Students will continue their study of mathematics. In           | Students will be able to independently use their lea             | rning to  |  |
| this unit, students will fluently multiply and divide           | Master multiplication facts within 100                           |   |  |
| within 100.   | <ul> <li>Use multiplication to solve division facts</li> </ul>   |   |  |
|   | Med  | ning  |  |
| Content Standards:  | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS   |  |
| CCSS.MATH.CONTENT.3.OA.C.7: Fluently multiply                   | <ul> <li>Automaticity of multiplication facts 0-10 is</li> </ul> | Why do we need to know math facts?                                      |  |
| and divide within 100, using strategies such as the             | beneficial when learning other computations in                   |   |  |
| relationship between multiplication and division                | mathematics.   |   |  |
| (e.g., knowing that $8 \times 5 = 40$ , one knows $40 \div 5 =$ |  |   |  |
| 8) or properties of operations. By the end of Grade             | Acquisition Acquisition  |   |  |
|   | Students will understand   | Students will be skilled at   |  |
| digit numbers.  | Multiplication facts 0 - 10                                      | <ul> <li>using multiplication facts to solve division facts.</li> </ul> |  |
|   |  | stating all multiplication facts 0 to 10 with                           |  |
|   |  | accuracy and fluency  |  |
| Used in Content Area Standards                                  |  | 21 <sup>st</sup> Century Skills   |  |
| not applicable  |  | Perseverance  |  |
|   |  | Communication   |  |
|   |  |   |  |

| Stage 2 - Evidence                          |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence     |  |  |
| ASSESSMENT: Written Assessments or Projects |  |  |
|   | Other Evidence: independent practice, classroom observations and discussions |  |

### Windham School District Curriculum Mathematics - Grade 3 Unit 3: Place Value

|   | Stage 1 Desired Results  |  |  |  |
|---|--|--|--|--|
| ESTABLISHED GOALS:  | Transfer   |  |  |  |
| Students will continue their study of mathematics. In                                       | Students will be able to independently use their lea                 | rning to   |  |  |
| this unit, students will use place value to add and   | <ul> <li>Multiply one-digit numbers by multiples of 10 in</li> </ul> | n the range of of 10 to 90                                     |  |  |
| subtract within 1,000. Students will round to the   | <ul> <li>Estimate answers to check for accuracy and unc</li> </ul>   | derstanding.   |  |  |
| nearest 10 and 100 and use that to estimate sums and  | Med  | aning  |  |  |
|   | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS  |  |  |
| by multiples of 10 in the range of 10 - 90.   | Understanding place value is an important                            | Why is estimation useful?                                      |  |  |
|   | strategy for developing proficiency in addition                      | How does place value affect estimation?                        |  |  |
| Content Standards:  | and subtraction.   | Why is estimation used in our everyday lives?                  |  |  |
| • CCSS.MATH.CONTENT.3.NBT.A.1: Use place value  |  | When is adding and subtraction two and three-                  |  |  |
| understanding to round whole numbers to the   |  | digit numbers useful in our everyday lives?                    |  |  |
| nearest 10 or 100.  | Acquisition  |  |  |  |
|   | Students will understand   | Students will be skilled at                                    |  |  |
| CCSS.MATH.CONTENT.3.NBT.A.2: Fluently add and     where the within 1000 values attracts and | <ul> <li>rounding of two-digit and three-digit whole</li> </ul>      | multiplying one-digit whole numbers by                         |  |  |
| subtract within 1000 using strategies and   | numbers .  | multiples of 10 in the range 10 to 90.                         |  |  |
| algorithms based on place value, properties of  | <ul> <li>regrouping for multi-digit arithmetic.</li> </ul>           | <ul> <li>rounding numbers to the nearest ten or</li> </ul>     |  |  |
| operations, and/or the relationship between   | place value  | hundred (up to 1,000)  |  |  |
| addition and subtraction.   |  | <ul> <li>rounding when estimating sums and</li> </ul>          |  |  |
| CCSS.MATH.CONTENT.3.NBT.A.3: Multiply one- digit whole graphers by multiples of 10 in the   |  | differences.   |  |  |
| digit whole numbers by multiples of 10 in the   |  | <ul> <li>estimating to assess the reasonableness of</li> </ul> |  |  |
| range 10-90 (e.g., $9 \times 80$ , $5 \times 60$ ) using strategies                         |  | their answers.   |  |  |
| based on place value and properties of operations.  |  | regrouping when performing multi-digit                         |  |  |
|   |  | arithmetic.  |  |  |
|   |  | <ul> <li>using place value to break large addition</li> </ul>  |  |  |
|   |  | problems into smaller ones that are easier to                  |  |  |
|   |  | add.   |  |  |

| Used in Content Area Standards | 21st Century Skills |
|--------------------------------|---------------------|
|                                | Problem Solving     |
| not applicable                 | Communication       |
|                                | Perseverance        |
|                                |                     |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

### Windham School District Curriculum Mathematics - Grade 3 Unit 4: Fractions

### **Stage 1 Desired Results**

### ESTABLISHED GOALS:

Students will continue their study of mathematics. In this unit, students will recognize the relationship between parts and whole. Students will write and represent fractions using pictures, number lines and other visual tools. Students will be able to compare fractions of the same size whole.

### Content Standards:

- CCSS.MATH.CONTENT.3.NF.A.1: Understand a fraction 1/b as the
  quantity formed by 1 part when a whole is partitioned into b equal
  parts; understand a fraction a/b as the quantity formed by a part of size
  1/b.
- CCSS.MATH.CONTENT.3.NF.A.2: Understand a fraction as a number on the number line; represent fractions on a number line diagram.
- CCSS.MATH.CONTENT.3.NF.A.2.A: Represent a fraction 1/b on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts. Recognize that each part has size 1/b and that the endpoint of the part based at 0 locates the number 1/b on the number line.
- CCSS.MATH.CONTENT.3.NF.A.2.B: Represent a fraction a/b on a number line diagram by marking off a length 1/b from 0. Recognize that the resulting interval has size a/b and that its endpoint locates the number a/b on the number line.
- CCSS.MATH.CONTENT.3.NF.A.3: Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.

### Transfer Students will be able to independently use their learning to...

- Explain how numbers are fractions
- Expand their knowledge of a number line to include fractions

### Meaning

### ENDURING UNDERSTANDINGS

 A fraction describes the division of a whole into equal parts. The denominator tells how many equal parts the whole is divided into. The numerator tells how many equal parts are indicated.

### ESSENTIAL QUESTIONS

How is a fraction related to a whole?

### Acquisition

### Students will understand...

- a fraction is a quantity formed when a part of a whole is divided into equal parts.
- a fraction is made up of equal parts.
- equivalent fractions
- Numerator and denominator
- Equal parts
- Unit Fraction
- Fraction tiles/ fraction strips
- Number lines
- Equivalent fractions

- writing a fraction to represent a drawing or place on a number line.
- partitioning a shape into parts with equal areas and labeling those areas with fractions.
- drawing a number line from 0 to 1, partitioning it into equal parts and labeling each part with a fraction.
- drawing a number line with more than 1 whole, partitioning it into

|   | marked off in appropriate units— whole numbers, halves, or quarters.  d in Content Area Standards  applicable   |   | • | an inch.  21st Century Skills  Problem solving Communication Perseverance   |
|---|---|---|---|---|
| • | CCSS.MATH.CONTENT.3.NF.A.3.B: Recognize and generate simple equivalent fractions, e.g., $1/2 = 2/4$ , $4/6 = 2/3$ . Explain why the fractions are equivalent, e.g., by using a visual fraction model. CCSS.MATH.CONTENT.3.NF.A.3.C: Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. <i>Examples: Express 3 in the form 3 = 3/1; recognize that 6/1 = 6; locate 4/4 and 1 at the same point of a number line diagram</i> . CCSS.MATH.CONTENT.3.NF.A.3.D: Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols $>$ , $=$ , or $<$ , and justify the conclusions, e.g., by using a visual fraction model. CCSS.MATH.CONTENT.3.MD.B.4: Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot, where the horizontal scale is | <ul><li>half inch</li><li>Quarter inch</li><li>Line plot</li></ul>              | • | the same numerator or two fractions that have the same denominator and use <, > or = by reasoning about their size and using a visual model. recognizing and generating simple equivalent fractions and explaining why they are equivalent. expressing whole numbers as fractions. recognizing fractions as parts to the whole with an understanding of the numerator and denominator parts. measuring lengths using rulers marked with halves and fourths of |
| • | CCSS.MATH.CONTENT.3.NF.A.3.A: Understand two fractions as equivalent (equal) if they are the same size, or the same point on a number line.   | <ul><li>Same numerator</li><li>Same denominator</li><li>Whole numbers</li></ul> | • | equal parts and labeling each part with a fraction. comparing two fractions that have   |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

### Windham School District Curriculum Mathematics - Grade 3 Unit 5: Time

| Stage 1 Desired Results                                |   |   |  |
|--|---|---|--|
| ESTABLISHED GOALS:                                     | Transf  | er  |  |
| Students will continue their study of mathematics.     | Students will be able to independently use their learning | to  |  |
| In this unit, students will tell and write time to the | • Tell and write time in hours, half-hours, quarter hour  | s, five-minutes, and minutes using analog and digital |  |
| nearest minute. Students will solve problems           | clocks.   |   |  |
| involving time intervals.                              | Meani   | ng  |  |
|  | ENDURING UNDERSTANDINGS                                   | ESSENTIAL QUESTIONS                                   |  |
| Content Standards:                                     | • Time can be measured using different units that are     | Why is a clock designed the way it is?                |  |
| CCSS.MATH.CONTENT.3.MD.A.1: Tell and                   | related to one another.                                   | How is time measured?                                 |  |
| write time to the nearest minute and                   | • The minute hand takes 5 minutes to move from one        | How are problems related to time used in our          |  |
| measure time intervals in minutes. Solve               | number to the next on a typical clock.                    | everyday life?  |  |
| word problems involving addition and                   | Acquisition   |   |  |
| subtraction of time intervals in minutes, e.g.,        | Students will understand                                  | Students will be skilled at                           |  |
|  | Fractions of time.  | telling time to the nearest minute.                   |  |
| line diagram.  | Minute hand   | Solving problems using time.                          |  |
|  | Hour hand   |   |  |
|  | AM and PM   |   |  |
|  | • 5 minute intervals                                      |   |  |
|  | Half past   |   |  |
|  | Quarter past  |   |  |
|  | Quarter of  |   |  |
|  | • 1 minute intervals                                      |   |  |
|  | Elapsed time (shown on number line, clock, or paper)      |   |  |
| Used in Content Area Standards 21st Century Skills     |   |   |  |
|  |   | Communication   |  |
| not applicable   |   | Perseverance  |  |
|  |   |   |  |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

### Windham School District Curriculum Mathematics - Grade 3 Unit 6: Area & Perimeter

| Stag  | ge 1 Desired Results  |  |
|---|---|--|
| ESTABLISHED GOALS:  | Transfer  |  |
| Students will continue their study of mathematics. In this unit,  | Students will be able to independently use their learning to                      |  |
| students will find the area and perimeter of given shapes.  | explain the difference between perimeter and area                                 |  |
|   | solve real world problems involving the area perimeter.                           |  |
| Content Standards:  |   |  |
| CCSS.MATH.CONTENT.3.MD.C.5: Recognize area as an attribute of   | Meaning   |  |
| plane figures and understand concepts of area measurement.  | ENDURING UNDERSTANDINGS ESSENTIAL QUESTIONS                                       |  |
| • CCSS.MATH.CONTENT.3.MD.C.5.A: A square with side length 1   | Perimeter and area are attributes of     How do we use area and perimeter in our  |  |
| unit, called "a unit square," is said to have "one square unit" of  | plane figures. everyday lives?  |  |
| area, and can be used to measure area.  | Area is application of multiplication   |  |
| CCSS.MATH.CONTENT.3.MD.C.5.B: A plane figure which can be   | Perimeter is an application of  |  |
| covered without gaps or overlaps by <i>n</i> unit squares is said to have   | addition  |  |
| an area of <i>n</i> square units.   | There is a distinct difference  |  |
| CCSS.MATH.CONTENT.3.MD.C.6: Measure areas by counting unit  | between area and perimeter and  |  |
| squares (square cm, square m, square in, square ft, and   | how they are measured.  |  |
| improvised units).  | Acquisition   |  |
| CCSS.MATH.CONTENT.3.MD.C.7: Relate area to the operations of  |   |  |
| multiplication and addition.  | a unit square as a square with a side     measuring the area by counting squares. |  |
| CCSS.MATH.CONTENT.3.MD.C.7.A: Find the area of a rectangle  | length of 1 unit  • finding the area of a rectangle using                         |  |
| with whole-number side lengths by tiling it, and show that the  | area as a certain number of unit multiplication.                                  |  |
| area is the same as would be found by multiplying the side  | squares with no gaps or overlaps   • solving real world problems involving the    |  |
| lengths.  | Area area of rectangles and perimeters of   |  |
| CCSS.MATH.CONTENT.3.MD.C.7.B: Multiply side lengths to find     areas of restangles with whole number side lengths in the | Unit square polygons.   |  |
| areas of rectangles with whole-number side lengths in the   | Perimeter     using area models to represent the                                  |  |
| context of solving real world and mathematical problems, and  | Square units distributive property.   |  |
|   | Units   |  |

| <ul> <li>overlapping parts, applying this technique to solve real world problems.</li> <li>CCSS.MATH.CONTENT.3.MD.D.8: Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.</li> <li>Used in Content Area Standards</li> </ul> not applicable   |  | <ul> <li>finding the perimeter of a polygon.</li> <li>21<sup>st</sup> Century Skills</li> <li>Communication</li> <li>Perseverance</li> </ul>   |
|---|--|--|
| <ul> <li>represent whole-number products as rectangular areas in mathematical reasoning.</li> <li>CCSS.MATH.CONTENT.3.MD.C.7.C: Use tiling to show in a concrete case that the area of a rectangle with whole-number side lengths a and b + c is the sum of a × b and a × c. Use area models to represent the distributive property in mathematical reasoning.</li> <li>CCSS.MATH.CONTENT.3.MD.C.7.D: Recognize area as additive. Find areas of rectilinear figures by decomposing them into non-overlapping rectangles and adding the areas of the non-</li> </ul> | <ul> <li>Length x Width</li> <li>Distributive Property</li> <li>distributive property as an area model</li> <li>perimeter as the outside distance around a polygon.</li> </ul> | <ul> <li>using addition to find areas of shapes that consist of non-overlapping rectangles.</li> <li>finding the perimeter of a polygon.</li> <li>when given the perimeter of a polygon and some side lengths, finding an unknown side length.</li> <li>showing that different rectangles can have the same perimeter</li> <li>showing that different rectangles can have the same area</li> </ul> |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

### Windham School District Curriculum Mathematics - Grade 3 Unit 7: Mass & Volume

| Stage 1 Desired Results   |  |   |
|---|--|---|
| ESTABLISHED GOALS:  |  | Transfer  |
| Students will continue their study of mathematics. In   | Students will be able to independently use their learning to   |   |
| this unit, students will use standard units to read and   | <ul> <li>use standard units of measurement</li> </ul>  | of mass and volume to solve problems.   |
| write mass and volume measurements.   |  | Meaning   |
| Content Standards:  ■ CCSS.MATH.CONTENT.3.MD.A.2: Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l).1 Add, subtract, multiply, or divide to | <ul> <li>Capacity is a measure of the amount of liquid a container can hold.</li> <li>Mass is a measure of the quantity of matter in an object. Weight and</li> </ul>      | <ul> <li>ESSENTIAL QUESTIONS</li> <li>Why is measurement important in our lives?</li> <li>How is measurement used and shared around the world?</li> </ul>   |
| solve one-step word problems involving masses or volumes that are given in the same units, e.g., by   | Acquisition  |   |
| using drawings (such as a beaker with a measurement scale) to represent the problem.  | <ul> <li>Students will understand</li> <li>mass, volume, and length.</li> <li>appropriate units to use when measuring mass and volume: grams, kilograms, liters</li> </ul> | <ul> <li>Students will be skilled at</li> <li>measuring liquid volumes and masses of objects using standard units of grams, kilograms and liters.</li> <li>estimating liquid volumes and masses of objects using standard units of grams, kilograms and liters.</li> <li>solving one-step word problems involving any operation using mass and volume given in the same units.</li> </ul> |
| Used in Content Area Standards  |  | 21 <sup>st</sup> Century Skills   |
| not applicable  |  | <ul><li>Communication</li><li>Perseverance</li><li>Problem solving</li></ul>  |

| Evaluative Criteria | Assessment Evidence  |  |
|---------------------|--|--|
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 3 Unit 8: Geometry Shapes & Attributes

|   | Stage 1 Desired Results  |  |  |
|---|--|--|--|
| ESTABLISHED GOALS:  | Transfer   |  |  |
| Students will continue their study of   | Students will be able to independently use their learning  | g to   |  |
| mathematics. In this unit, students will be   | <ul> <li>distinguish quadrilaterals based on their attributes.</li> </ul>  |  |  |
| able to identify and classify quadrilaterals  | <ul> <li>Categorize shapes based on shared attributes.</li> </ul>  |  |  |
| based on their attributes.  |  | eaning   |  |
|   |  | ESSENTIAL QUESTIONS  |  |
| <ul> <li>Content Standards:</li> <li>CCSS.MATH.CONTENT.3.G.A.1:         Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share     </li> </ul>                | <ul> <li>There are many types of quadrilaterals including rhombuses, rectangles, and squares.</li> <li>Shapes are categorized based on attributes they share.</li> </ul> | <ul> <li>How can two-dimensional shapes be described, analyzed and classified?</li> <li>Why is a square always a rectangle, but a rectangle isn't always a square?</li> </ul>  |  |
| attributes (e.g., having four sides), and   | 4  | How does math define different shapes in our world?  |  |
| that the shared attributes can define a   |  | students will be skilled at  |  |
| larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories. | <ul><li>shapes and their attributes (i.e. angles, lines, sides).</li><li>hierarchical way for defining shapes into larger</li></ul>                                      | <ul> <li>recognizing rhombuses, rectangles and squares as examples of quadrilaterals.</li> <li>drawing quadrilaterals that do not belong to any special subcategories of quadrilaterals (such as rhombuses, rectangles and squares).</li> <li>categorizing shapes based on their properties and attributes they share</li> </ul> |  |

| Used in Content Area Standards | 21st Century Skills |
|--------------------------------|---------------------|
|                                | Communication       |
| not applicable                 | Perseverance        |
|                                | Problem solving     |

| Stage 2 - Evidence   |   |  |
|--|---|--|
| Evaluative Criteria Assessment Evidence                                      |   |  |
|  | ASSESSMENT: Written Assessments or Projects |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |   |  |

### Windham School District Curriculum Mathematics - Grade 3

### Unit 9: Measurement & Data - Picture Graphs & Bar Graphs

|   | Stage 1 Desired Results   |   |  |
|---|---|---|--|
| ESTABLISHED GOALS:                              | Stage I Desired Results   | Transfor  |  |
|   | Transfer  |   |  |
|   | Students will be able to independently use their I  | 9   |  |
| mathematics. In this unit, students will create | read and understand graphs and what they in the second secon | represent.  |  |
| graphs to show data. Students will analyze and  | compare data using a graph setting.   |   |  |
| interpret pictures and bar graphs.              |   | Meaning   |  |
|   | ENDURING UNDERSTANDINGS   | ESSENTIAL QUESTIONS   |  |
| Content Standards:                              | <ul> <li>Some problems can be solved by making,</li> </ul>  | <ul> <li>How can we use graphs to represent and show data?</li> </ul> |  |
| CCSS.MATH.CONTENT.3.MD.B.3: Draw a              | reading, and analyzing a graph.   | How can understanding (interpreting) pictures and bar                 |  |
| scaled picture graph and a scaled bar           |   | graphs help us to understand real world data?                         |  |
| graph to represent a data set with several      |   | Acquisition   |  |
|   | Students will understand  | Students will be skilled at   |  |
| many more" and "how many less"                  | Bar graph   | Use bar graphs and picture graphs, to answer                          |  |
| problems using information presented in         | Picture Graph   | questions and solve problems.   |  |
| scaled bar graphs.                              | Data  | Draw a bar graph or picture graph, with given data.                   |  |
|   | Scale   | Generate measurement data by measuring lengths                        |  |
|   | Key   | using rulers marked with halves and fourths of an inch.               |  |
|   | Survey  |   |  |
|   | Tally marks   |   |  |
| Used in Content Area Standards                  |   | 21 <sup>st</sup> Century Skills                                       |  |
|   |   | Communication   |  |
| not applicable                                  |   | Perseverance  |  |
|   |   | Problem solving   |  |
|   |   | Critical Thinking   |  |
|   |   |   |  |

| Evaluative Criteria | Assessment Evidence  |  |
|---------------------|--|--|
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

### <u>Title of Curriculum</u>: Grade 4 Mathematics

| Unit Name                               | What (content, vocab)  | Why (enduring understandings)  | How (skills)  |
|---|--|--|---|
| Place Value                             | <ul> <li>Round</li> <li>Compare</li> <li>Periods (ones, thousands etc.)</li> <li>Determine operation</li> <li>Break down (steps)</li> <li>Estimate to check</li> </ul>   | <ul> <li>Place value is based on groups of ten and helps to organize our number system.</li> <li>Place value can be used to compare and order numbers.</li> </ul>  | standard, and word form  Round whole numbers to any place   |
| Multi-digit Addition and Subtraction    | <ul> <li>Line up place value</li> <li>Regroup</li> <li>Determine operation</li> <li>Break down (steps)</li> <li>Estimate to check</li> </ul>   | <ul> <li>Place value, properties of operations, and the relationship between addition and subtraction can be used in fluently adding &amp; subtracting whole numbers</li> <li>Operations with whole numbers can be used to solve word problems.</li> </ul>               | <ul> <li>lining up numbers before adding/subtracting</li> <li>adding multi digit number with regrouping</li> <li>using borrowing when subtracting</li> <li>identifying whether a word problem requires addition or subtraction</li> </ul>   |
| Multi-digit Multiplication and Division | <ul> <li>Different algorithms</li> <li>Inverse operations</li> <li>Equations</li> <li>Rectangular arrays</li> <li>Area models</li> <li>Determine operation</li> <li>Break down (steps)</li> <li>Estimate to check</li> </ul> | <ul> <li>Multiplication and division have an inverse relationship. The inverse relationship between multiplication and division can be used to solve problems.</li> <li>When dividing the remainder must be less than the divisor. The nature of the question</li> </ul> | <ul> <li>Multiply a whole number (up to four digits) by a one-digit whole number</li> <li>Multiply two two-digit numbers</li> <li>Demonstrate that multiplication is the inverse of division</li> <li>Show mastery of all division facts with accuracy and fluency</li> <li>Find whole number quotients and remainders with up to four-digit dividends and one-digit divisors</li> <li>Use multiple strategies to solve problems</li> </ul> |

| Factors and Multiples | factor and multiple   | asked determines how to interpret and use the remainder.  • Each estimation technique gives a way to replace numbers with other numbers that are close and easy to compute with mentally.  • Every counting number is   | ·   |
|-----------------------|---|---|---|
|                       | <ul> <li>prime and composite</li> <li>a whole number as a product of each of its factors.</li> <li>1 is neither prime nor composite.</li> </ul> | <ul> <li>divisible by 1 and itself.</li> <li>Some counting numbers are divisible by numbers beyond 1 and itself.</li> <li>The product of any nonzero number and any other nonzero number is divisible by each number and called a multiple of each number.</li> </ul> | <ul> <li>range 1 to 100</li> <li>Recognize that a whole number is a multiple of each of its factors</li> <li>Determine whether a given whole number, in the range 0 to 100, is a multiple of a given one-digit number</li> <li>Determine whether a given whole number, in the range 0 to 100, is prime or composite.</li> <li>Use factors and multiples to solve problems including finding equivalent fractions.</li> <li>Use multiple strategies to solve problems</li> <li>Assess the reasonableness of answers</li> </ul> |
| Algebra: Patterns     | <ul> <li>Predictable</li> <li>Numerical/Geometrical</li> <li>Rules</li> <li>Determine operation</li> </ul>                                      | <ul> <li>Relationships can be described and generalizations made for mathematical situations that have numbers or objects that repeat in predictable ways.</li> <li>Some patterns consist of shapes or numbers that are arranged in a unit that repeats.</li> </ul>   | <ul> <li>extending a given pattern.</li> <li>writing a rule for a given pattern.</li> <li>identifying the features of a pattern.</li> <li>creating a pattern</li> <li>Naming a pattern's rule.</li> </ul>   |

| be represented by an infinite set of different but equivalent fractions.  Benchmark fractions such as ½ are useful when comparing two fractions to each other.  Fractions can be built from unit fractions by applying and extending understandings of operations and decimals.  There is an equivalence between fractions and decimals.  benchmark fractions such as ½ are useful when comparing two fractions and decimals.  benchmark fractions such as ½ are useful when comparing two fractions and adition and subtraction  benchmark fractions such as ½ are useful when comparing two fractions on particular fractions and addition and subtraction  benchmark fractions and built equivalent fractions are using multiplication of fractions  benchmark fractions and addition and subtraction  benchmark fractions and subtraction  benchmark fractions and built equivalent fractions and addition and subtraction  benchmark fractions and subtraction  benchmark fractions and built equivalent fractions and addition and subtraction  benchmark fractions and subtraction  benchmark fractions and built equivalent fractions and addition and subtraction  benchmark fractions and subtraction  benchmark fractions and built equivalent fractions and addition and subtraction  benchmark fractions to show fractions and subtraction  benchmark fractions and pictures to show fraction addition and subtraction  benchmark fractions to solve and subtraction  benchmark fractions to solve and subtraction  benchmark fractions and subtraction  benchmark fractions and pictures to show fractions addition and subtraction  benchmark fractions and pictures to show fractions and indictions.  benchmark fractions and pictures to show fractions and indictions.  benchmark fractions and |                        |  | Г  | <del></del>  |
|--|------------------------|--|--|--|
| described using mathematical rules. Some real-world quantities have a mathematical relationship; the value of one quantity can be found if you know the value of another quantity.  The same fractional amount can be represented by an infinite set of different but equivalent fractions. Benchmark fractions such as ½ are useful when comparing two fractions to each other. Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers. There is an equivalence between fractions and decimals.  decimals.  decimals.  decimals   a Add and subtract fractions and mixed number with like denominators Subtract fractions and mixed number with like denominators Subtract fractions and prictures to show fraction addition and subtraction Solve word problems using multiplication of fractions Fractions and be built from unit fractions by applying and extending understandings of operations on whole numbers. There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals.  Determine if two fractions with like and unlike denominators Use visual model to represent fraction multiplication Fractions on whole numbers. There is an equivalence between fractions and decimals.  Determine if two fractions with like and unlike denominators Use visual model to represent fractions Compare fractions with like and unlike denominators Use visual models to compare fractions Compare fractions to decimals Convert factionals to fractions with simplification Locate decimals to fundredths Use >, <, = in comparison sentence   |                        |  | •  |  |
| mathematical rules.  Some real-world quantities have a mathematical relationship; the value of one quantity can be found if you know the value of another quantity.  The same fractional amount can be represented by an infinite set of different but equivalent fractions.  Benchmark fractions such as ½ are useful when comparing two fractions to each other.  Fractions to each other.  Fractions by applying and extending understandings of operations on whole numbers.  There is an equivalence between fractions and decimals.  mathematical rules.  Some real-world quantities have a mathematical relationship; the value of one quantity.  Add and subtract fractions and mixed number with like denominators  Subtract fractions from a whole  Use models and pictures to show fraction addition and subtraction  Solve word problems using multiplication of fractions  Solve word problems using multiplication of fractions  Use a visual model to represent fractions between fractions and decimals or compare fractions with simplification  Find equivalent fractions or Use a visual model to compare fractions  Use visual models to compare fractions  Convert fractions to decimals  Convert fractions to decimals to fractions with simplification  Locate decimals to fractions with simplification  Locate decimals on number line  Compare decimals to fundredths  Use >, <, = in comparison sentence  |                        |  | •  |  |
| Some real-world quantities have a mathematical relationship; the value of one quantity can be found if you know the value of another quantity.      The same fractional amount can be represented by an infinite set of different but equivalent fractions.     Benchmark fractions such as ½ are useful when comparing two fractions to each other.     Fractions can be built from unit fractions on whole numbers.     There is an equivalence between fractions and decimals.      Some real-world quantities have a mathematical relationship; the value of one quantity can be found if you know the value of another quantity.  Add and subtract fractions and mixed number with like denominators  Subtract fractions from a whole Use models and pictures to show fraction addition and subtraction Solve word problems using multiplication of fractions Comparing two fractions to each other.  Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions on whole numbers.  There is an equivalence between fractions on multiplication  Find quivalent fractions and in the denominators  Use a visual model to represent fractions by denominators  Use visual models to compare fractions  Convert fractions to decimals to fractions with simplification  Locate decimals to fundredths  Use >, <, = in comparison sentence   |                        |  | described using                            |  |
| quantities have a mathematical relationship; the value of one quantity can be found if you know the value of another quantity.  • The same fractional amount can be represented by an infinite set of different but equivalent fractions.  • Benchmark fractions such as ¾ are useful when comparing two fractions to each other.  • Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.  • There is an equivalence between fractions and decimals.  • There is an equivalence between fractions and decimals.  • Quantities have a mathematical relationship; the value of one quantity.  • The same fractional amount can be represented by an infinite set of different but equivalent fractions.  • Benchmark fractions such as ¾ are useful when comparing two fractions to each other.  • Fractions can be built from unit fractions and extending understandings of operations on whole numbers.  • There is an equivalence between fractions and decimals.  • There is an equivalence between fractions and decimals.  • There is an equivalence between fractions and decimals to fractions with simplification  • Convert fractions on umber line  • Compare decimals to hundredths  • Use >, <, = in comparison sentence  |                        |  | mathematical rules.                        |  |
| ### Practions and Decimals  • The same fractional amount can be represented by an infinite set of different but equivalent fractions. • Benchmark fractions such as ⅓ are useful when comparing two fractions to each other. • Fractions can be built from unit fractions operations on whole numbers. • There is an equivalence between fractions and decimals. • There is an equivalence between fractions and decimals.  ■ The same fractional amount can be another quantity.  ■ The same fractional amount can be represented by an infinite set of different but equivalent fractions.  ■ Benchmark fractions such as ⅓ are useful when comparing two fractions to each other.  ■ Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers. ■ There is an equivalence between fractions and decimals.  ■ There is an equivalence between fractions and decimals.  ■ There is an equivalence between fractions and decimals.  ■ There is an equivalence between fractions and decimals.  ■ There is an equivalence between fractions and decimals.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ There is an equivalence between fractions on whole numbers.  ■ The is a nequivalence between fractions on whole numbers.  ■ The isame fractions on wh  |                        |  | <ul> <li>Some real-world</li> </ul>        |  |
| relationship; the value of one quantity can be found if you know the value of another quantity.  • The same fractional amount can be represented by an infinite set of different but equivalent fractions.  • Benchmark fractions such as ½ are useful when comparing two fractions to each other.  • Fractions can be built from unit fractions by applying and extending understandings of operations and decimals.  • There is an equivalence between fractions and decimals.  • There is an equivalence between fractions and decimals.  • There is an equivalence between fractions and decimals.  • There is an equivalence between fractions and decimals.  • There is an equivalence between fractions and decimals.  • Add and subtract fractions and mixed number with like denominators  • Subtract fractions from a whole  • Use models and pictures to show fraction addition and subtraction  • Solve word problems using multiplication of fractions to each other.  • Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.  • There is an equivalence between fractions and decimals.  • There is an equivalence between fractions and decimals.  • There is an equivalence between fractions and decimals.  • Convert decimals to fractions with simplification  • Locate decimals to hundredths  • Use >, <, = in comparison sentence   |                        |  | quantities have a                          |  |
| one quantity can be found if you know the value of another quantity.  The same fractional amount can be represented by an infinite set of different but equivalent fractions.  Benchmark fractions such as ½ are useful when comparing two fractions to each other.  Fractions can be built from unit fractions on whole numbers.  There is an equivalence between fractions and decimals.  one quantity can be found if you know the value of another quantity.  The same fractional amount can be represented by an infinite set of different but equivalent fractions.  Benchmark fractions such as ½ are useful when comparing two fractions on whole numbers.  Fractions can be built from unit fractions on be built from unit fractions on whole numbers.  There is an equivalence between fractions and decimals.  |                        |  | mathematical                               |  |
| Fractions and Decimals  • The same fractional amount can be represented by an infinite set of different but equivalent fractions. • Benchmark fractions such as ½ are useful when comparing two fractions to each other. • Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers. • There is an equivalence between fractions and decimals.  if you know the value of another quantity.  The same fractional amount can be represented by an infinite set of different but equivalent fractions.  Benchmark fractions such as ½ are useful when comparing two fractions to each other.  Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.  There is an equivalence between fractions and decimals.  if you know the value of another quantity.  The same fractional amount can be represented by an infinite set of different but equivalent fractions.  Benchmark fractions on sub equivalent fractions on addition and subtraction of solve word problems using multiplication of fractions on multiplication of fractions on multiplication of poperations on whole numbers.  There is an equivalent fractions by applying and extending understandings of operations on whole numbers.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals.  |                        |  | relationship; the value of                 |  |
| ### another quantity.    The same fractional amount can be represented by an infinite set of different but equivalent fractions.   Benchmark fractions such as ½ are useful when comparing two fractions to each other.   Fractions can be built from unit fractions on whole numbers.   There is an equivalence between fractions and decimals.   There is an equivalence between fractions and decimals amount can be represented by an infinite set of different but equivalent fractions.   Benchmark fractions such as ½ are useful when comparing two fractions on didition and subtraction addition and subtract fractions amount can be represented by an infinite set of different but equivalent fractions.   Benchmark fractions on be oblited from unit fractions on to each other.   Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.   There is an equivalence between fractions and decimals.   There is an equivalence between fractions and decimals.   There is an equivalence between fractions and decimals to convert fractions with simplification  |                        |  | one quantity can be found                  |  |
| Fractions and Decimals  ■ The same fractional amount can be represented by an infinite set of different but equivalent fractions. ■ Benchmark fractions such as ½ are useful when comparing two fractions to each other. ■ Fractions can be built from unit fractions by applying and extending understandings of operations and decimals. ■ The same fractional amount can be represented by an infinite set of different but equivalent fractions. ■ Benchmark fractions such as ½ are useful when comparing two fractions to each other. ■ Fractions can be built from unit fractions by applying and extending understandings of operations and decimals. ■ There is an equivalence between fractions and decimals. ■ The same fractional amount can be represented by an infinite set of different but equivalent fractions. ■ Benchmark fractions such as ½ are useful when comparing two fractions to each other. ■ Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers. ■ There is an equivalence between fractions and decimals. ■ The same fractional amount can be represented by an infinite set of different but equivalent fractions. ■ Benchmark fractions such as ½ are useful when comparing two fractions such as ¼ are useful when comparing two fractions to each other. ■ Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers. ■ There is an equivalence between fractions and decimals. ■ The same fractions infinite set of different but equivalent fractions. ■ Subtract fractions from a whole Use models and pictures to show fractions Such as ¼ are useful when comparing two fractions such as ¼ are useful when comparing two fractions such as ¼ are useful when comparing two fractions such as ¼ are useful when comparing two fractions such as ¼ are useful when comparing two fractions such as ¼ are useful when comparing two fractions on whole numbers. ■ The reactions on whole numbers ■ Convert fractions on with like denominators ■ Convert fract  |                        |  | if you know the value of                   |  |
| be represented by an infinite set of different but equivalent fractions.  Benchmark fractions such as ½ are useful when comparing two fractions to each other.  Fractions can be built from unit fractions by applying and extending understandings of operations and decimals.  There is an equivalence between fractions and decimals.  be represented by an infinite set of different but equivalent fractions.  Benchmark fractions such as ½ are useful when comparing two fractions such as ½ are useful when comparing two fractions on whole numbers.  Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals.  Benchmark fractions such as ½ are represented by an infinite set of different but equivalent fractions.  Benchmark fractions such as ½ are useful when comparing two fractions such as ½ are useful when comparing two fractions son be built from unit fractions by applying and extending to operations on whole numbers.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals.  Determine if two fractions with like and unlike denominators  Use visual model to represent fraction multiplication  Find equivalent fractions  Use visual models to compare fractions on whole numbers.  Use visual models to compare fractions on equivalent fractions and decimals on number line  Compare decimals to hundredths  Use >, <, = in comparison sentence  |                        |  | another quantity.                          |  |
| of different but equivalent fractions.  Benchmark fractions such as ½ are useful when comparing two fractions to each other.  Fractions can be built from unit fractions by applying and extending understandings of operations and decimals.  There is an equivalence between fractions and decimals.  represented by an infinite set of different but equivalent fractions.  Benchmark fractions such as ½ are useful when comparing two fractions to each other.  Benchmark fractions such as ½ are useful when comparing two fractions to each other.  Fractions can be built from unit from unit from unit fractions by applying and extending understandings of operations on whole numbers.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals.  Enchmark fractions such as ½ are equivalent fractions.  Benchmark fractions such as ½ are equivalent fractions on bollet we useful when comparing two fractions addition and subtraction  Solve word problems using multiplication of fractions  Use a visual model to represent fraction multiplication  Find equivalent fractions  Determine if two fractions on petitions are equivalent equivalent fractions are equivalent equivalent fractions.  There is an equivalence between fractions on whole numbers.  There is an equivalence between fractions and decimals.   | Fractions and Decimals | The same fractional amount can                       | The same fractional                        | Add and subtract fractions and mixed number                  |
| <ul> <li>fractions.</li> <li>Benchmark fractions such as ½ are useful when comparing two fractions to each other.</li> <li>Fractions can be built from unit fractions by applying and extending understandings of operations and decimals.</li> <li>There is an equivalence between fractions and decimals.</li> <li>set of different but equivalent fractions.</li> <li>Benchmark fractions such as ½ are useful when comparing two fractions such as ½ are useful when comparing two fractions so each other.</li> <li>Fractions can be built from unit fractions to each other.</li> <li>Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> <li>Use a visual model to represent fraction multiplication</li> <li>Find equivalent fractions</li> <li>Determine if two fractions with like and unlike denominators</li> <li>Use visual models to compare fractions on whole numbers.</li> <li>Convert fractions to decimals</li> <li>Convert decimals to fractions with simplification</li> <li>Locate decimals on number line</li> <li>Compare decimals to hundredths</li> <li>Use , &lt;, = in comparison sentence</li> </ul>  |                        | be represented by an infinite set                    | amount can be                              | with like denominators                                       |
| <ul> <li>Benchmark fractions such as ½ are useful when comparing two fractions to each other.</li> <li>Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> <li>There is an equivalence between fractions and decimals.</li> <li>Enchmark fractions.</li> <li>Benchmark fractions.</li> <li>Benchmark fractions.</li> <li>Benchmark fractions such as ½ are useful when comparing two fractions to each other.</li> <li>Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> </ul>   |                        | of different but equivalent                          | represented by an infinite                 | Subtract fractions from a whole                              |
| <ul> <li>useful when comparing two fractions to each other.</li> <li>Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> <li>There is an equivalence between fractions and decimals.</li> <li>There is an equivalence between fractions and decimals.</li> </ul> <ul> <li>Benchmark fractions such as ½ are useful when comparing two fractions to each other.</li> <li>Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> <li>There is an equivalence between fractions and decimals.</li> <li>There is an equivalence between fractions and decimals.</li> <li>Convert fractions using multiplication of fractions</li> <li>Use a visual model to represent fraction multiplication</li> <li>Compare fractions with like and unlike denominators</li> <li>Use visual models to compare fractions on understanding of the province operations on whole numbers.</li> <li>Convert fractions on number line</li> <li>Compare decimals to hundredths</li> <li>Use &gt;, &lt;, = in comparison sentence</li> </ul>   |                        | fractions.   | set of different but                       | Use models and pictures to show fraction                     |
| fractions to each other.  Fractions can be built from unit fractions by applying and extending understandings of operations and decimals.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals.  There is an equivalence between between fractions and decimals.  There is an equivalence between fractions and decimals.  There is an equivalence between between fractions and decimals.  There is an equivalence between between fractions and decimals.  There is an equivalence between between fractions and decimals.  There is an equivalence between between fractions and decimals.  There is an equivalence between between fractions and decimals.  There is an equivalence between between fractions and decimals.  There is an equivalence between between fractions and decimals.  There is an equivalence between between fractions and decimals.  There is an equivalence between between fractions and decimals.   |                        | • Benchmark fractions such as ½ are                  | equivalent fractions.                      | addition and subtraction                                     |
| <ul> <li>Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> <li>There is an equivalence between fractions and decimals.</li> <li>There is an equivalence between fractions on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> <li>Use a visual model to represent fraction multiplication</li> <li>Find equivalent fractions on Every fractions are equivalent denominators</li> <li>Use visual model to represent fraction multiplication</li> <li>Compare fractions with like and unlike denominators</li> <li>Use visual model to represent fraction multiplication</li> <li>Compare fractions on the built from unit fractions on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> <li>Use visual model to represent fraction multiplication</li> <li>Compare fractions on the built from unit fractions on whole numbers.</li> <li>Determine if two fractions</li> <li>Use visual model to represent fraction multiplication</li> <li>Compare fractions on the denominators</li> <li>Use visual model to represent fraction multiplication</li> <li>Compare fractions on the private fractions are equivalent on the provided denominators</li> <li>Use visual model to represent fractions</li> <li>Compare fractions on the private fractions</li> <li>Use a visual model to represent fractions</li> </ul>   |                        | useful when comparing two                            | Benchmark fractions such                   | Solve word problems using multiplication of                  |
| fractions by applying and extending understandings of operations on whole numbers.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions on whole numbers.  There is an equivalence between fractions on whole numbers.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals to compare fractions with simplification  Locate decimals on number line  Compare decimals to hundredths  Use >, <, = in comparison sentence  |                        | fractions to each other.                             | as ½ are useful when                       | fractions  |
| <ul> <li>extending understandings of operations on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> <li>There is an equivalence between fractions and decimals.</li> <li>Fractions can be built from unit fractions by applying and extending understandings of operations on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> <li>There is an equivalence between fractions and decimals.</li> <li>Find equivalent fractions         <ul> <li>Compare fractions with like and unlike denominators</li> <li>Use visual models to compare fractions</li> <li>Convert decimals to fractions with simplification</li> <li>Locate decimals on number line</li> <li>Compare decimals to hundredths</li> <li>Use &gt;, &lt;, = in comparison sentence</li> </ul> </li> </ul>   |                        | <ul> <li>Fractions can be built from unit</li> </ul> | comparing two fractions                    | Use a visual model to represent fraction                     |
| operations on whole numbers.  There is an equivalence between fractions and decimals.  from unit fractions by applying and extending understandings of operations on whole numbers.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals.  There is an equivalence between fractions and decimals to fractions with simplification  Locate decimals to hundredths  Use >, <, = in comparison sentence   |                        | fractions by applying and                            | to each other.                             | multiplication   |
| <ul> <li>There is an equivalence between fractions and decimals.</li> <li>applying and extending understandings of operations on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> <li>Compare fractions with like and unlike denominators</li> <li>Use visual models to compare fractions</li> <li>Convert fractions to decimals</li> <li>Convert decimals to fractions with simplification</li> <li>Locate decimals on number line</li> <li>Compare decimals on number line</li> <li>Use &gt;, &lt;, = in comparison sentence</li> </ul>  |                        | extending understandings of                          | <ul> <li>Fractions can be built</li> </ul> | Find equivalent fractions                                    |
| fractions and decimals.  understandings of operations on whole numbers.  There is an equivalence between fractions and decimals.  There is an equivalence of the tween fractions and decimals.  Locate decimals to hundredths of the tween fractions of the tween fractions on number line of the tween fractions on the fractions of the fractions of the tween fractions on the fractions of tween fractions on the fractions of the fractions of tween fractions on the fractions of the fractions  |                        | operations on whole numbers.                         | from unit fractions by                     | Determine if two fractions are equivalent                    |
| <ul> <li>operations on whole numbers.</li> <li>There is an equivalence between fractions and decimals.</li> <li>Use visual models to compare fractions</li> <li>Convert fractions to decimals</li> <li>Convert decimals to fractions with simplification</li> <li>Locate decimals on number line</li> <li>Compare decimals to hundredths</li> <li>Use &gt;, &lt;, = in comparison sentence</li> </ul>  |                        | <ul> <li>There is an equivalence between</li> </ul>  | applying and extending                     | Compare fractions with like and unlike                       |
| numbers.  There is an equivalence between fractions and decimals.  Convert fractions to decimals  Convert decimals to fractions with simplification  Locate decimals on number line  Compare decimals to hundredths  Use >, <, = in comparison sentence  |                        | fractions and decimals.                              | understandings of                          | denominators   |
| <ul> <li>There is an equivalence between fractions and decimals.</li> <li>Convert decimals to fractions with simplification</li> <li>Locate decimals on number line</li> <li>Compare decimals to hundredths</li> <li>Use &gt;, &lt;, = in comparison sentence</li> </ul>   |                        |  | operations on whole                        | Use visual models to compare fractions                       |
| between fractions and decimals.  between fractions and decimals.  compare decimals to hundredths  Use >, <, = in comparison sentence   |                        |  | numbers.                                   | Convert fractions to decimals                                |
| decimals.  • Locate decimals on number line • Compare decimals to hundredths • Use >, <, = in comparison sentence  |                        |  | There is an equivalence                    | Convert decimals to fractions with                           |
| <ul> <li>Compare decimals to hundredths</li> <li>Use &gt;, &lt;, = in comparison sentence</li> </ul>   |                        |  | between fractions and                      | simplification   |
| • Use >, <, = in comparison sentence   |                        |  | decimals.                                  | Locate decimals on number line                               |
|  |                        |  |  | Compare decimals to hundredths                               |
|  |                        |  |  | <ul> <li>Use &gt;, &lt;, = in comparison sentence</li> </ul> |
| • Use multiple strategies to solve problems  |                        |  |  | Use multiple strategies to solve problems                    |
| Assess the reasonableness of answers   |                        |  |  | Assess the reasonableness of answers                         |
| Display measurement data with fractions in a   |                        |  |  | Display measurement data with fractions in a                 |

|   |   |  | <ul><li>line plot.</li><li>Solve fraction addition and subtraction using a line plot</li></ul>  |
|---|---|--|---|
| Measurement & Data:<br>Conversion and<br>Area/Perimeter | <ul> <li>Systems of measurement</li> <li>Relative units</li> <li>Measurement equivalence</li> <li>Area and perimeter</li> <li>Formulas for rectangles</li> <li>Determine operation</li> <li>Break down (steps)</li> <li>Estimate to check</li> </ul>  | <ul> <li>Some attributes of objects are measurable and can be quantified using unit amounts.</li> <li>Time can be expressed using different units that are related to each other.</li> <li>Some problems can be solved by applying the formula for the perimeter of a rectangle or the formula for the area of a rectangle.</li> </ul> | <ul> <li>applying area and perimeter in real world problems.</li> <li>solving problems related to the addition and subtraction of time in minutes.</li> <li>finding elapsed time.</li> <li>using strategies such as a number line to solve problems relating to time intervals.</li> <li>showing measurement data on a line plot and</li> </ul>   |
| Measurement & Data:<br>Lines and Angles                 | <ul> <li>Formed by two rays common endpoint</li> <li>Fraction of a circle</li> <li>Angle represents turn</li> <li>Lines, line segments, and rays</li> <li>Right, acute, and obtuse</li> <li>Symmetry</li> <li>Determine operation</li> <li>Break down (steps)</li> <li>Estimate to check</li> </ul> | <ul> <li>Line segments and rays are sets of points that describe parts of lines, shapes and solids.</li> <li>Angles are formed by two intersecting lines or by rays with a common endpoint and are classified by size.</li> </ul>  | <ul> <li>Measure angles with a protractor</li> <li>Represent an angle measurement as a fraction of a circle (over 360)</li> <li>Draw an angle with a given measurement</li> <li>Find unknown angle using addition and subtraction</li> <li>Identify points, lines, line segments, rays, perpendicular, and parallel lines.</li> <li>Identify right, acute, and obtuse angles.</li> <li>Identify right triangles</li> <li>Classify two-dimensional figures based on parallel and perpendicular lines</li> <li>Identify and draw lines of symmetry on two-dimensional figures</li> <li>Use multiple strategies to solve problems</li> <li>Assess the reasonableness of answers</li> </ul> |

### Windham School District Curriculum Mathematics - Grade 4 Unit 1: Place Value

|   | Stage 1 Desired Results                                 |   |  |
|---|---|---|--|
| ESTABLISHED GOALS:  | Trar  | nsfer   |  |
| sudents will continue their study of mathematics. In Students will be able to independently use their learning to |   |   |  |
| this unit, students will use place value to read, write,  | • read multi digit numbers from 1,000-1,000,000.        |   |  |
| compare and round whole numbers to a given place.   | • compare two multi digit numbers from 1,000-1,000,000. |   |  |
|   | Mea   | ning  |  |
| Content Standards:  | ENDURING UNDERSTANDINGS                                 | ESSENTIAL QUESTIONS                                     |  |
| CCSS.MATH.CONTENT.4.NBT.A.1: Recognize that   | Place value is based on groups of ten and helps         | <ul> <li>How is our number system organized?</li> </ul> |  |
| in a multi-digit whole number, a digit in one place   | to organize our number system.                          | How does the position of a digit in a number            |  |
| represents ten times what it represents in the  | Place value can be used to compare and order            | affect its value?                                       |  |
| place to its right. For example, recognize that 700   | numbers.  | In what ways can numbers be composed and                |  |
| $\div$ 70 = 10 by applying concepts of place value and  |   | decomposed?   |  |
| division.   |   | When can rounding be useful and in what                 |  |
|   |   | situations should we not round?                         |  |
| CCSS.MATH.CONTENT.4.NBT.A.2: Read and write   |   |   |  |
| multi-digit whole numbers using base-ten  |   | isition   |  |
| •   |   | Students will be skilled at                             |  |
| Compare two multi-digit numbers based on  | That a digit in one place represents ten times          | Regroup numbers to the next place value                 |  |
| meanings of the digits in each place, using >, =,   | what it represents in the place to its right.           | Write a multi-digit whole number in expanded,           |  |
| and < symbols to record the results of  | Base-ten numerals, number names, and                    | standard, and word form                                 |  |
| comparisons.  | expanded form.  | Round whole numbers to any place                        |  |
| CCSS.MATH.CONTENT.4.NBT.A.3: Use place value  | Round   | Compare multi-digit whole numbers                       |  |
| understanding to round multi-digit whole numbers  | •   | Read multi-digit numbers                                |  |
| to any place.   | <ul> <li>Periods (ones, thousands etc.)</li> </ul>      | Order multi-digit numbers                               |  |
| CCSS.MATH.CONTENT.4.OA.A.3: Solve multi-step  | Determine operation                                     | Use multiple strategies to solve problems               |  |
| word problems posed with whole numbers and  | Break down (steps)                                      | Assess the reasonableness of answers                    |  |
| having whole-number answers using the four  | Estimate to check                                       |   |  |
| operations, including problems in which   |   |   |  |

| problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.  • *Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000. |   |
|---|---|
| Used in Content Area Standards  | 21 <sup>st</sup> Century Skills                         |
| not applicable  | <ul><li>Problem solving</li><li>Communication</li></ul> |

| Stage 2 - Evidence   |   |  |
|--|---|--|
| Evaluative Criteria  | Assessment Evidence                         |  |
|  | ASSESSMENT: Written Assessments or Projects |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |   |  |

# Windham School District Curriculum Mathematics - Grade 4 Unit 2: Multi-Digit Addition & Subtraction

|   | •   |  |  |  |
|---|---|--|--|--|
|   | Stage 1 Desired Results   |  |  |  |
| ESTABLISHED GOALS:  | Transfer  |  |  |  |
| Students will continue their study of mathematics. In   | Students will be able to independently use their learning   | to   |  |  |
| this unit, students will fluently add and subtract multi-   | <ul> <li>Add and subtract multi-digit numbers from 1,000-1,0</li> </ul>   | 00,000.  |  |  |
| digit whole numbers.  | Meaning   |  |  |  |
| Content Standards:  | <ul><li>ENDURING UNDERSTANDINGS</li><li>● Place value, properties of operations, and the</li></ul>  | ESSENTIAL QUESTIONS  ■ Why is it important to be fluent in adding  |  |  |
| <ul> <li>CCSS.MATH.CONTENT.4.NBT.B.4: Fluently add and subtract multi-digit whole numbers using the standard algorithm.</li> <li>CCSS.MATH.CONTENT.4.OA.A.3: Solve multi-step</li> </ul>                                    | relationship between addition and subtraction can be used in fluently adding and subtracting whole numbers.   | and subtracting multi-digit whole numbers?   |  |  |
| word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which   | word problems.  Acquisition   | 0  |  |  |
| remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including | <ul> <li>Students will understand</li> <li>Placement of the digits (line up the digits) when adding/subtracting</li> <li>That you add/subtract from right to left</li> <li>borrowing for subtracting</li> </ul> | <ul> <li>Students will be skilled at</li> <li>lining up numbers before adding/subtracting</li> <li>adding multi digit number with regrouping using borrowing when subtracting</li> </ul> |  |  |
| rounding.*Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000.   | <ul> <li>regrouping for adding</li> <li>Line up place value</li> <li>Regroup</li> <li>Determine operation</li> <li>Break down (steps)</li> <li>Estimate to check</li> </ul>                                     | identifying whether a word problem requires addition or subtraction  |  |  |
| Used in Content Area Standards  |   | 21 <sup>st</sup> Century Skills  |  |  |
|   |   | <ul> <li>Problem solving</li> </ul>  |  |  |

| not applicable | Communication |
|----------------|---------------|
|                | Perseverance  |

| Stage 2 - Evidence  |  |  |  |
|---------------------|--|--|--|
| Evaluative Criteria | Assessment Evidence  |  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Mathematics - Grade 4 Unit 3: Multi-Digit Multiplication & Division

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|--|-------|--|
|  |       |  |
|  |       |  |

Students will continue their study of mathematics. In this unit, students will be able to multiply a whole number (up to four digits) by a one digit whole number as well as two two digit numbers.

#### Content Standards:

- CCSS.MATH.CONTENT.4.NBT.B.5: Multiply a whole number of up to four digits by a one-digit whole number, and multiply two two-digit numbers, using strategies based on place value and the properties of operations. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.
- CCSS.MATH.CONTENT.4.NBT.B.6: Find wholenumber quotients and remainders with up to fourdigit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.
- CCSS.MATH.CONTENT.4.OA.A.3: Solve multi-step word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which

#### **Stage 1 Desired Results**

Students will be able to independently use their learning to...

- demonstrate the connection between multiplication and division.
- multiply multi-digit numbers
- divide 4 digit dividends by 1 digit divisors

#### Meaning

Transfer

#### ENDURING UNDERSTANDINGS

- Multiplication and division have an inverse relationship. The inverse relationship between multiplication and division can be used to solve problems.
- When dividing the remainder must be less than the divisor. The nature of the question asked determines how to interpret and use the remainder.
- Each estimation technique gives a way to replace numbers with other numbers that are close and easy to compute with mentally.

#### **ESSENTIAL QUESTIONS**

- How can we use a model to show how the standard algorithm works?
- Why is place value important in all algorithms for multiplication?
- What is the relationship between repeated addition and multiplication?
- How are multiplication and division related?
- What is the relationship between repeated subtraction and division?

#### Acquisition

#### Students will understand...

- distributive property
- set up for a long division problem
- connection between multiplying and dividing

- multiplying with multiples of 10
- estimating products
- multiplying a whole number (up to four digits) by a one-digit whole number.
- multiplying two two-digit numbers.

| Used in Content Area Standards not applicable   | 21st Century Skills     Problem solving     Communication     Perseverance   |
|---|--|
| remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. | <ul> <li>demonstrating that multiplication is the inverse of division.</li> <li>showing mastery of all division facts 0-9 with accuracy and fluency.</li> <li>finding whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division.</li> </ul> |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 4 Unit 4: Factors & Multiples

| FST | ΔΡΙ | ISH  | IFD | GO | ALS: |
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Students will continue their study of mathematics. In this unit, students will identify factors and multiples as well as find prime and composite numbers.

#### Content Standards:

- CCSS.MATH.CONTENT.4.OA.B.4: Find all factor pairs for a whole number in the range 1-100.
   Recognize that a whole number is a multiple of each of its factors. Determine whether a given whole number in the range 1-100 is a multiple of a given one-digit number. Determine whether a given whole number in the range 1-100 is prime or composite.
- CCSS.MATH.CONTENT.4.OA.A.3: Solve multistep
  word problems posed with whole numbers and
  having whole-number answers using the four
  operations, including problems in which
  remainders must be interpreted. Represent these
  problems using equations with a letter standing
  for the unknown quantity. Assess the
  reasonableness of answers using mental
  computation and estimation strategies including
  rounding.

#### **Stage 1 Desired Results**

#### Transfer

#### Students will be able to independently use their learning to...

- Name factors and multiples of a given number.
- Identify prime and composite numbers.

#### Meaning

#### ENDURING UNDERSTANDINGS

- Every counting number is divisible by 1 and itself.
- Some counting numbers are divisible by numbers beyond 1 and itself.
- The product of any nonzero number and any other nonzero number is divisible by each number and called a multiple of each number.

#### **ESSENTIAL QUESTIONS**

 In what ways are factors and multiples connected and what is the difference between them?

#### **Acquisition**

#### Students will understand...

- factor and multiple
- prime and composite
- a whole number as a product of each of its factors.
- 1 is neither prime nor composite.

- Finding all factor pairs for a whole number in the range 1 to 100
- Recognizing that a whole number is a multiple of each of its factors
- Determining whether a given whole number, in the range 0 to 100, is a multiple of a given onedigit number
- Determining whether a given whole number, in the range 0 to 100, is prime or composite.
- Using factors and multiples to solve problems

|                                | • | including finding equivalent fractions. Using multiple strategies to solve problems Assessing the reasonableness of answers |
|--------------------------------|---|---|
| Used in Content Area Standards |   | 21st Century Skills   |
|                                | • | Communication   |
| not applicable                 | • | Perseverance  |
|                                | • | Critical Thinking   |
|                                |   |   |

| Stage 2 - Evidence  |  |  |  |
|---------------------|--|--|--|
| Evaluative Criteria | Assessment Evidence  |  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

## Windham School District Curriculum Mathematics - Grade 4 Unit 5: Algebra - Patterns

|   | Stage 1 Desired Results   |  |  |
|---|---|--|--|
| ESTABLISHED GOALS:  | Transfer  |  |  |
| Students will continue their study of   | Students will be able to independently use their learning to  |  |  |
| mathematics. In this unit, students will generate   | <ul> <li>Use patterns found in a sequence to solve real-world pro</li> </ul>  | blems.   |  |
| and analyze patterns.   | Meaning   |  |  |
| <ul> <li>Content Standards:</li> <li>CCSS.MATH.CONTENT.4.OA.C.5: Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself.</li> <li>CCSS.MATH.CONTENT.4.OA.A.3: Solve multi-step word problems posed with</li> </ul> | objects that repeat in predictable ways.  | <ul> <li>ESSENTIAL QUESTIONS</li> <li>How do patterns help us to make predictions and solve problems?</li> <li>How are geometric and numerical patterns similar and different from one another?</li> <li>How can we identify features of a pattern?</li> <li>How does understanding patterns help you understand relationships between numbers?</li> </ul> |  |
| whole numbers and having whole-number answers using the four operations,  | you know the value of another quantity.  Acquisition  | 1  |  |
| including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.   | Students will understand  • patterns can be predictable.  • difference between a numerical and geometric pattern.  • pattern rules. | <ul> <li>Students will be skilled at</li> <li>extending a given pattern.</li> <li>writing a rule for a given pattern.</li> <li>identifying the features of a pattern.</li> <li>creating a pattern</li> <li>Naming a pattern's rule.</li> </ul>   |  |
| Used in Content Area Standards  |   | 21 <sup>st</sup> Century Skills  |  |
|   |   | Communication  |  |
| not applicable  |   | <ul> <li>Perseverance</li> </ul>   |  |

|  | <ul><li>Critical thinking</li><li>Problem solving</li></ul> |
|--|---|
|--|---|

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

## Windham School District Curriculum **Mathematics - Grade 4 Unit 6: Fractions/Decimals**

Fractions can be built from unit

extending understandings of

operations on whole numbers.

There is an equivalence between

fractions by applying and

fractions and decimals.

#### **Stage 1 Desired Results** ESTABLISHED GOALS: Transfer Students will continue their study of mathematics. In this unit, students will Students will be able to independently use their learning to... be able to add, subtract, multiply fractions as well as order and find Add, subtract, and multiply fractions. equivalent fractions. Students will also be able to compare decimals. Order and find equivalent fractions comparing to a benchmark fraction. Content Standards: Compare decimals. • CCSS.MATH.CONTENT.4.NF.A.1: Explain why a fraction a/b is Meaning equivalent to a fraction $(n \times a)/(n \times b)$ by using visual fraction models, ENDURING UNDERSTANDINGS **ESSENTIAL QUESTIONS** with attention to how the number and size of the parts differ even • The same fractional amount can though the two fractions themselves are the same size. Use this be represented by an infinite set principle to recognize and generate equivalent fractions. of different but equivalent CCSS.MATH.CONTENT.4.NF.A.2: Compare two fractions with different fractions. numerators and different denominators, e.g., by creating common Benchmark fractions such as ½ are fractions? denominators or numerators, or by comparing to a benchmark fraction useful when comparing two fractions to each other.

- such as 1/2. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions, e.g., by using a visual fraction model.
- CCSS.MATH.CONTENT.4.NF.B.3.B: Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model. Examples: 3/8 = 1/8 + 1/8 + 1/8; 3/8 =1/8 + 2/8; 21/8 = 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8.
- CCSS.MATH.CONTENT.4.NF.B.3.C: Add and subtract mixed numbers with like denominators, e.g., by replacing each mixed number with an

- In what situations would we need to involve fractions in a word problem?
- Why don't we add or subtract the denominators when adding/subtracting
- Why is it that when we multiply a fraction by a fraction we get a smaller result?
- Why do we multiply or divide the numerator and denominator by the same number when finding equivalent fractions?
- How can you use a model to show equivalent fractions?
- Why do we need denominators of 10 and 100 when we turn fractions into decimals?

- equivalent fraction, and/or by using properties of operations and the relationship between addition and subtraction.
- CCSS.MATH.CONTENT.4.NF.B.3.D: Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem.
- CCSS.MATH.CONTENT.4.NF.C.5: Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100.2 For example, express 3/10 as 30/100, and add 3/10 + 4/100 = 34/100.
- CCSS.MATH.CONTENT.4.NF.C.6: Use decimal notation for fractions with denominators 10 or 100. For example, rewrite 0.62 as 62/100; describe a length as 0.62 meters; locate 0.62 on a number line diagram.
- CCSS.MATH.CONTENT.4.NF.C.7: Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions, e.g., by using a visual model.
- CCSS.MATH.CONTENT.4.NF.B.4: Apply and extend previous understandings of multiplication to multiply a fraction by a whole number.
- CCSS.MATH.CONTENT.4.NF.B.4.A: Understand a fraction a/b as a multiple of 1/b. For example, use a visual fraction model to represent 5/4 as the product  $5 \times (1/4)$ , recording the conclusion by the equation  $5/4 = 5 \times (1/4)$ .
- CCSS.MATH.CONTENT.4.NF.B.4.B: Understand a multiple of a/b as a multiple of 1/b, and use this understanding to multiply a fraction by a whole number. For example, use a visual fraction model to express 3 × (2/5) as 6 × (1/5), recognizing this product as 6/5. (In general, n × (a/b) = (n × a)/b.)
- CCSS.MATH.CONTENT.4.NF.B.4.C: Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual

- Why is a hundredth smaller than a tenth when a hundred is bigger than a ten?
- How are decimals related to fractions?

#### Acauisition

Students will understand...

- addition and subtraction of fractions as joining and separating parts referring to the same whole.
- fractions with the same denominator can be decomposed into a sum of fractions in more than one way.
- fractions can be expressed as a multiple of a whole number and a fraction
- when two fractions are equivalent.
- benchmark fractions
- numerators and denominators
- place value system for decimals up to the thousandths place.

- adding and subtracting fractions and mixed numbers with like denominators.
- solving word problems involving addition and subtraction of fractions with like denominators.
- subtracting fractions from a whole.
- showing fraction addition and subtraction using models and pictures.
- solving word problems using multiplication of fractions.
- using a visual model to represent fraction multiplication.
- finding equivalent fractions.
- determining if two fractions are equivalent.
- comparing fractions with like and unlike denominators
- using <, > and = when comparing fractions.
- using visual models to compare fractions.
- identifying the relationship of "10 times as much" and "1/10 of" in multi-digit numbers within our place value system.
- reading and writing decimals from 0.001 to 10,000,000 in standard, expanded, and word form.

| fraction models and equations to represent the problem. For example, if each person at a party will eat 3/8 of a pound of roast beef, and there will be 5 people at the party, how many pounds of roast beef will be needed? Between what two whole numbers does your answer lie? | • | comparing decimals. identifying the place value of any digit in numbers 0.001 to 10,000,000. explaining the pattern in the number of zeroes and placement of the decimal point when a number is multiplied or divided by a power of 10. rounding decimals to the nearest tenths, hundredths, and thousandths. |
|---|---|---|
| Used in Content Area Standards  |   | 21 <sup>st</sup> Century Skills   |
|   | • | Communication   |
| not applicable  | • | Perseverance  |
|   | • | Problem solving   |
|   | • | Critical Thinking   |
|   |   |   |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

### Windham School District Curriculum Mathematics - Grade 4

### Unit 7: Measurement & Data - Conversion & Area/Perimeter

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Students will continue their study of mathematics. In this unit, students will find equivalence in units of measure as well as use measurement formulas to find area/perimeter.

#### Content Standards:

- CCSS.MATH.CONTENT.4.MD.A.1: Know relative sizes of measurement units within one system of units including km, m, cm; kg, g; lb, oz.; l, ml; hr, min, sec. Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit. Record measurement equivalents in a two-column table. For example, know that 1 ft is 12 times as long as 1 in. Express the length of a 4 ft snake as 48 in. Generate a conversion table for feet and inches listing the number pairs (1, 12), (2, 24), (3, 36), ...
- CCSS.MATH.CONTENT.4.MD.A.2: Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit.
   Represent measurement quantities using diagrams

#### **Stage 1 Desired Results**

#### Students will be able to independently use their learning to...

- Understand when the different forms of measurement are applicable to use
- Find equivalence in units of measure
- Use different forms of measurement to solve real-world problems

#### Meaning

Transfer

#### ENDURING UNDERSTANDINGS

- Some attributes of objects are measurable and can be quantified using unit amounts.
- Time can be expressed using different units that are related to each other.
- Some problems can be solved by applying the formula for the perimeter of a rectangle or the formula for the area of a rectangle.

#### **ESSENTIAL QUESTIONS**

- What is the importance of measuring?
- What is a system of measurement and why are there different systems?
- What is the purpose of having more than one unit of measurement within a system?
- What are some real-world situations where we would use area and perimeter?
- How are area and perimeter related?

#### **Acquisition**

#### Students will understand...

Systems of measurement

- Relative units
- Measurement equivalence
- Area and perimeter
- Formulas for rectangles
- Determine operation
- Break down (steps)
- Estimate to check

- finding area and perimeter using formulas.
- applying area and perimeter in real world problems.
- solving problems related to the addition and subtraction of time in minutes.
- finding elapsed time.
- using strategies such as a number line to solve problems relating to time intervals.

| ot applicable   | <ul> <li>Communication</li> <li>Perseverance</li> <li>Problem solving</li> <li>Critical Thinking</li> </ul>       |
|---|---|
| Jsed in Content Area Standards  | 21 <sup>st</sup> Century Skills   |
| such as number line diagrams that feature a measurement scale.  CCSS.MATH.CONTENT.4.MD.A.3: Apply the area and perimeter formulas for rectangles in real world and mathematical problems. For example, find the width of a rectangular room given the area of the flooring and the length, by viewing the area formula as a multiplication equation with an unknown factor.  CCSS.MATH.CONTENT.4.OA.A.3: Solve multi-step word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. | showing measurement data on a line plot and drawing a horizontal scale using whole numbers, halves, and quarters. |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Mathematics - Grade 4 Unit 8: Measurement & Data Lines & Angles

#### ESTABLISHED GOALS:

Students will continue their study of mathematics. In this unit, students will understand concepts of angles and angle measurement as well as understand and classify lines, angles, and shapes.

#### Content Standards:

- CCSS.MATH.CONTENT.4.MD.C.5: Recognize angles as geometric shapes that are formed wherever two rays share a common endpoint, and understand concepts of angle measurement:
- CCSS.MATH.CONTENT.4.MD.C.5.A: An angle is measured with reference to a circle with its center at the common endpoint of the rays, by considering the fraction of the circular arc between the points where the two rays intersect the circle. An angle that turns through 1/360 of a circle is called a "onedegree angle," and can be used to measure angles.
- CCSS.MATH.CONTENT.4.MD.C.5.B: An angle that turns through n one-degree angles is said to have an angle measure of n degrees.
- CCSS.MATH.CONTENT.4.OA.A.3: Solve multi-step word problems posed with whole numbers and having wholenumber answers using the four operations, including problems in which remainders must be interpreted.
   Represent these problems using equations with a letter standing for the unknown quantity. Assess the

#### **Stage 1 Desired Results**

#### Students will be able to independently use their learning to...

- Find angle measurements and use them in solving real-world problems
- Understand the connection between lines, angles, and circles.

#### Meaning

Transfer

#### ENDURING UNDERSTANDINGS

- Line segments and rays are sets of points that describe parts of lines, shapes and solids.
- Angles are formed by two intersecting lines or by rays with a common endpoint and are classified by size.

#### **ESSENTIAL QUESTIONS**

- When measuring angles, why is it important to use the correct measuring tool?
- How do angles relate to circles and lines?
- What should be taken into consideration when solving an angle's measurement?
- How is symmetry present in our everyday life?
- What strategies can be used to verify symmetry, parallel lines, and perpendicular lines?

#### Acquisition

#### Students will understand...

- angle is formed when two rays share a common endpoint.
- angles as a fraction of a circle.
- angles as turns.
- lines, line segments, and rays.

- measuring angles with a protractor.
- representing an angle measurement as a fraction over 360.
- drawing an angle with a given measurement.

| <ul> <li>reasonableness of answers using mental computation and estimation strategies including rounding.</li> <li>CCSS.MATH.CONTENT.4.G.A.1: Draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines. Identify these in two-dimensional figures.</li> <li>CCSS.MATH.CONTENT.4.G.A.2: Classify two-dimensional figures based on the presence or absence of parallel or perpendicular lines, or the presence or absence of angles of a specified size. Recognize right triangles as a category, and identify right triangles.</li> <li>CCSS.MATH.CONTENT.4.G.A.3: Recognize a line of symmetry for a two-dimensional figure as a line across the figure such that the figure can be folded along the line into matching parts. Identify line-symmetric figures and draw lines of symmetry.</li> </ul> | <ul> <li>Parallel and perpendicular lines</li> <li>classification of angles as right, acute, and obtuse.</li> <li>right triangles</li> <li>line of symmetry means that a figure can be folded on a line into matching parts.</li> </ul> | <ul> <li>solving problems related to angle addition and subtraction.</li> <li>finding an unknown angle using addition, subtraction, or sums of parts.</li> <li>identifying points, lines, line segments, rays, perpendicular, and parallel lines in two-dimensional figures.</li> <li>identify right, acute, and obtuse angles in two-dimensional figures.</li> <li>classifying two-dimensional figures based on parallel and perpendicular lines.</li> <li>identifying and drawing lines of symmetry in two-dimensional figures.</li> </ul> |
|---|---|--|
| Used in Content Area Standards  |   | 21 <sup>st</sup> Century Skills  |
| not applicable  |   | <ul><li>Communication</li><li>Perseverance</li></ul>   |
|   | <ul><li>Problem solving</li><li>Critical Thinking</li></ul>   |  |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

#### <u>Title of Curriculum:</u> 5th Grade Mathematics

| Operations: Place Value of Decimals; Adding and Subtracting Decimals               | <ul> <li>place value system</li> <li>decimal places to thousandths</li> <li>exponents</li> <li>powers of 10</li> <li>decimal point placement</li> </ul>   | • The Base Ten numeration system is a scheme for recording numbers using digits 0-9, groups of ten and place value.  | Identify the relationship between digits of a number in reference "10 times as much" and "1/10 of"      Read and write decimals in standard.   |
|--|---|--|--|
|  |   | <ul> <li>Place value patterns lead to a deeper understanding of decimal place value and increases the skill of reading and writing decimals.</li> <li>Place value can be used to compare and order whole numbers and decimals.</li> </ul>  | <ul> <li>Read and write decimals in standard, expanded and word form</li> <li>Identify place value</li> <li>Explain patterns in number of zeroes/placement of decimal when a number is multiplied or divided by a power 10</li> <li>Round decimals</li> <li>Compare and order decimals</li> <li>Add and subtract decimals to hundredths</li> <li>Explain and/or model answers</li> <li>Recognize the connections between addition and subtraction of decimals</li> <li>Check for reasonableness of answers using estimation</li> </ul> |
| Operations: Multiplying Multidigit Whole Numbers and Decimals  Unit 3: Numbers and | place value regrouping multi-digit whole numbers array area model partial products product decimal operations decimal point placement standard multiplication algorithm divisor dividend quotient | <ul> <li>The standard multiplication algorithm involving decimals is an extension of the standard algorithm for multiplying whole numbers. Place value determines the placement of the decimal point in a product.</li> <li>The product of two decimals less than one is less than either factor.</li> <li>Using models can help students understand the standard</li> </ul> | <ul> <li>Solve multi-digit multiplication problems</li> <li>Explain answers using words, rectangular arrays, and/or area models</li> <li>Multiply decimals to hundredths</li> <li>Check for reasonableness of answers using estimation</li> </ul>  |

| Decimals  | decimal point placement   | <ul> <li>algorithm for dividing whole numbers.</li> <li>Estimation techniques are beneficial when checking for reasonableness of answers.</li> <li>Dividing by 2-digit divisors is just an extension of the steps for dividing with 1-digit divisors.</li> <li>A number divided by a decimal can be represented as an equivalent calculation using place value to change the divisor to a whole number.</li> </ul>  | <ul> <li>Recognize the connection between multiplication and division of whole numbers</li> <li>Explain answers using words, rectangular arrays, and/or area models</li> <li>Check for reasonableness of answers using estimation</li> <li>Solve problems using division including decimals</li> <li>Divide decimals to hundredths</li> </ul> |
|---|---|---|---|
| Unit 4: Numbers and Operations: Adding and Subtracting Fractions and Mixed Numbers            | <ul> <li>fractions</li> <li>fraction bar</li> <li>common denominator</li> <li>mixed number</li> <li>improper fraction</li> <li>equivalent fractions</li> <li>simplest form</li> </ul> | <ul> <li>The same fractional amount can be represented by an infinite set of different but equivalent fractions.</li> <li>A fraction in simplest form is when 1 is the only common factor of the numerator and denominator.</li> <li>A number line can be used to estimate fractions to the nearest half or whole fraction.</li> <li>All whole numbers can be represented as fractions.</li> <li>Fractional amounts greater than 1 can be represented using a whole number and a fraction.</li> </ul> | Solve real world word problems using<br>addition and subtraction of fractions and<br>mixed numbers  |
| Unit 5: Numbers and<br>Operations: Multiplying and<br>Dividing Fractions and Mixed<br>Numbers | <ul> <li>improper fraction</li> <li>mixed number</li> <li>equivalence</li> <li>simplest form</li> <li>area</li> </ul>   | When you multiply two fractions<br>that are both less than 1, the<br>product is smaller than either<br>fraction.  | <ul> <li>Multiply fractions with whole numbers</li> <li>Multiply mixed numbers</li> <li>Solve word problems involving multiplying fractions and/or mixed numbers</li> </ul>   |

|  | <ul> <li>inverse operations</li> <li>multiplication/division relationship</li> <li>reciprocal</li> </ul>   | <ul> <li>One way to find the product of mixed numbers is to change the calculation to an equivalent one involving improper fractions.</li> <li>The inverse relationship between multiplication and division can be used to divide with fractions.</li> <li>The inverse relationship between multiplication and division can be used to divide with fractions.</li> <li>Divide unit fractions by whole numbers and whole numbers by unit fractions</li> <li>Explain answers using words, models and the relationship between multiplication and division</li> </ul>   |
|--|--|--|
| Unit 6: Geometry and Data:<br>Volume Concepts and<br>Measurement Conversions | <ul> <li>volume</li> <li>cubic units</li> <li>formula</li> <li>base</li> <li>area</li> <li>unit cubes</li> <li>three-dimensional figure</li> <li>right rectangular prism</li> <li>solid figure</li> <li>measurement system</li> <li>conversions</li> <li>metric</li> <li>U.S. Customary</li> </ul> | <ul> <li>Many everyday objects closely approximate standard geometric solids.</li> <li>Volume is a measure of the amount of space inside a solid.</li> <li>Relationships exist that enable you to convert between units of measurements by multiplying or dividing.</li> <li>Find the volume of a right rectangular prism by counting cubic units.</li> <li>Find the volume of a right rectangular prism by counting cubic units.</li> <li>Find the volume of a right rectangular prism by counting cubic units.</li> <li>Find the volume of a right rectangular prism by counting cubic units.</li> <li>Create multiple solid figures given a common volume.</li> <li>Solve real world problems related to volume</li> <li>Find the volume of a solid figure formed by two right rectangular prisms.</li> <li>Convert within a measurement system</li> <li>Solve multi-step, real world problems involving conversions within a measurement system</li> </ul> |
| Unit 7: Algebraic Thinking:<br>Numerical Expressions                         | <ul> <li>grouping symbols</li> <li>parentheses, brackets, braces</li> <li>order of operations</li> <li>numerical expressions</li> </ul>  | <ul> <li>There is an agreed upon order for which operations in a numerical expression are performed.</li> <li>Some mathematical phrases can be represented using mathematical expressions.</li> <li>Simplify expressions involving parentheses, brackets, braces using order of operations</li> <li>Write simple expressions given verbal or word-form expressions</li> </ul>  |
| Unit 8: Geometry and Data:<br>Coordinate Plane and                           | <ul><li>coordinate plane</li><li>x-axis</li></ul>  | <ul> <li>Relationships can be described and generalizations made for</li> <li>Plot ordered pairs on a coordinate plane</li> </ul>  |

|                               |  |  | _  |
|-------------------------------|--|--|--|
| Classifying Two-Dimensional   | • y-axis                                       | mathematical situations that have              | Name coordinate pairs on a coordinate                          |
| Figures & Algebraic Thinking: | • origin                                       | numbers or objects that repeat in              | plane  |
| Analyzing Patterns and        | coordinate                                     | predictable ways.                              | Represent real world problems involving                        |
| Relationships                 | ordered pair                                   | The coordinate system is a                     | the first quadrant of the coordinate plane                     |
|                               | first quadrant                                 | scheme that uses two                           | • Explain the meaning of each coordinate in                    |
|                               | <ul><li>hierarchy</li></ul>                    | perpendicular lines intersecting at            | t the context of the problem                                   |
|                               | <ul> <li>properties/attributes</li> </ul>      | a 0 to name the location of points             | Form and plot coordinate pairs based on                        |
|                               | <ul> <li>categories/subcategories</li> </ul>   | on a plane.                                    | numerical patterns   |
|                               | <ul> <li>two-dimensional figures</li> </ul>    | <ul> <li>Mathematical relationships</li> </ul> | Locate and label the origin on a coordinate                    |
|                               | <ul><li>classifying/grouping</li></ul>         | represented by rules can also be               | plane  |
|                               | <ul> <li>triangles by angles and by</li> </ul> | represented by a graph of the                  | • Explain the differences between the terms:                   |
|                               | sides  | rule. Ordered pairs that satisfy               | axis, coordinate and ordered pairs                             |
|                               | <ul> <li>classifying quadrilaterals</li> </ul> | the rule can be used to graph the              | <ul> <li>Classify and group two-dimensional figures</li> </ul> |
|                               | <ul> <li>relationships between</li> </ul>      | data.  | in a hierarchy based on properties                             |
|                               | corresponding terms                            | Two-dimensional figures can be                 | <ul> <li>Give all names for a given figure</li> </ul>          |
|                               |  | classified in a hierarchy based on             | Name a common property of a group of                           |
|                               |  | their properties.                              | figures  |
|                               |  |  | <ul> <li>Generate patterns given rules</li> </ul>              |
|                               |  |  | <ul> <li>Identify relationships between</li> </ul>             |
|                               |  |  | corresponding terms  |
|                               |  |  | Form ordered pairs from corresponding                          |
|                               |  |  | terms in two patterns and graph them on a                      |
|                               |  |  | coordinate plane   |

# Windham School District Curriculum Mathematics - Grade 5 Unit 1: Numbers & Operations Place Value & Adding & Subtracting Decimals

#### ESTABLISHED GOALS:

Students will continue their study in Mathematics in the area of Numbers and Operations. In this unit students will gain a deeper understanding about place value from millions to thousandths while mastering the relationship between the different place values. They will gain an understanding of how to add and subtract decimals to the hundredths place.

#### Content Standards:

- CCSS.5.NBT.2 Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole number exponents to denote powers of 10.
- CCSS.5.NBT.1. Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left
- CCSS.5.NBT.3. Read, write, and compare decimals to thousandths.

#### **Stage 1 Desired Results**

#### Students will be able to independently use their learning to...

 use knowledge of place value to manipulate numbers using various operations to solve real-life word problems.

Transfer

#### Meaning

#### ENDURING UNDERSTANDINGS

- The Base Ten numeration system is a scheme for recording numbers using digits 0-9, groups of ten and place value.
- Place value patterns lead to a deeper understanding of decimal place value and increases the skill of reading and writing decimals.
- Place value can be used to compare and order whole numbers and decimals.

#### **ESSENTIAL QUESTIONS**

- How can you describe the relationship between any two place-value positions?
- How can you use exponents to represent powers of 10?
- How do you represent whole numbers and decimals?
- How can you use place value to round decimals to a given place value?
- How can you use base-ten blocks to model decimal addition/subtraction?

#### Students will understand...

- place value system
- decimal places to thousandths
- exponents
- powers of 10
- decimal point placement

### Acquisition Students will be skilled at...

- identifying the relationship between digits of a number in reference "10 times as much" and "1/10 of"
- reading and writing decimals in standard, expanded and word form
- identifying place value

| <ul> <li>CCSS.5.NBT.4 Use place value understanding to round decimals to any place.</li> <li>CCSS.5.NBT.7. Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties, of operations, and/or the relationship between addition and subtractions; relate the strategy to a written method and explain the reasoning used.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP1 Make sense of problems and persevere</li> </ul> | <ul> <li>Explaining patterns in the number of zeros and the placement of a decimal point when a number is multiplied or divided by a power 10</li> <li>rounding decimals</li> <li>comparing and ordering decimals</li> <li>Adding and subtracting decimals to hundredths</li> <li>Explaining and/or modeling answers</li> <li>Recognizing the connections between addition and subtraction of decimals</li> <li>Checking for reasonableness of answers using estimation</li> </ul> |
|---|--|
| <ul> <li>mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul>   |  |
| Used in Content Area Standards  | 21 <sup>st</sup> Century Skills  |
|   | Critical thinking     Communication  |
|   | Communication  |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Mathematics - Grade 5 Unit 2: Numbers & Operations Multiplying Whole Numbers & Decimals

#### ESTABLISHED GOALS:

Students will continue their study in Mathematics in the area of Numbers and Operations. In this unit students will master multi-digit multiplication of whole numbers and decimals.

#### Content Standards:

- CCSS.5.NBT.5. Fluently multiply whole numbers using the standard algorithm.
- CCSS.5.NBT.7. Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties, of operations, and/or the relationship between addition and subtractions; relate the strategy to a written method and explain the reasoning used.
- CCSS.MP4 Model with mathematics.
- CCSS.MP6 Attend to precision.
- CCSS.MP1 Make sense of problems and persevere in solving them. CCSS.MP4 Model with mathematics.
- CCSS.MP8 Look for and express regularity in repeated reasoning.

#### **Stage 1 Desired Results**

#### Students will be able to independently use their learning to...

use their knowledge of multiplying whole numbers to multiply decimals and apply it to solving word problems.

Transfer

#### Meaning

#### ENDURING UNDERSTANDINGS

- The standard multiplication algorithm involving decimals is an extension of the standard algorithm for multiplying whole numbers. Place value determines the placement of the decimal point in a product.
- The product of two decimals less than one is less than either factor.

#### **ESSENTIAL QUESTIONS**

- How can you use a basic fact or diagram (array area model) and a pattern to multiply a two digit number?
- How can your understanding of partial products and place value inform your use of the standard algorithm?
- How can powers of ten help you determine the digits' placement in relation to the decimal point?
- How can you use models to multiply a decimal and whole number?
- What is the connection between multiplying whole numbers and decimals?

#### Acquisition

#### Students will understand...

- place value
- regrouping

- multiplying multi-digit whole numbers fluently
- solving multi-digit multiplication problems

|                                | <ul> <li>multi-digit whole numbers</li> <li>array area model</li> <li>partial products</li> <li>product</li> <li>decimal operations</li> <li>decimal point placement</li> <li>standard multiplication algorithm</li> </ul> | • | explaining answers using words, rectangular arrays, and/or area models multiplying decimals to hundredths checking for reasonableness of answers using estimation solving problems using multiplication of decimals |
|--------------------------------|--|---|---|
| Used in Content Area Standards |  |   | 21 <sup>st</sup> Century Skills   |
|                                |  | • | Critical thinking   |
|                                |  | • | Communication   |
|                                |  |   |   |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Mathematics - Grade 5 Unit 3: Numbers & Operations Dividing Whole Numbers & Decimals

#### ESTABLISHED GOALS:

Students will continue their study in Mathematics in the area of Numbers and Operations. In this unit students will master multi-digit division of whole numbers and will gain an understanding of how to divide decimals.

#### Content Standards:

- CCSS.5.NBT.6. Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculations by using equations, rectangular arrays, and/or area models.
- CCSS.5.NBT.7. Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties, of operations, and/or the relationship between addition and subtractions; relate the strategy to a written method and explain the reasoning used.

#### **Stage 1 Desired Results**

#### Students will be able to independently use their learning to...

- use their understanding of dividing decimals to solve real-life word problems
- gain a deeper understanding of estimation.

#### Meaning

Transfer

#### ENDURING UNDERSTANDINGS

- Using models can help students understand the standard algorithm for dividing whole numbers.
- Estimation techniques are beneficial when checking for reasonableness of answers.
- Dividing by 2-digit divisors is just an extension of the steps for dividing with 1-digit divisors.
- A number divided by a decimal can be represented as an equivalent calculation using place value to change the divisor to a whole number.

#### ESSENTIAL QUESTIONS

- How is multiplication used to solve a division problem within the standard algorithm?
- How can powers of ten help you determine the digits' placement in relation to the decimal point?
- How can you use models to divide decimals?

#### Acquisition

#### Students will understand...

- divisor
- dividend
- quotient
- decimal point placement

- dividing multi-digit whole numbers
- recognizing the connection between multiplication and division of whole numbers
- explaining answers using words, rectangular arrays, and/or area models

|  | <ul><li>Critical thinking</li><li>Communication</li></ul>  |
|--|--|
| Used in Content Area Standards   | 21st Century Skills  |
| <ul> <li>CCSS.MP1 Make sense of problems and persevere in solving them. CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul> | <ul> <li>checking for reasonableness of answers using estimation</li> <li>solving problems using division including decimals</li> <li>dividing decimals to hundredths</li> </ul> |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Mathematics - Grade 5 Unit 4: Numbers & Operations Adding & Subtracting Fractions & Mixed Numbers

#### ESTABLISHED GOALS:

Students will continue their study in Mathematics in the area of Number and Operations. In this unit students will gain an understanding of how to add and subtract fractions and mixed numbers with unlike denominators.

#### Content Standards:

- CCSS.5.NF.1. Add and subtract fractions with unlike denominators (including mixed numbers) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators. For example, 2/3 +5/3 = 15/12 = 23/12. (In general, a/b + c/d = (ad + bc)/bd).
- CCSS.5.NF.2. Solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators, e.g., by using visual fraction models or equations to represent the problem. Use benchmark fractions and number sense of fractions to estimate mentally and assess the reasonableness of answers. For example,

#### Stage 1 Desired Results

#### Students will be able to independently use their learning to...

- use adding and subtracting fractions to solve word problems
- Use their increased knowledge base in number and operations when learning algebraic skills.

Transfer

Meanina

#### **ENDURING UNDERSTANDINGS**

- The same fractional amount can be represented by an infinite set of different but equivalent fractions.
- A fraction in simplest form is when 1 is the only common factor of the numerator and denominator.
- A number line can be used to estimate fractions to the nearest half or whole fraction.
- All whole numbers can be represented as fractions.
- Fractional amounts greater than 1 can be represented using a whole number and a fraction

#### **ESSENTIAL QUESTIONS**

- How can you use models to add and subtract fractions that have different denominators?
- How can you use your knowledge of factors to rewrite a pair of fractions so they have a common denominator?
- Can you explain why the denominators are not combined?
- How can you use regrouping to find the sums and differences of two mixed numbers?

#### Acquisition

#### Students will understand...

- fractions
- fraction bar
- common denominator

- Adding and subtracting fractions with unlike denominators
- Adding and subtracting mixed numbers

| <ul> <li>recognize an incorrect result 2/5 + 1/2 = 3/7, by observing that 3/7 &lt; 1/2.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul> | <ul> <li>mixed number</li> <li>improper fraction</li> <li>equivalent fractions</li> <li>simplest form</li> </ul> | <ul> <li>Determining equivalent fractions</li> <li>Using estimation to check for reasonableness of answers</li> <li>Solving real world word problems using addition and subtraction of fractions and mixed numbers</li> </ul> |
|---|--|---|
| Used in Content Area Standards  |  | • Critical thinking   |
|   |  | <ul> <li>Communication</li> </ul>   |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

## Windham School District Curriculum Mathematics - Grade 5

### **Unit 5: Numbers & Operations - Multiplying & Dividing Fractions**

## Stage 1 Desired Results ESTABLISHED GOALS:

Students will continue their study in Mathematics in the area of Numbers and Operation. In this unit students will gain an understanding of how to multiply and fractions and mixed numbers. They will also gain an understanding of how to divide fractions using the reciprocal of a unit fraction.

#### Content Standards:

- CCSS.5.NF.4. Apply and extend previous understandings of multiplication to multiply a fraction or whole number by a fraction.
- CCSS.5.NF.5. Interpret multiplication as scaling (resizing), by:
- CCSS.MATH.CONTENT.5.NF.B.5.A: Comparing the size of a product to the size
  of one factor on the basis of the size of the other factor, without performing
  the indicated multiplication.
- CCSS.MATH.CONTENT.5.NF.B.5.B: Explaining why multiplying a given number by a fraction greater than 1 results in a product greater than the given number (recognizing multiplication by whole numbers greater than 1 as a familiar case); explaining why multiplying a given number by a fraction less than 1 results in a product smaller than the given number; and relating the principle of fraction equivalence  $a/b = (n \times a)/(n \times b)$  to the effect of multiplying a/b by 1.
- CCSS.5.NF.6. Solve real world problems involving multiplication of fractions and mixed numbers, e.g., by using visual fraction models or equations to represent the problem.
- CCSS.5.NF.3. Interpret a fraction as division of the numerator by the denominator ( $a/b = a \div b$ ). Solve word problems involving division of whole

#### Transfer

#### Students will be able to independently use their learning to...

- use their knowledge of multiplying fractions and mixed numbers to simplify expressions and solve equations
- make a connection between multiplying and dividing fractions
- Use their knowledge of number operations in real-life contexts

#### Meaning

#### ENDURING UNDERSTANDINGS

- When you multiply two fractions that are both less than 1, the product is smaller than either fraction.
- One way to find the product of mixed numbers is to change the calculation to an equivalent one involving improper fractions.
- The inverse relationship between multiplication and division can be used to divide with fractions.

#### **ESSENTIAL QUESTIONS**

- How can you use modeling to visualize the process of fraction multiplication?
- How can you use a model to show the fractional part of a quantity?

#### Acquisition

#### Students will understand...

- improper fraction
- mixed number
- equivalence
- simplest form
- area

- Multiplying using fractions and whole numbers as factors
- Multiplying using mixed numbers

| •   | numbers leading to answers in the form of fractions or mixed numbers, e.g., by using visual fraction models or equations to represent the problem. For example, interpret 3/4 as the result of dividing 3 by 4, noting that 3/4 multiplied by 4 equals 3, and that when 3 wholes are shared equally among 4 people each person has a share of size 3/4. If 9 people want to share a 50-pound sack of rice equally by weight, how many pounds of rice should each person get? Between what two whole numbers does your answer lie?  CCSS.5.NF.7. Apply and extend previous understandings of division to divide unit fractions by whole numbers and whole numbers by unit fractions.  CCSS.5.NF.B.7.C: Solve real world problems involving division of unit fractions by non-zero whole numbers and division of whole numbers by unit fractions, e.g., by using visual fraction models and equations to represent the problem. For example, how much chocolate will each person get if 3 people share 1/2 lb. of chocolate equally? How many 1/3-cup servings are in 2 cups of raisins?  CCSS.MP1 Make sense of problems and persevere in solving them.  CCSS.MP2 Reason abstractly and quantitatively.  CCSS.MP4 Model with mathematics.  CCSS.MP5 Use appropriate tools strategically.  CCSS.MP6 Attend to precision.  CCSS.MP8 Look for and express regularity in repeated reasoning. | <ul> <li>inverse operations</li> <li>multiplication/division relationship</li> <li>reciprocal</li> </ul> | <ul> <li>Solving word problems involving multiplying fractions and/or mixed numbers</li> <li>Finding the area of a rectangle with fractional side lengths</li> <li>Comparing the size of factors to the size of a product</li> <li>Solving real life word problems involving the division of whole numbers that give quotients of fractions or mixed numbers</li> <li>Dividing unit fractions by whole numbers and whole numbers by unit fractions</li> <li>Explaining answers using words, models and the relationship between multiplication and division</li> </ul> |
|-----|---|--|--|
| Use | ed in Content Area Standards  |  | 21 <sup>st</sup> Century Skills  |
|     |   |  | <ul><li>Critical thinking</li><li>Communication</li></ul>  |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Mathematics - Grade 5 Unit 6: Geometry & Data Volume Concepts & Measurement Conversions

#### ESTABLISHED GOALS:

Students will continue their study in Mathematics in the area of Geometry and Data. In this unit students will gain an understanding of volume as an attribute of solid figures and how to compute the volume of right rectangular prisms. Students will also be able to convert measurements within the metric or U.S. Customary systems.

- Content Standards:
  - CCSS.5.MD.1. Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05m), and use these conversions in solving multi-step, real world problems.
- CCSS.5.MD.3. Recognize volume as an attribute of solid figures and understand concepts of volume measurement.
- CCSS.5.MD.4. Measure volumes by counting unit cubes, using cubic cm, cubic in, cubic ft., and improvised units.
- CCSS.5.MD.5. Relate volume to the operations of multiplication and addition and solve real world and CCSS.MP1 Make sense of problems and persevere in solving them.
- CCSS.MP3 Construct viable arguments and critique the reasoning of others.
- CCSS.MP6 Attend to precision.
- CCSS.MP7 Look for and make use of structure.

### Stage 1 Desired Results

#### Students will be able to independently use their learning to...

use their conceptual understanding of volume to compare volumes of different solids

Transfer

- apply their knowledge of measurement and conversions in science classes
- Apply their knowledge of geometry concepts in real life contexts

#### Meaning

#### ENDURING UNDERSTANDINGS

- Many everyday objects closely approximate standard geometric solids.
- Volume is a measure of the amount of space inside a solid.
- Relationships exist that enable you to convert between units of measurements by multiplying or dividing.

#### **ESSENTIAL QUESTIONS**

- What is a unit cube and how can you use it to build a solid figure?
- How can you use unit cubes to find the volume of a right rectangular prism and cube?
- How can you use multiplication to find the volume of a right rectangular prism?
- How does the area of the base of a prism relate to the volume of a right rectangular prism?
- How can you compare and convert metric units using base ten multiplication and division knowledge?
- How can you compare and convert customary units of length, capacity, and weight?

| CCSS.MP8 Look for and express regularity in repeated |   | Acquisition  |
|--|---|--|
| reasoning. mathematical problems involving volume.   | Students will understand  volume cubic units formula base area unit cubes three-dimensional figure right rectangular prism solid figure | <ul> <li>Students will be skilled at</li> <li>Finding the volume of a right rectangular prism by counting cubic units</li> <li>Finding the volume of a right rectangular prism using a formula</li> <li>Creating multiple solid figures given a common volume.</li> <li>Solving real world problems related to volume</li> <li>Finding the volume of a solid figure formed by two right rectangular prisms</li> <li>Converting within a measurement system</li> <li>Solving multi-step, real world problems involving conversions within a measurement system</li> </ul> |
| Used in Content Area Standards                       | 21st Century Skills   |  |
|  |   | <ul><li>Critical thinking</li><li>Communication</li><li>Technology literacy</li></ul>  |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 5 Unit 7: Algebraic Thinking - Numerical Expressions

| Stage 1 Desired Results  |  |  |  |
|--|--|--|--|
| ESTABLISHED GOALS:   | Tr   | ansfer   |  |
| Students will continue their study in Mathematics in the area of   | Students will be able to independently use their learning to   |  |  |
| Algebraic Thinking. In this unit students will solve various expressions   | <ul> <li>apply order of operations to more cor</li> </ul>  | nplex algebraic expressions within algebra.  |  |
| using order of operations.   | Me   | eaning   |  |
| <ul> <li>Content Standards:</li> <li>CCSS.5.OA.1. Use parentheses, brackets, or braces in numerical expressions, and evaluate expressions with these symbols.</li> <li>CCSS.5.OA.2. Write simple expressions that record calculations with numbers, and interpret numerical expressions without evaluating them. For example, express the calculation "add 8 and 7, then multiply by 2" as 2 x (8 = 7). Recognize that 3 x (18932 + 921) is three times as large as 18932 + 921, without having to calculate the indicated sum or product.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP2 Reason abstractly and quantitatively</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP7 Look for and make use of structure.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul> | <ul> <li>ENDURING UNDERSTANDINGS</li> <li>There is an agreed upon order for which operations in a numerical expression are performed.</li> <li>Some mathematical phrases can be represented using mathematical expressions.</li> </ul> | <ul> <li>ESSENTIAL QUESTIONS</li> <li>Why are parentheses, brackets and braces important in numerical expressions?</li> <li>How does the order of operations impact the answer?</li> </ul>                                   |  |
|  | Acquisition  |  |  |
|  | <ul> <li>Students will understand</li> <li>grouping symbols</li> <li>parentheses, brackets, braces</li> <li>order of operations</li> <li>numerical expressions</li> </ul>  | <ul> <li>Students will be skilled at</li> <li>Simplifying expressions involving parentheses, brackets, braces using order of operations</li> <li>Writing simple expressions given verbal or word-form expressions</li> </ul> |  |
| Used in Content Area Standards   |  | 21 <sup>st</sup> Century Skills  |  |
|  |  | Critical thinking  |  |
|  |  | Communication  |  |

#### **Stage 2 - Evidence**

| Evaluative Criteria | Assessment Evidence  |
|---------------------|--|
|                     | ASSESSMENT: Written Assessments or Projects                                  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |

# Windham School District Curriculum Mathematics - Grade 5

## Unit 8: Geometry & Data - Coordinate Plane, Classifying Two-Dimensional Figures, & Analyzing Patterns & Relationships

#### ESTABLISHED GOALS:

Students will continue their study in Mathematics in the area of Geometry and Data. In this unit students will learn about the Coordinate Plane and be able to graph points and solve real-world problems by graphing points. Students will also be able to classify and identify characteristics of two dimensional figures. Lastly, students will analyze and identify different number patterns and apply them to real-life word problems.

#### Content Standards:

CCSS.5.G.1. Use a pair of perpendicular number lines, called axes, to define a coordinate system, with the intersection of the lines (the origin) arranged to coincide with the 0 on each line and a given point in the plan located by using an ordered pair of numbers, called its coordinates. Understand that the first number indicates how far to travel from the origin in the direction of one axis, and the second number indicates how far to travel in the direction of the second axis, with the convention that the names of the two axes and the coordinates correspond (e.g., x-axis and x-coordinate, y-axis and y-coordinate).

#### **Stage 1 Desired Results**

#### Students will be able to independently use their learning to...

use their understanding of graphing ordered pairs to make connections to real life problems such as map locations.

Transfer

- see how different figures exist in our world
- apply number patterns to the coordinate plane when creating lines on a graph.

#### Meaning

#### **ENDURING UNDERSTANDINGS**

- Relationships can be described and generalizations made for mathematical situations that have numbers or objects that repeat in predictable ways.
- The coordinate system is a scheme that uses two perpendicular lines intersecting at a 0 to name the location of points on a plane.
- Mathematical relationships represented by rules can also be represented by a graph of the rule. Ordered pairs that satisfy the rule can be used to graph the data.
- Two-dimensional figures can be classified in a hierarchy based on their properties.

#### **ESSENTIAL QUESTIONS**

- How can you identify and plot points on a coordinate grid?
- How can you use a coordinate grid to display data?
- How can you identify a relationship within the numerical patterns they generate?
- How can you classify and compare triangles and quadrilaterals?
- What types of relationships can occur between corresponding terms in two different numerical patterns?

#### Acauisition

#### Students will understand...

coordinate plane

#### Students will be skilled at...

Plotting ordered pairs on a coordinate plane

| <ul> <li>CCSS.5.G.2. Represent real world and mathematical problems by graphing points in the first quadrant of the coordinate plane, and interpret coordinate values of points in the context of the situation.</li> <li>CCSS.5.G.3. Understand that attributes belonging to a category of two-dimensional figures also belong to all subcategories of that category. For example, all rectangles have 4 right angles and squares are rectangles, so all squares have 4 right angles.</li> <li>CCSS.5.G.4. Classify two-dimensional figures in a hierarchy based on properties.</li> <li>CCSS.5.OA.3. Generate two numerical patterns using two given rules. Identify apparent relationships between corresponding terms. Form ordered pairs consisting of corresponding terms from the two patterns, and graph the ordered pairs on a coordinate plane.</li> <li>CCSS.MP2 Reason abstractly and quantitatively</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul> | <ul> <li>axis</li> <li>x-axis</li> <li>y-axis</li> <li>origin</li> <li>coordinate</li> <li>ordered pair</li> <li>first quadrant</li> <li>hierarchy</li> <li>properties/attributes</li> <li>categories/subcategories</li> <li>two-dimensional figures</li> <li>classifying/grouping</li> <li>triangles by angles and by sides</li> <li>classifying quadrilaterals</li> <li>relationships between corresponding terms</li> </ul> | • | Naming coordinate pairs on a coordinate plane Representing real world problems involving the first quadrant of the coordinate plane Explaining the meaning of each coordinate in the context of the problem Forming and plotting coordinate pairs based on numerical patterns Locating and labeling the origin on a coordinate plane Explaining the differences between the terms: axis, coordinate and ordered pairs Classifying and grouping two-dimensional figures in a hierarchy based on properties Giving all names for a given figure Naming a common property of a group of figures Generating patterns given rules Identifying relationships between corresponding terms Forming ordered pairs from corresponding terms in two patterns and graph them on a coordinate plane |
|---|--|---|--|
| Used in Content Area Standards  |  |   | 21 <sup>st</sup> Century Skills  |
|   |  | • | Communication Critical thinking  |
|   |  |   |  |

| Stage 2 - Evidence                          |  |  |  |
|---|--|--|--|
| Evaluative Criteria Assessment Evidence     |  |  |  |
| ASSESSMENT: Written Assessments or Projects |  |  |  |
|   | Other Evidence: independent practice, classroom observations and discussions |  |  |

#### <u>Title of Curriculum</u>: Grade 6 Mathematics

| Unit Name  | What   | Why? How   |  |
|--|--|--|--|
| Unit 1: Number and<br>Operations: Ratios and<br>Proportional | <ul> <li>Proportions</li> </ul>  | <ul> <li>(Enduring Understanding)</li> <li>A ratio or rate describes the relationship between two quantities.</li> <li>Ratio reasoning can be applied to</li> </ul>  | <ul> <li>(skills)</li> <li>Simplify ratios</li> <li>Compare ratios in different formats</li> <li>Find equivalent ratios</li> </ul>   |
| Relationships  | <ul> <li>Fraction, decimal, percent conversions</li> <li>Terminating and repeating decimals</li> <li>ratios as a fraction or percentage</li> <li>equivalent ratios</li> <li>a rate is a ratio involving units</li> <li>100% is all of the original amount</li> </ul> | <ul> <li>many different types of mathematical and real-life problems</li> <li>A rate is a type of ratio that represents a measure or quantity. Therefore the process for solving ratio problems can be applied to rates.</li> </ul>  | <ul> <li>Calculate unit rate</li> <li>Find a missing number in a proportion</li> <li>Interchange fractions, decimals and percents</li> <li>Find percent of a quantity.</li> <li>Solve percent real world problems</li> </ul> |
| Unit 2: Number and<br>Operations: Fractions<br>and Decimals  | <ul> <li>Factors</li> <li>Multiples</li> <li>Place Value</li> <li>Reciprocal</li> <li>Dividend</li> <li>Divisor</li> <li>Quotient</li> <li>the value of a digit in relationship to its position in a number</li> </ul>   | <ul> <li>Multiplication and division are inverse operations.</li> <li>Operations on decimals and whole numbers are based upon place value relationships.</li> <li>Number lines are visual models used to represent the density principle: between any two whole numbers are many rational numbers, including decimals and fractions.</li> <li>The magnitude of numbers affects the outcome of operations on them.</li> <li>Computational fluency includes applying the most effective and efficient strategy when applicable.</li> </ul> | <ul> <li>Divide fractions by fractions</li> <li>Find common factors, greatest common factors, and multiples</li> <li>Add, subtract, multiply and divide mixed numbers</li> <li>Divide decimals</li> </ul>                    |
| Unit 3: Numbers and<br>Operations - Integers                 | <ul><li>Integers</li><li>Rational Number</li><li>Absolute Value</li></ul>  | <ul> <li>Positive and negative numbers are<br/>used together to describe quantities<br/>having opposite directions or values</li> </ul>  | Create a number line with integers   |

|  | <ul> <li>Opposite</li> <li>Number Line</li> <li>Coordinate Plane</li> <li>X Axis</li> <li>Y Axis</li> <li>Reflection</li> <li>Horizontal</li> <li>Vertical</li> <li>absolute value as the distance away from zero on a number line</li> </ul> | <ul> <li>All rational numbers can be represented as a point on the number line.</li> <li>Students will understand that absolute value is the distance from zero on a number line.</li> <li>The coordinate plane can be used to describe location in two dimensions, defined by an ordered pair.</li> </ul>  | <ul> <li>Understand the relationship between a positive or negative number and its opposite</li> <li>Find missing values in a situation</li> <li>Graph with positive and negative coordinates</li> </ul>  |
|--|---|---|---|
| Unit 4: Algebraic Thinking - expressions | <ul> <li>Algebraic expressions</li> <li>Exponents</li> <li>Constant</li> <li>Coefficient</li> <li>Term</li> <li>Like Terms</li> <li>Variable</li> <li>Distributive Property</li> </ul>  | <ul> <li>Expressions are powerful tools for exploring, reasoning about, and representing situations.</li> <li>Variables have many different meanings, depending on context and purpose.</li> <li>Variables permit writing expressions whose values are unknown or vary under different circumstances.</li> <li>Two or more expressions may be equivalent, even when their symbolic forms differ.</li> <li>Linear expressions may be added to or subtracted from one another.</li> </ul> | understandings of arithmetic to algebraic expressions, including whole number exponents   |
| Unit 5: Algebraic<br>Thinking: Equations | <ul> <li>Equations</li> <li>Inequalities</li> <li>Greater than</li> <li>Less than</li> <li>Greater than or equal to</li> <li>Less than or equal to</li> <li>Dependant Variable</li> </ul>   | <ul> <li>Solving an equation is a process of answering a question by finding the value of the variable that makes the equation true.</li> <li>An equation is two equivalent expressions.</li> <li>Variables are used to represent two</li> </ul>  | <ul> <li>Write an equation to express one quantity, the dependent variable, in terms of the other quantity, the independent variable.</li> <li>Write an equation from data tables and graphs</li> <li>Define a variable and create an equation</li> </ul> |

|                                      | <ul> <li>Independent Variable</li> <li>Constant</li> <li>Coefficient</li> <li>Substitution</li> <li>Equivalent</li> </ul> | quantities in a real world problem that change in relationship to one another.  and / or an inequality from a word problem  Solve one step equations and inequalities         |
|--------------------------------------|---|---|
| Unit 6: Geometry and Data - Area and | <ul><li>Length</li><li>Width</li></ul>  | <ul> <li>The area of all 2-dimensional figures can be calculated by breaking</li> <li>Draw a net for a given solid</li> <li>Calculate area of the irregular shapes</li> </ul> |
| Surface Area                         | Parallelogram   | irregular shapes into rectangles or  Calculate area of the fregular shapes  • Calculate area and surface area using   |
|                                      | Altitude  | triangles. models   |
|                                      | Trapezoid   | A three-dimensional figure can be     Fluently calculate area and surface area  |
|                                      | <ul> <li>Area as space inside a figure</li> </ul>   | represented by two-dimensional using formulas   |
|                                      | Area of a parallelogram A = bh  | nets, which can help determine the   • Calculate surface area of rectangular  |
|                                      | • Area of a triangle A = ½ bh   | surface area of three-dimensional prisms  |
|                                      | <ul> <li>Area of a trapezoid A = ½ (b1 + b2)h</li> </ul>  | figures.  |
|                                      | Units squared   |   |
|                                      | Net   |   |
|                                      | Surface Area  |   |
|                                      | Area  |   |
|                                      | Composite Figures   |   |
|                                      | Kite  |   |
|                                      | Compose   |   |
|                                      | • decompose   |   |
|                                      | • irregular shapes  |   |
|                                      | <ul><li>Two-dimensional figures</li><li>three-dimensional figures</li></ul>   |   |
|                                      | <ul><li>three-dimensional figures</li><li>faces, edges, vertices.</li></ul>   |   |
|                                      | Solid   |   |
|                                      | • prism   |   |
|                                      | lateral surface area  |   |
|                                      | <ul> <li>area is the surface inside a flat,</li> </ul>  |   |
|                                      | closed figure.  |   |

| Unit 7: Geometry and<br>Data - Volume                        | <ul> <li>irregular shapes are the combination of multiple figures.</li> <li>nets are three-dimensional figures drawn on a surface.</li> <li>surface area is the sum of the areas of all faces.</li> <li>Polygon</li> <li>Polyhedron</li> <li>Edge</li> <li>Vertex</li> <li>Length</li> <li>Width</li> <li>Depth</li> <li>Cubic Units</li> <li>Formula: V=LWH or V=Bh</li> <li>Irregular Figures</li> <li>Prism</li> <li>volume as the space inside a solid.</li> </ul> | <ul> <li>Volume is the number of cubes that can fit inside of a solid.</li> <li>The generic formula for volume is the area of the base multiplied by the height.</li> </ul>   | <ul> <li>Find volume by packing it with unit cubes of the appropriate unit fraction edge lengths (modeling)</li> <li>Identify faces, edges, and vertices</li> <li>Calculate volume using models</li> <li>Fluently calculate volume using formulas</li> <li>Solve real word problems involving volume</li> </ul>  |
|--|--|---|--|
| Unit 8: Geometry and<br>Data - Statistics and<br>Probability | <ul> <li>Variability</li> <li>Data</li> <li>statistical questioning</li> <li>statistical process</li> <li>Sample</li> <li>bar graph</li> <li>Frequency</li> <li>Mode</li> <li>dot plot</li> <li>Distribution</li> <li>Symmetric</li> <li>Outliers</li> <li>Histogram</li> <li>Measure of center</li> </ul>   | <ul> <li>A statistical question anticipates variability in the data related to the question and accounts for it in the answers.</li> <li>A set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.</li> <li>A measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.</li> </ul> | <ul> <li>Create statistical questions</li> <li>Determine measures of central tendency</li> <li>Choose which measure of central tendency is appropriate for a given set of points</li> <li>Analyze data from a given dot plot, histogram, and box plots</li> <li>Report observations about data using mathematical vocabulary: giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation),</li> </ul> |

| Median                    |  |
|---------------------------|--|
| balance point             |  |
| Mean                      |  |
| measures of variation     |  |
| Range                     |  |
| Quartile                  |  |
| Interquartile range (IQR) |  |
| Box-and-whisker plot      |  |
| Deviation                 |  |
| Absolute Deviation        |  |
| Mean Absolute Deviation   |  |
| misleading data           |  |
| statistical variability   |  |

# Windham School District Curriculum Mathematics - Grade 6 Unit 1: Numbers & Operations Ratios & Proportional Relationships

#### ESTABLISHED GOALS:

Students will continue their study of mathematics in the area of numbers and operations. In this unit, students will explore the concepts and ratios and proportions and how they relate to real-world applications.

#### Content Standards:

- CCSS.6.RP.1. Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities.
- CCSS.6.RP.2 Understand the concept of a unit rate a/b associated with a ratio a:b with b ≠ 0, and use rate language in the context of a ratio relationship.
- CCSS.6.RP.3. Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations.
- CCSS.MP1 Make sense of problems and persevere in solving them.
- CCSS.MP3 Construct viable arguments and critique the reasoning of others.
- CCSS.MP6 Attend to precision.

#### **Stage 1 Desired Results**

#### Students will be able to independently use their learning to...

apply their knowledge of ratios and proportions to real-life applications.

#### Meaning

Transfer

#### ENDURING UNDERSTANDINGS

- A ratio or rate describes the relationship between two quantities.
- Ratio reasoning can be applied to many different types of mathematical and real-life problems
- A rate is a type of ratio that represents a measure or quantity. Therefore the process for solving ratio problems can be applied to rates.

#### **ESSENTIAL QUESTIONS**

- What does 100% represent?
- How can you define a part to whole relationship?
- How can proportions be used for problem solving?
- Can you give an example of a rate in a real world setting?
- What is the difference between a rate and a ratio?

#### Acquisition

#### Students will understand...

- Ratios
- Unit Rates
- Proportions
- Fraction, decimal, percent conversions
- Terminating and repeating decimals
- ratios as a fraction or percentage

- Simplifying ratios
- Comparing ratios in different formats
- Finding equivalent ratios
- Calculating unit rate
- Finding the missing number in a proportion.

| CCSS.MP8 Look for and express regularity in repeated reasoning | <ul> <li>equivalent ratios</li> <li>a rate is a ratio involving units</li> </ul> | • | Converting between fractions, decimals and percents |
|--|--|---|---|
|  | • 100% is all of the original amount   | • | Finding a missing percent                           |
|  | • Numbers can be expressed in different formats                                  | • | Finding the percent of a quantity                   |
|  | based on a given situation.  | • | Solving percent word problems                       |
| Used in Content Area Standards                                 |  |   | 0.454.00  |
| Used in Content  | t Area Standards   |   | 21 <sup>st</sup> Century Skills                     |
| Used in Content  | t Area Standards   | • | Critical Thinking                                   |
| Used in Content  | t Area Standards   | • | •   |
| Used in Content  | t Area Standards   | • | Critical Thinking                                   |

| Stage 2 - Evidence                          |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence     |  |  |
| ASSESSMENT: Written Assessments or Projects |  |  |
|   | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

### Windham School District Curriculum Mathematics - Grade 6

### **Unit 2: Numbers & Operations - Fractions & Decimals**

| = 5 7 | ΓΔ | RI | 15   | ΗF | $D_{i}$ | $G \cap$ | ΔΙ | LS: |  |
|-------|----|----|------|----|---------|----------|----|-----|--|
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Students will continue their study of mathematics in the area of numbers and operations. In this unit, students will master fraction and decimal operations and apply them to real-life applications.

#### Content Standards:

- CCSS.6.NS.1. Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions.
- CCSS.6.NS.2. Fluently divide multi-digit numbers using the standard algorithm.
- CCSS.6.NS.3. Fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.
- CCSS.6.NS.4. Find the greatest common factor of two whole numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12. Use the distributive property to express a sum of two whole numbers 1-100 with a common factor as a multiple of a sum of two whole numbers with no common factor.
- CCSS.MP4 Model with mathematics.
- CCSS.MP5 Use appropriate tools strategically.
- CCSS.MP7 Look for and make use of structure.

#### **Stage 1 Desired Results**

#### Students will be able to independently use their learning to...

• fluently add, subtract, multiply, and divide rational numbers using the standard algorithm with speed and accuracy without the use of math tools (calculator).

Transfer

• apply their knowledge to real-life applications as well as future algebraic topics

#### Meanina

#### ENDURING UNDERSTANDINGS

- Multiplication and division are inverse operations.
- Operations on decimals and whole numbers are based upon place value relationships.
- Number lines are visual models used to represent the density principle: between any two whole numbers are many rational numbers, including decimals and fractions.
- The magnitude of numbers affects the outcome of operations on them.
- Computational fluency includes applying the most effective and efficient strategy when applicable.

#### **ESSENTIAL QUESTIONS**

- Is the product of two numbers always greater than either factor?
- Why is the quotient of two fractions larger than the dividend or divisor?
- What is the relationship between a mixed number and an improper fraction?
- What strategies do you use to find equivalent fractions?
- What is the connection between fractions, decimals, and percents?

#### Acquisition

#### Students will understand:

- Factors
- Multiples
- Place Value
- Reciprocal
- Dividend

- Dividing fractions by fractions
- Dividing decimal numbers
- Adding, subtracting, multiplying and dividing mixed numbers

|                                | <ul> <li>Divisor</li> <li>Quotient</li> <li>the value of a digit in relationship to its position in a number</li> </ul> | <ul> <li>Simplifying numerical expressions using the order of operations.</li> <li>Finding common factors, greatest common factors, and multiples, least common multiple</li> </ul> |
|--------------------------------|---|---|
| Used in Content Area Standards |   | 21st Century Skills   |
|                                |   | Critical Thinking   |
|                                |   | Communication   |
|                                |   | Collaboration   |

| Stage 2 - Evidence                          |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence     |  |  |
| ASSESSMENT: Written Assessments or Projects |  |  |
|   | Other Evidence: independent practice, classroom observations and discussions |  |

## Windham School District Curriculum Mathematics - Grade 6 Unit 3: Numbers & Operations - Integers

| FST   | ΔRI | ISE   | 1FD | GO   | ALS:  |
|-------|-----|-------|-----|------|-------|
| L.) I | ADI | _1. ) | யப  | (1() | AL.). |

Students will continue their study of mathematics in the area of numbers and operations. In this unit, students will understand rational numbers with an emphasis on integers.

#### Content Standards:

- CCSS.6.NS.5. Understand that positive and negative numbers are used together to describe quantities having opposite directions or values; use positive and negative numbers to represent quantities in real-world contexts, explaining the meaning of 0 in each situation.
- CCSS.6.NS.6. Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates.
- CCSS.6.NS.7. Understand ordering and absolute value of rational numbers.
- CCSS.6.NS.8. Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate plane. Include use of coordinates and absolute

#### Stage 1 Desired Results

#### Students will be able to independently use their learning to...

- explain the necessity for both positive and negative numbers.
- understand the importance of the sign and direction of a number in real world applications.
- discuss the real world significance of an ordered pair as a location on a coordinate plane.

#### Meaning

Transfer

#### **ENDURING UNDERSTANDINGS**

- Positive and negative numbers are used together to describe quantities having opposite directions or values
- All rational numbers can be represented as a point on the number line.
- Students will understand that absolute value is the distance from zero on a number line.
- The coordinate plane can be used to describe location in two dimensions, defined by an ordered pair.

#### **ESSENTIAL QUESTIONS**

- How can a number line be used to determine size and direction of a number?
- What is the value in distinguishing between positive and negative numbers?
- How is the coordinate plane configured?
- What are some situations in everyday life where you use negative as well as positive numbers?

#### **Acquisition**

#### Students will understand ...

- Integers
- Rational Number
- Absolute Value
- Opposite
- Number Line
- Coordinate Plane
- X Axis
- Y Axis

- Creating a number line with integers
- Determining the absolute value, direction, and opposite of a given integer
- Writing a number sentence which reflects the actions and changes in real world situations
- Graphing with positive and negative coordinates on a coordinate grid

| <ul> <li>value to find distance between points with the same first coordinate or the same second coordinate.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul> | <ul> <li>Reflection</li> <li>Horizontal</li> <li>Vertical</li> <li>absolute value as the distance away from zero on a number line</li> </ul> |                                   |
|--|--|-----------------------------------|
| Used in Content Area Standards   |  | 21 <sup>st</sup> Century Skills   |
|  |  | Critical Thinking                 |
|  |  | <ul> <li>Communication</li> </ul> |
|  |  | <ul> <li>Collaboration</li> </ul> |

| Stage 2 - Evidence                      |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence |  |  |
|   | ASSESSMENT: Written Assessments or Projects                                  |  |
|   | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

### **Windham School District Curriculum Mathematics - Grade 6 Unit 4: Algebraic Thinking - Expressions**

|  | Stage 1 Desired Results   |  |
|--|---|--|
| ESTABLISHED GOALS:   | Tro   | ansfer   |
| Students will continue their study of mathematics in                   | Students will be able to independently use their le                 | arning to  |
| the area of Algebraic Thinking. In this unit, students                 | <ul> <li>write algebraic expressions to solve real world</li> </ul> | problems   |
| will create, simplify, and evaluate expressions.                       | <ul> <li>use their knowledge of algebraic expressions a</li> </ul>  | s they solve algebraic equations                                 |
|  | Me  | eaning   |
| Content Standards:   | ENDURING UNDERSTANDINGS   | ESSENTIAL QUESTIONS  |
| CCSS.6.EE.1 Write and evaluate numerical                               | <ul> <li>Expressions are powerful tools for exploring,</li> </ul>   | • What is meant by an "algebraic expression"?                    |
| expressions involving whole-number exponents.                          | reasoning about, and representing situations.                       | How can algebraic expressions be used to                         |
| <ul> <li>CCSS.6.EE.2. Write, read, and evaluate</li> </ul>             | <ul> <li>Variables have many different meanings,</li> </ul>         | represent real-life situations?                                  |
| expressions in which letters stand for numbers.                        | depending on context and purpose.                                   | <ul> <li>How is a variable used in the real world?</li> </ul>    |
| <ul> <li>CCSS.6.EE.3. Apply the properties of operations to</li> </ul> |   | Why do we need an order of operations?                           |
| generate equivalent expressions.                                       | values are unknown or vary under different                          | Why is algebraic reasoning important?                            |
| • CCSS.6.EE.4. Identify when two expressions are                       | circumstances.  | , sugar a sea grant  |
| equivalent (i.e., when the two expressions name                        | <ul> <li>Two or more expressions may be equivalent,</li> </ul>      |  |
| the same number regardless of which value is                           | even when their symbolic forms differ.                              |  |
| substituted into them).  | <ul> <li>Linear expressions may be added to or</li> </ul>           |  |
| • CCSS.6.EE.6. Use variables to represent numbers                      | subtracted from one another.  |  |
| and write expressions when solving a real-world o                      | r   |  |
| mathematical problem; understand that a variable                       | Acqu  | uisition   |
| can represent an unknown number, or, depending                         |   | Students will be skilled at                                      |
| on the purpose at hand, any number in a specified                      |   | <ul> <li>simplifying algebraic expressions with whole</li> </ul> |
| set.   | • Exponents   | numbers.   |
| <ul> <li>CCSS.MP1 Make sense of problems and persevere</li> </ul>      |   | <ul> <li>creating algebraic expressions from verbal,</li> </ul>  |
| in solving them.   | Coefficient   | written and interpretational expressions                         |
| CCSS.MP3 Construct viable arguments and critique                       |   | <ul> <li>applying and extending previous</li> </ul>              |
| the reasoning of others.   | Like Terms  | understandings of arithmetic to algebraic                        |
| <ul> <li>CCSS.MP7 Look for and make use of structure.</li> </ul>       | Variable  | expressions, including whole number                              |

|                                | Distributive Property | exponents           |
|--------------------------------|-----------------------|---------------------|
| Used in Content Area Standards |                       | 21st Century Skills |
|                                |                       | Collaboration       |
|                                |                       | Critical Thinking   |
|                                |                       | Communication       |

| Stage 2 - Evidence                      |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence |  |  |
|   | ASSESSMENT: Written Assessments or Projects                                  |  |
|   | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

## Windham School District Curriculum Mathematics - Grade 6 Unit 5: Algebraic Thinking - Equations

| FST | ΔRΙ | ISHE | ED G | OALS | ζ. |
|-----|-----|------|------|------|----|
|     |     |      |      |      |    |

Students will continue their study of mathematics in the area of Algebraic Thinking. In this unit, students will create and solve one-step questions. They will also use this knowledge in real-life applications.

#### Content Standards:

- CCSS.6.EE.3. Apply the properties of operations to generate equivalent expressions.
- CCSS.6.EE.5. Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true.
- CCSS.6.EE.7. Solve real-world and mathematical problems by writing and solving equations of the form x + P = q and px = q for cases in which p, q and x are all nonnegative rational numbers.
- CCSS.6.EE.8. Write an inequality of the form x > c or x < c have infinitely many solutions; represent solutions of such inequalities on number line diagrams.
- CCSS.6.EE.9. Use variable to represent two quantities in a real-world problem that change in relationship to one another; write an equation to

#### **Stage 1 Desired Results**

#### Students will be able to independently use their learning to...

use their knowledge of equation writing and solving as a technique for solving problems.

#### Meaning

Transfer

#### ENDURING UNDERSTANDINGS

- Solving an equation is a process of answering a question by finding the value of the variable that makes the equation true.
- An equation is two equivalent expressions.
- Variables are used to represent two quantities in a real world problem that change in relationship to one another.

#### ESSENTIAL QUESTIONS

- Why do we use inverse operations to solve algebraic equations?
- What is a variable in the real world?
- How is algebra used in the world we live in every day?
- What does it mean to be unequal?

#### Acquisition

#### Students will understand...

- how to solve one-step algebraic equations and inequalities.
- the difference between dependent and independent variables.

- Writing an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable.
- Writing an equation from data tables and graphs
- Defining a variable and create an equation and / or an inequality from a word problem
- Solving one step equations and inequalities

|  | <ul> <li>Collaboration</li> <li>Critical Thinking</li> <li>Communication</li> </ul> |
|--|---|
| Used in Content Area Standards                       | 21st Century Skills   |
| CCSS.MP7 Look for and make use of structure.         |   |
| the reasoning of others.                             |   |
| CCSS.MP3 Construct viable arguments and critique     |   |
| in solving them.                                     |   |
| CCSS.MP1 Make sense of problems and persevere        |   |
| and relate these to the equation.                    |   |
| independent variables using graphs and tables,       |   |
| relationship between the dependent and               |   |
| as the independent variable. Analyze the             |   |
| variable, in terms of the other quantity, thought of |   |
| express one quantity, thought of as the dependent    |   |

| Stage 2 - Evidence                      |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence |  |  |
|   | ASSESSMENT: Written Assessments or Projects                                  |  |
|   | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

### Windham School District Curriculum Mathematics - Grade 6

### Unit 6: Geometry & Data - Area & Surface Area

|  | Stage 1 Desired Results   |  |
|--|---|--|
| ESTABLISHED GOALS:                                   | Transfer  |  |
| Students will continue their study of mathematics    | Students will be able to independently use their learning to              |  |
| in the area of Geometry. In this unit, students will | <ul> <li>find the surface area of any solid.</li> </ul>                   |  |
| continue their understanding of area, surface        | <ul> <li>apply area formulas when solving real life scenarios.</li> </ul> |  |
| area.  | Meaning   |  |
|  | ENDURING UNDERSTANDINGS   | ESSENTIAL QUESTIONS  |
| Content Standards:                                   | • The area of all 2-dimensional figures can be calculated by              | <ul> <li>How is geometry part of the world?</li> </ul>       |
| • CCSS.6.G.1. Find the area of right triangles,      | breaking irregular shapes into rectangles or triangles.                   | How can proportional reasoning help you                      |
| other triangles, special quadrilaterals, and         | • A three-dimensional figure can be represented by two-                   | find the length of a corresponding side of a                 |
| polygons by composing into rectangles or             | dimensional nets, which can help determine the surface                    | similar figure?  |
| decomposing into triangles and other                 | area of three-dimensional figures.  | Why are there different formulas to find                     |
| shapes; apply these techniques in the                |   | the area of different polygons?                              |
| context of solving real-world and                    |   | How can the use of a coordinate plane aid                    |
| mathematical problems.                               |   | in finding the area, lengths, and widths of a                |
| • CCSS.6.G.3. Draw polygons in the coordinate        |   | polygon?   |
| plane given coordinates for the vertices; use        |   | How can a net make it easier to find the                     |
| coordinates to find the length of a side             |   | surface area of a 3-dimensional object?                      |
| joining points with the same first coordinate        |   | How can nets be used to find surface area                    |
| or the same second coordinate. Apply these           |   | on irregular polygons?                                       |
| techniques in the context of solving real-           | Acquisition   |  |
|  | Students will understand  | Students will be skilled at                                  |
| CCSS.6.G.4. Represent three-dimensional              | • Length  | <ul> <li>calculating the area of irregular shapes</li> </ul> |
| figures using nets made up of rectangles and         | • Width   | (composite figures).   |
| triangles, and use the nets to find the surface      | - raranciogram  | <ul> <li>drawing a net for a given solid.</li> </ul>         |
| area of these figures. Apply these techniques        | Altitude  | <ul> <li>identifying faces, edges and vertices.</li> </ul>   |
| in the context of solving real-world and             | Trapezoid   |  |

| mathematical problems.                      | Area as space inside a figure   | calculating surface area of rectangular     |
|---|---|---|
| CCSS.MP1 Make sense of problems and         | <ul> <li>Area of a parallelogram A = bh</li> </ul>                    | prisms.                                     |
| persevere in solving them.                  | <ul> <li>Area of a triangle A = ½ bh</li> </ul>                       | Calculating area and surface area using     |
| CCSS.MP6 Attend to precision.               | <ul> <li>Area of a trapezoid A = ½ (b1 + b2)h</li> </ul>              | models                                      |
| CCSS.MP8 Look for and express regularity in | <ul> <li>Units squared</li> </ul>                                     | Fluently, calculating area and surface area |
| repeated reasoning.                         | • Net   | using formulas                              |
|   | Surface Area  | Calculating surface area of rectangular     |
|   | • Area  | prisms                                      |
|   | Composite Figures   |   |
|   | • Kite  |   |
|   | • Compose   |   |
|   | <ul> <li>decompose</li> </ul>   |   |
|   | <ul><li>irregular shapes</li></ul>                                    |   |
|   | <ul> <li>Two-dimensional figures</li> </ul>                           |   |
|   | <ul> <li>three-dimensional figures</li> </ul>                         |   |
|   | <ul> <li>faces, edges, vertices.</li> </ul>                           |   |
|   | • Solid   |   |
|   | • prism   |   |
|   | <ul> <li>lateral surface area</li> </ul>                              |   |
|   | <ul> <li>area is the surface inside a flat, closed figure.</li> </ul> |   |
|   | • irregular shapes are the combination of multiple figures.           |   |
|   | • nets are three-dimensional figures drawn on a surface.              |   |
|   | • surface area is the sum of the areas of all faces.                  |   |
| Used in Content Area Standards              |   | 21 <sup>st</sup> Century Skills             |
|   |   | Collaboration                               |
|   |   | Critical Thinking                           |
|   |   | Communication                               |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

### Windham School District Curriculum Mathematics - Grade 6 Unit 7: Geometry & Data - Volume

| Stage 1 Desired Results   |  |   |  |  |
|---|--|---|--|--|
| ESTABLISHED GOALS:  |  | Transfer                                      |  |  |
| Students will continue their study of mathematics in the area of      | Students will be able to independently use their learning to |   |  |  |
| Geometry. In this unit, students will continue their understanding of | <ul> <li>apply volume formulas in the cont</li> </ul>        | text of solving real-world problems           |  |  |
| volume.   | <ul> <li>explain the difference between su</li> </ul>        | urface area and volume of objects.            |  |  |
|   |  | Meaning                                       |  |  |
| Content Standards:  | ENDURING UNDERSTANDINGS                                      | ESSENTIAL QUESTIONS                           |  |  |
| CCSS.6.G.2. Find the volume of a right rectangular prism with         | <ul> <li>Volume is the number of cubes</li> </ul>            | What does volume mean?                        |  |  |
| fractional edge lengths by packing it with unit cubes of the          | that can fit inside of a solid.                              | How can the volume of a triangular prism be   |  |  |
| appropriate unit fraction edge lengths, and show that the volume      | The generic formula for volume is                            | found by placing unit cubes inside it?        |  |  |
| is the same as would be found by multiplying the edge lengths of      | the area of the base multiplied by                           | 1   |  |  |
| the prism. Apply the formulas V = I w h and V = b h to find volumes   | the height.  |   |  |  |
| of right rectangular prisms with fractional edge lengths in the       | Acquisition  |   |  |  |
| context of solving real-world and mathematical problems.              | Students will understand                                     | Students will be skilled at                   |  |  |
| • CCSS.MP1 Make sense of problems and persevere in solving them.      | Polygon  | Finding volume by packing it with unit cubes  |  |  |
| CCSS.MP6 Attend to precision.   | Polyhedron   | of the appropriate unit fraction edge lengths |  |  |
| CCSS.MP8 Look for and express regularity in repeated reasoning        | Edge   | (modeling)                                    |  |  |
|   | Vertex   | Calculating volume using models               |  |  |
|   | Length   | Fluently calculating volume using formulas    |  |  |
|   | Width  | Solving real word problems involving volume   |  |  |
|   | Depth  |   |  |  |
|   | Cubic Units  |   |  |  |
|   | Formula: V=LWH or V=Bh                                       |   |  |  |
|   | Irregular Figures  |   |  |  |
|   | Prism  |   |  |  |
|   | <ul> <li>volume as the space inside a</li> </ul>             |   |  |  |
|   | solid.   |   |  |  |

| Used in Content Area Standards | 21 <sup>st</sup> Century Skills |
|--------------------------------|---------------------------------|
|                                | Collaboration                   |
|                                | Critical Thinking               |
|                                | Communication                   |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

## Windham School District Curriculum Mathematics - Grade 6 Unit 8: Geometry & Data - Statistics & Probability

| FST | ΔRI | <b>ISHFD</b> | GOA | ıς٠ |
|-----|-----|--------------|-----|-----|
|     |     |              |     |     |

Students will continue their study of mathematics in the area of Data. In this unit, students will continue their understanding of data analysis and statistical graphs.

#### Content Standards:

- CCSS.6.SP.1. Recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. CCSS.6.SP.2. Understand that a set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.
- CCSS.6.SP.3. Recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.
- CCSS.6.SP.4. Display numerical data in plots on a number line, including dot plots, histograms, and box plots.
- CCSS.6.SP.5. Summarize numerical data sets in relation to their context, such as by:
- CCSS.6.SP.5. a. Reporting the number observations.

#### Stage 1 Desired Results

#### Transfer

#### Students will be able to independently use their learning to...

- analyze graphs found in multiple sources
- describe data using graphs and measures of central tendency.

#### Meaning

#### ENDURING UNDERSTANDINGS

- A statistical question anticipates variability in the data related to the question and accounts for it in the answers.
- A set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.
- A measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.

#### ESSENTIAL QUESTIONS

- How are statistics used to collect, analyze, and draw conclusions in today's society?
- Why are statistics important in the world?
- What are the ways that data can be represented visually?
- Why is it better to use different graphs and diagrams to understand data?
- What are the different ways in which we can summarize data sets?

#### **Acquisition**

#### Students will understand...

- Variability
- Data
- statistical questioning
- statistical process
- Sample
- bar graph
- Frequency

- Determining measures of central tendency and variation
- Choosing which measure of central tendency is appropriate for a given set of points
- Analyzing data from a given dot plot, histogram, and box plots
- Reporting observations about data using

| <ul> <li>CCSS.6.SP.5. b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.</li> <li>CCSS.6.SP.5. c. Giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.</li> <li>CCSS.6.SP.5. d. Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision</li> </ul> | <ul> <li>Mode</li> <li>dot plot</li> <li>Distribution</li> <li>Symmetric</li> <li>Outliers</li> <li>Histogram</li> <li>Measure of center</li> <li>Median</li> <li>balance point</li> <li>Mean</li> <li>measures of variation</li> <li>Range</li> <li>Quartile</li> <li>Interquartile range (IQR)</li> <li>Box-and-whisker plot</li> <li>Deviation</li> <li>Absolute Deviation</li> <li>Mean Absolute Deviation</li> <li>misleading data</li> <li>statistical variability</li> <li>line plots</li> <li>scatter plots</li> </ul> | mathematical vocabulary: giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation). |
|---|--|--|
| Used in Content Area Standards  |  | 21st Century Skills  |
|   |  | Communication  |
|   |  | Critical Thinking  |
|   |  | Perseverance   |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

<u>Title of Curriculum:</u> 6th Grade Accelerated Math

| Unit Name  | What (content, vocab)   | Why (enduring understandings)  | How (skills)   |
|--|---|--|--|
| Unit 1: Number and Operations: Ratios and Proportional Relationships | <ul> <li>Ratios</li> <li>Unit Rates</li> <li>Proportions</li> <li>Fraction, decimal, percent conversions</li> <li>Terminating and repeating decimals</li> <li>ratios as a fraction or percentage</li> <li>equivalent ratios</li> <li>a rate is a ratio involving units</li> <li>100% is all of the original amount</li> </ul> | <ul> <li>A ratio or rate describes the relationship between two quantities.</li> <li>Ratio reasoning can be applied to many different types of mathematical and real-life problems</li> <li>A rate is a type of ratio that represents a measure or quantity. Therefore the process for solving ratio problems can be applied to rates.</li> </ul>  | <ul> <li>Simplify ratios</li> <li>Compare ratios in different formats</li> <li>Find equivalent ratios</li> <li>Calculate unit rate</li> <li>Find a missing number in a proportion</li> <li>Convert between fractions, decimals and percents</li> <li>Find a missing percent</li> <li>Find percent of a quantity.</li> <li>Solve percent real world problems</li> </ul> |
| Unit 2: Number and Operations: Fractions and Decimals                | <ul> <li>Factors</li> <li>Multiples</li> <li>Place Value</li> <li>Reciprocal</li> <li>Dividend</li> <li>Divisor</li> <li>Quotient</li> <li>the value of a digit in relationship to its position in a number</li> <li>Positive exponents</li> </ul>  | <ul> <li>Multiplication and division are inverse operations.</li> <li>Operations on decimals and whole numbers are based upon place value relationships.</li> <li>Number lines are visual models used to represent the density principle: between any two whole numbers are many rational numbers, including decimals and fractions.</li> <li>The magnitude of numbers affects the outcome of operations on them.</li> <li>Computational fluency includes applying the most effective and efficient strategy when applicable.</li> </ul> | <ul> <li>Divide fractions by fractions</li> <li>Find common factors, greatest common factors, and multiples, least common multiple</li> <li>Add, subtract, multiply and divide mixed numbers</li> <li>Divide decimals</li> <li>Simplify numerical expressions using the order of operations</li> </ul>   |
| Unit 3: Numbers and<br>Operations: Integers                          | <ul><li>Integers</li><li>Rational Numbers</li></ul>   | Positive and negative numbers are used together to describe  | Create a number line with integers   |

|   | <ul> <li>Absolute Value</li> <li>Coordinate Grid</li> <li>Opposite</li> <li>Number Line</li> <li>Coordinate Plane</li> </ul>   | <ul> <li>quantities having opposite directions(number line) or values</li> <li>All rational numbers can be represented as a point on a</li> <li>Understand the relationship between a positive or negative number and its opposite</li> <li>Determine the absolute value, direction of number line movement,</li> </ul>   |
|---|--|---|
|   | <ul> <li>X Axis</li> <li>Y Axis</li> <li>Reflection</li> <li>Horizontal</li> <li>Vertical</li> </ul>   | <ul> <li>unmber line</li> <li>Understand that absolute value is the distance from zero on a number line</li> <li>The coordinate plane can be used to describe a location in two dimensions, defined by an ordered pair</li> <li>Ordering and absolute value of rations numbers</li> <li>Write a number sentence which reflects the actions and changes in real world situations</li> <li>Graph with positive and negative coordinates on a coordinate grid</li> <li>Add, subtract, multiply and divide integers</li> </ul>  |
| Unit 4:<br>Algebraic Thinking:<br>Expressions | <ul> <li>Algebraic expressions</li> <li>Exponents</li> <li>Constant</li> <li>Coefficient</li> <li>Term</li> <li>Like Terms</li> <li>Variable</li> <li>Distributive Property</li> <li>Integer</li> <li>Rational number</li> </ul> | <ul> <li>Expressions are powerful tools for exploring, reasoning about, and representing situations.</li> <li>Variables have many different meanings, depending on context and purpose.</li> <li>Variables permit writing expressions whose values are unknown or vary under different circumstances.</li> <li>Two or more expressions may be equivalent, even when their symbolic forms differ.</li> <li>Linear expressions may be added to or subtracted from one another.</li> <li>simplify algebraic expressions with whole numbers.</li> <li>create algebraic expressions from verbal, written and interpretational expressions understandings of arithmetic to algebraic expressions, including whole number exponents</li> </ul> |

| Unit 5:<br>Algebraic Thinking: Equations            | <ul> <li>multi-step algebraic equations and inequalities</li> <li>dependent and independent variables.</li> <li>Integers</li> <li>Like terms</li> <li>Rational numbers</li> <li>like terms</li> <li>equivalent expressions</li> </ul>   | <ul> <li>Solving an equation is a process of answering a question by finding the value of the variable that makes the equation true.</li> <li>An equation is two equivalent expressions.</li> <li>Variables are used to represent two quantities in a real world problem that change in relationship to one another.</li> </ul> | <ul> <li>Write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable.</li> <li>Write an equation from data tables and graphs</li> <li>Define a variable and create an equation and / or an inequality from a word problem</li> <li>Solve multi step equations and inequalities</li> </ul> |
|---|---|---|---|
| Unit 6: Geometry and Data:<br>Area and Surface Area | <ul> <li>Length</li> <li>Width</li> <li>Parallelogram</li> <li>Altitude</li> <li>Trapezoid</li> <li>Area as space inside a figure</li> <li>Area of a parallelogram A = bh</li> <li>Area of a triangle A = ½ bh</li> <li>Area of a trapezoid A = ½ (b1 + b2)h</li> <li>Units squared</li> <li>Net</li> <li>Surface Area</li> <li>Composite (irregular) Figures</li> <li>Kite</li> <li>irregular shapes</li> <li>Two-dimensional figures</li> <li>three-dimensional figures</li> <li>faces, edges, vertices.</li> <li>Solid</li> <li>prism</li> <li>lateral surface area</li> </ul> | <ul> <li>The area of all 2-dimensional figures can be calculated by breaking irregular shapes into rectangles or triangles.</li> <li>A three-dimensional figure can be represented by two-dimensional nets, which can help determine the surface area of three-dimensional figures.</li> </ul>                                  | <ul> <li>calculating the area of irregular shapes (composite figures).</li> <li>drawing a net for a given solid.</li> <li>identifying faces, edges and vertices.</li> <li>calculating surface area of rectangular prisms.</li> <li>Calculating area and surface area</li> </ul>   |

| Unit 7: Geometry and Data:<br>Triangles                  | <ul> <li>Radius</li> <li>Circumference</li> <li>Diameter</li> <li>Pi</li> <li>180 degrees in every triangle.</li> <li>classifications of triangles for both sides and angles: acute, obtuse, right, scalene, isosceles, equilateral</li> <li>supplementary, complementary, vertical, and adjacent angles</li> <li>Angle pair relationships: adjacent, vertical, complementary, supplementary, linear pair</li> </ul> | <ul> <li>differences between geometrical figures.</li> <li>Analyzing geometric relationships develops reasoning and justification skills.</li> </ul>  | <ul> <li>and/or angles</li> <li>Determine the missing angles in triangles</li> <li>Classify triangles by their sides and angles</li> <li>Identify values of angles in complementary and supplementary relationships</li> <li>Use vertical, complementary, and supplementary angle relationships to find missing angles</li> </ul>  |
|--|--|---|--|
| Unit 8: Geometry and Data:                               | Polygon  | Area, surface area and volume   | <ul> <li>Solve for unknown angles using equations</li> <li>Calculate volume using models</li> </ul>  |
| Volume   | <ul> <li>Polyhedron</li> <li>Edge</li> <li>Vertex</li> <li>Length</li> <li>Width</li> <li>Depth</li> <li>Cubic Units</li> <li>Formula: V=LWH or V=Bh</li> <li>Irregular Figures</li> <li>Prism</li> <li>volume as the space inside a solid.</li> </ul>   | <ul> <li>have applications in real world situations.</li> <li>Dimension is a measure of the width, height, or length of a figure.</li> <li>Different 3-dimensional figures can have the same volume even if the dimensions are not all the same.</li> </ul> | <ul> <li>Fluently calculate volume using formulas</li> <li>Apply the formulas for volume of three- dimensional figures</li> <li>Differentiate between volume and the surface area to solve problem for three-dimensional figures</li> <li>Calculate and explain how to find the area, volume, and surface area for two- and three- dimensional objects from real-world situations</li> </ul> |
| Unit 9: Geometry and Data:<br>Statistics and Probability | <ul> <li>Data</li> <li>statistical questioning</li> <li>Sample</li> <li>bar graph, histogram</li> </ul>  | <ul> <li>A statistical question anticipates<br/>variability in the data related to<br/>the question and accounts for it<br/>in the answers.</li> </ul>  | Determine measures of central tendency   |

- Frequency
- dot plots, line plots, scatter plots
- Distribution
- Symmetric
- Outliers
- Measure of center: Median, Mean Mode
- balance point
- measures of variation: range, quartile, interquartile range (IQR), absolute deviation, mean absolute deviation
- Box-and-whisker plot
- misleading data
- statistical variability

- A set of data collected to answer

   a statistical question has a
   distribution, which can be
   described by its center, spread,
   and overall shape.
- A measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.
- Choose which measure of central tendency is most appropriate for a given set of points
- Analyze data from given dot plots, histograms and box plots
- Report observations about data using mathematical vocabulary
- Make predictions from graphs
- Summarize and describe distributions using both measures of central tendency as well as variation data

# Windham School District Curriculum Accelerated Math - Grade 6 Unit 1: Number & Operations Ratios & Proportional Relationships

| ESTABLISHED GOALS: |
|--------------------|
|--------------------|

Students will continue their study of mathematics in the area of numbers and operations. In this unit, students will explore the concepts and ratios and proportions and how they relate to real-world applications.

#### Content Standards:

- CCSS.6.RP.1. Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities.
- CCSS.6.RP.2 Understand the concept of a unit rate a/b associated with a ratio a:b with b ≠ 0, and use rate language in the context of a ratio relationship.
- CCSS.6.RP.3. Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations.
- CCSS.MP1 Make sense of problems and persevere in solving them.
- CCSS.MP3 Construct viable arguments and critique the reasoning of others.

#### Stage 1 Desired Results

#### Students will be able to independently use their learning to...

• apply their knowledge of ratios and proportions to real-life applications.

#### Meaning

Transfer

#### ENDURING UNDERSTANDINGS

- A ratio or rate describes the relationship between two quantities.
- Ratio reasoning can be applied to many different types of mathematical and real-life problems
- A rate is a type of ratio that represents a measure or quantity. Therefore the process for solving ratio problems can be applied to rates.

#### **ESSENTIAL QUESTIONS**

- What does 100% represent?
- How can you define a part to whole relationship?
- How can proportions be used for problem solving?
- Can you give an example of a rate in a real world setting?
- What is the difference between a rate and a ratio?

#### Acquisition

#### Students will understand...

- ratios
- unit rates
- proportions
- Fraction, decimals percent connections
- Terminating and repeating decimals
- Ratio as a fraction or percentage
- Equivalent ratios
- A rate is a ratio involving units

- Simplifying ratios
- Comparing ratios in different formats
- Finding equivalent ratios
- Calculating unit rate
- Finding the missing number in a proportion.
- Conversions between fractions, decimals and percents
- Finding a missing percent

| <ul> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning</li> </ul> | <ul> <li>100% is all of the original amount</li> <li>Numbers can be expressed in different formats based on a given situation</li> </ul> | <ul><li>Finding the percent of a quantity</li><li>Solving percent word problems</li></ul> |
|---|--|---|
| Used in Content Area Standards  |  | 21st Century Skills   |
|   |  | Critical Thinking   |
|   |  | Collaboration   |
|   |  | Communication   |
|   |  |   |

| Stage 2 - Evidence   |   |  |
|--|---|--|
| Evaluative Criteria Assessment Evidence                                      |   |  |
|  | ASSESSMENT: Written Assessments or Projects |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |   |  |

## Windham School District Curriculum Accelerated Math - Grade 6 Unit 2: Number & Operations - Fractions & Decimals

|   | Stage 1 Desired Results  |  |  |
|---|--|--|--|
| ESTABLISHED GOALS:  | Trai   | nsfer  |  |
| Students will continue their study of mathematics in              | Students will be able to independently use their lea                               | rning to   |  |
| the area of numbers and operations. In this unit,                 | <ul> <li>fluently perform all operations on positive ratio</li> </ul>              | nal numbers with speed and accuracy without the                      |  |
| students will master fraction and decimal operations              | use of math tools (calculator)   |  |  |
| and apply them to real-life applications.                         | apply this knowledge to real-life applications as well as future algebraic topics. |  |  |
|   | Med  | ning   |  |
| Content Standards:  | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS  |  |
| CCSS.6.NS.1. Interpret and compute quotients of                   | <ul> <li>Multiplication and division are inverse</li> </ul>                        | <ul> <li>Is the product of two numbers always greater</li> </ul>     |  |
| fractions, and solve word problems involving                      | operations.  | than either factor?  |  |
| division of fractions by fractions.                               | <ul> <li>Operations on decimals and whole numbers</li> </ul>                       | <ul> <li>Why is the quotient of two fractions larger than</li> </ul> |  |
| CCSS.6.NS.2. Fluently divide multi-digit numbers                  | are based on place value relationships.  | the dividend or divisor?   |  |
| using the standard algorithm.                                     | <ul> <li>Number lines are visual models used to</li> </ul>                         | What is the relationship between a mixed                             |  |
| • CCSS.6.NS.3. Fluently add, subtract, multiply, and              | represent the density principle: between any                                       | number and an improper fraction?                                     |  |
| divide multi-digit decimals using the standard                    | two whole numbers are many rational  | What strategies do you use to find equivalent                        |  |
| algorithm for each operation.                                     | numbers, including decimals and fractions.   | fractions?   |  |
| CCSS.6.NS.4. Find the greatest common factor of                   | <ul> <li>The magnitude of numbers affects the outcome</li> </ul>                   | <ul> <li>What is the connection between fractions,</li> </ul>        |  |
| two whole numbers less than or equal to 100 and                   | of operations on them.   | decimals, and percents?  |  |
| the least common multiple of two whole numbers                    | <ul> <li>Computational fluency includes applying the</li> </ul>                    |  |  |
| less than or equal to 12. Use the distributive                    | most effective and efficient strategy when   |  |  |
| property to express a sum of two whole numbers                    | applicable.  |  |  |
| 1-100 with a common factor as a multiple of a sum                 | Acqu   | isition  |  |
| of two whole numbers with no common factor.                       | Students will understand   | Students will be skilled at  |  |
| <ul> <li>CCSS.MP4 Model with mathematics.</li> </ul>              | Factors  | Dividing fractions by fractions                                      |  |
| <ul> <li>CCSS.MP5 Use appropriate tools strategically.</li> </ul> | Multiples  | Dividing decimal numbers   |  |
| CCSS.MP7 Look for and make use of structure.                      | Place value  | Adding, subtracting, multiplying and dividing                        |  |

Reciprocal

mixed numbers

|                                | <ul> <li>Dividend</li> <li>Divisor</li> <li>quotient</li> <li>the value of a digit in relationship to its position in a number</li> <li>positive exponents</li> </ul> | •                   | Simplifying numerical expressions using the order of operations. Finding common factors, greatest common factors, and multiples, least common multiple |
|--------------------------------|---|---------------------|--|
| Used in Content Area Standards |   | 21st Century Skills |  |
|                                |   | •                   | Critical Thinking Communication Collaboration  |

| Stage 2 - Evidence   |   |  |
|--|---|--|
| Evaluative Criteria Assessment Evidence                                      |   |  |
|  | ASSESSMENT: Written Assessments or Projects |  |
| Other Evidence: independent practice, classroom observations and discussions |   |  |

## Windham School District Curriculum Accelerated Math - Grade 6 Unit 3: Number & Operations - Integers

| ΞςτΔ | RH | SHFD | GOA | ۱ <b>ς</b> ٠ |
|------|----|------|-----|--------------|

Students will continue their study of mathematics in the area of numbers and operations. In this unit, students will understand rational numbers with an emphasis on integers.

#### Content Standards:

- CCSS.6.NS.5. Understand that positive and negative numbers are used together to describe quantities having opposite directions or values; use positive and negative numbers to represent quantities in real-world contexts, explaining the meaning of 0 in each situation.
- CCSS.6.NS.6. Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates.
- CCSS.6.NS.7. Understand ordering and absolute value of rational numbers.
- CCSS.6.NS.8. Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate

#### **Stage 1 Desired Results**

#### Students will be able to independently use their learning to...

- explain the necessity for both positive and negative numbers.
- understand the significance of a number having both a sign and direction.
- Discuss the real world significance of an ordered pair as a location on a coordinate plane (for example: on a map)

Transfer

Fluently perform operations on integers

#### ENDURING UNDERSTANDINGS

- Positive and negative numbers are used together to describe quantities having opposite directions with the same values
- All rational numbers can be represented as a point on the number line.
- Absolute value is the distance from zero on a number line.
- The coordinate plane can be used to describe location in two dimensions, defined by an ordered pair.

### Meaning ESSENTIAL QUESTIONS

- How can a number line be used to determine size and direction of a number?
- What is the value in distinguishing between positive and negative numbers?
- How is the coordinate plane configured?
- What are some situations in everyday life where you use negative as well as positive numbers?

#### Acquisition

#### Students will understand ...

- Integers
- Rational number
- Absolute value
- Opposite
- Number line

- Creating a number line with integers
- Understanding the relationship between a positive or negative number and its opposite
- Determining the absolute value, direction, and opposite of a given integer

| <ul> <li>plane. Include use of coordinates and absolute value to find distance between points with the same first coordinate or the same second co</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP7 Look for and make use of structure.ordinate.</li> </ul> | <ul> <li>Coordinate plane</li> <li>x-axis</li> <li>y-axis</li> <li>Reflection</li> <li>Horizontal</li> <li>vertical</li> <li>absolute value as the distance away from zero on a number line</li> </ul> | <ul> <li>Writing a number sentence which reflects the actions and changes in real world situations</li> <li>Graphing with positive and negative coordinates on a coordinate grid</li> <li>Add, subtract, multiply and divide integers</li> </ul> |
|---|--|--|
| Used in Content Area Standards  | Used in Content Area Standards   |  |
|   |  | Critical Thinking  |
|   |  | Communication  |
|   |  | Collaboration  |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |

## Windham School District Curriculum Accelerated Math - Grade 6 Unit 4: Algebraic Thinking - Expressions

| Stage 1 Desired Results  |  |  |  |
|--|--|--|--|
| ESTABLISHED GOALS:   | Transfer   |  |  |
|  | Students will be able to independently use their lea   | arning to  |  |
| Students will continue their study of mathematics in the   | <ul> <li>write algebraic expressions to solve real world  </li> </ul>  | problems   |  |
| area of Algebraic Thinking. In this unit, students will  | <ul> <li>use their knowledge of algebraic expressions as</li> </ul>  | s they solve algebraic equations   |  |
| create, simplify, and evaluate expressions.  | Med  | aning  |  |
| <ul> <li>Content Standards:         <ul> <li>CCSS.6.EE.1 Write and evaluate numerical expressions involving whole-number exponents.</li> <li>CCSS.6.EE.2. Write, read, and evaluate expressions in which letters stand for numbers.</li> <li>CCSS.6.EE.3. Apply the properties of operations to generate equivalent expressions.</li> <li>CCSS.6.EE.4. Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them).</li> </ul> </li> </ul> | <ul> <li>ENDURING UNDERSTANDINGS</li> <li>Expressions are powerful tools for exploring, reasoning about, and representing situations.</li> <li>Variables have many different meanings, depending on context and purpose.</li> <li>Variables permit writing expressions whose values are unknown or vary under different circumstances.</li> <li>Two or more expressions may be equivalent, even when their symbolic forms differ.</li> <li>Linear expressions may be added to or subtracted from one another.</li> </ul> | <ul> <li>ESSENTIAL QUESTIONS</li> <li>What is meant by an "algebraic expression"?</li> <li>How can algebraic expressions be used to represent real-life situations?</li> <li>How is a variable used in the real world?</li> <li>Why do we need an order of operations?</li> <li>Why is algebraic reasoning important?</li> </ul> |  |
| CCSS.6.EE.6. Use variables to represent numbers  | Acqu   | isition  |  |
|  | Students will understand   | Students will be skilled at  |  |
| or mathematical problem; understand that a   | Algebraic expressions  | <ul> <li>simplifying algebraic expressions with whole</li> </ul>   |  |
| variable can represent an unknown number, or,  | Exponents  | numbers.   |  |
| depending on the purpose at hand, any number   | Constant   | <ul> <li>creating algebraic expressions from verbal,</li> </ul>  |  |
| in a specified set.  | Coefficient  | written and interpretational expressions   |  |
| CCSS.MATH.CONTENT.7.EE.A.1 Apply properties  | Term   | <ul> <li>applying and extending previous</li> </ul>  |  |
| of operations as strategies to add, subtract,  | Like Terms   | understandings of arithmetic to algebraic  |  |
|  | Variable   | expressions, including whole number  |  |

| <ul> <li>factor, and expand linear expressions with rational coefficients.</li> <li>CCSS.MATH.CONTENT.7.EE.A.2 Understand that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related. For example, a + 0.05a = 1.05a means that "increase by 5%" is the same as "multiply by 1.05."</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul> | <ul> <li>Distributive Property</li> <li>Integer</li> <li>Rational number</li> </ul> | exponents                       |
|--|---|---------------------------------|
| Used in Content Area Standards   |   | 21 <sup>st</sup> Century Skills |
|  |   | Collaboration                   |
|  |   | Critical Thinking               |
|  |   | Communication                   |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

### Windham School District Curriculum Accelerated Math - Grade 6 Unit 5: Algebraic Thinking - Equations

| FST | ΔRΙ | ISHE | ED G | OALS | ζ. |
|-----|-----|------|------|------|----|
|     |     |      |      |      |    |

Students will continue their study of mathematics in the area of Algebraic Thinking. In this unit, students will create and solve multi-step equations. They will also use this knowledge in real-life applications.

### Content Standards:

- CCSS.6.EE.3. Apply the properties of operations to generate equivalent expressions.
- CCSS.6.EE.5. Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true.
   CCSS.6.EE.7. Solve real-world and mathematical problems by writing and solving equations of the form x + P = q and px = q for cases in which p, q and x are all nonnegative rational numbers.
- CCSS.6.EE.8. Write an inequality of the form x > c or x < c have infinitely many solutions; represent solutions of such inequalities on number line diagrams.
- CCSS.6.EE.9. Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to

### **Stage 1 Desired Results**

### Transfer

### Students will be able to independently use their learning to...

- write and solve equations as a technique for solving problems
- analyze the relationship between the dependent and independent variables using graphs and tables,
   and relate these to the equation.

### Meaning

### ENDURING UNDERSTANDINGS

- Solving an equation is a process of answering a question by finding the value of the variable that makes the equation true.
- An equation is two equivalent expressions.
- Variables are used to represent two quantities in a real world problem that change in relationship to one another.

### **ESSENTIAL QUESTIONS**

- Why do we use inverse operations to solve algebraic equations?
- What is a variable in the real world?
- How is algebra used in the world we live in every day?
- What does it mean to be unequal?

### Acquisition

### Students will understand...

- multi-step algebraic equations and inequalities.
- the difference between dependent and independent variables.
- Integers
- Like terms
- Rational numbers
- like terms
- equivalent expressions

- Solving multi-step equations and inequalities
- Writing an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable.
- Writing an equation from data tables and graphs
- Defining a variable and creating an equation and / or an inequality from a word problem

| express one quantity, thought of as the dependent    | ·                                 |
|--|-----------------------------------|
| variable, in terms of the other quantity, thought of |                                   |
| as the independent variable. Analyze the             |                                   |
| relationship between the dependent and               |                                   |
| independent variables using graphs and tables,       |                                   |
| and relate these to the equation.                    |                                   |
| • CCSS.MATH.CONTENT.7.EE.B.4: Use variables to       |                                   |
| represent quantities in a real-world or              |                                   |
| mathematical problem, and construct simple           |                                   |
| equations and inequalities to solve problems by      |                                   |
| reasoning about the quantities.                      |                                   |
| CCSS.MP1 Make sense of problems and persevere        |                                   |
| in solving them.                                     |                                   |
| CCSS.MP3 Construct viable arguments and critique     |                                   |
| the reasoning of others.                             |                                   |
| CCSS.MP7 Look for and make use of structure.         |                                   |
| Used in Content Area Standards                       | 21st Century Skills               |
|  | Collaboration                     |
|  | Critical Thinking                 |
|  | <ul> <li>Communication</li> </ul> |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Accelerated Math - Grade 6 Unit 6: Geometry & Data - Area & Surface Area

|   | Stage 1 Desired Results  |  |  |
|---|--|--|--|
| ESTABLISHED GOALS:  | Transfer   |  |  |
| Students will continue their study of mathematics in                    | Students will be able to independently use their lea                 | rning to   |  |
| the area of Geometry. In this unit, students will                       | <ul> <li>find the surface area of any solid</li> </ul>               |  |  |
| continue to build their understanding of area and                       | <ul> <li>apply area formulas when solving real life scena</li> </ul> | rios   |  |
| surface area and use it to solve problems.                              | Med  | ning   |  |
|   | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS  |  |
| Content Standards:  | The area of all 2-dimensional figures can be                         | <ul><li>How is geometry part of the world?</li></ul>                 |  |
| <ul> <li>CCSS.6.G.1. Find the area of right triangles, other</li> </ul> | calculated by breaking irregular shapes into                         | Why are there different formulas to find the                         |  |
| triangles, special quadrilaterals, and polygons by                      | rectangles or triangles.   | area of different polygons?  |  |
| composing into rectangles or decomposing into                           | A three-dimensional figure can be represented                        | <ul> <li>How can a net make it easier to find the surface</li> </ul> |  |
| triangles and other shapes; apply these techniques                      | by 2-dimensional nets, which can help                                | area of a 3-dimensional object?                                      |  |
| in the context of solving real-world and                                | determine the surface area of three-                                 | How can nets be used to find surface area on                         |  |
| mathematical problems.  | dimensional figures.   | irregular polygons?  |  |
| CCSS.6.G.3. Draw polygons in the coordinate plane                       |  | isition  |  |
| given coordinates for the vertices; use coordinates                     | Students will understand   | Students will be skilled at  |  |
| to find the length of a side joining points with the                    | Dimensions: Length, width, altitude                                  | <ul> <li>calculating the area of irregular shapes</li> </ul>         |  |
| same first coordinate or the same second                                | Parallelogram, trapezoid, kite                                       | (composite figures).   |  |
| coordinate. Apply these techniques in the context                       | Area as space inside a figure  | <ul> <li>Calculate the area and circumference of circles.</li> </ul> |  |
| of solving real-world and mathematical problems.                        | <ul><li>Area of a parallelogram A = bh</li></ul>                     | <ul> <li>drawing a net for a given solid.</li> </ul>                 |  |
| CCSS.6.G.4. Represent three-dimensional figures                         | <ul> <li>Area of a triangle A = ½ bh</li> </ul>                      | <ul> <li>identifying faces, edges and vertices.</li> </ul>           |  |
| using nets made up of rectangles and triangles,                         | <ul> <li>Area of a trapezoid A = ½ (b1 + b2)h</li> </ul>             | <ul> <li>calculating surface area of rectangular prisms.</li> </ul>  |  |
| and use the nets to find the surface area of these                      | Units squared  | Calculate area and surface area using models                         |  |
| figures. Apply these techniques in the context of                       | Composite (irregular) Figures  | and formulas   |  |
| solving real-world and mathematical problems.                           | Two-dimensional figures  | Calculate surface area of rectangular prisms,                        |  |
|   | <ul> <li>three-dimensional figures (solids)</li> </ul>               | triangular prisms, cones, cylinders, and                             |  |
|   | faces, edges, vertices.  | pyramids   |  |

| <ul> <li>CCSS.7.G.4 Know the formulas for the area and circumference of a circle and use them to solve problems; give an informal derivation of the relationship between the circumference and area of a circle.</li> <li>CCSS.7.G.6 Solve real-world and mathematical problems involving area, volume and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP6 Attend to precision.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul> | <ul> <li>prism</li> <li>nets are three-dimensional figures drawn on a surface.</li> <li>surface area and lateral surface area</li> <li>Radius and diameter of a circle</li> <li>Circumference</li> <li>Pi</li> </ul> |                                       |
|--|--|---------------------------------------|
| Used in Content Area Standards   |  | 21st Century Skills                   |
|  |  | Collaboration                         |
|  |  | <ul> <li>Critical Thinking</li> </ul> |
|  |  | <ul> <li>Communication</li> </ul>     |

| Stage 2 - Evidence   |  |  |  |
|--|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |  |

### Windham School District Curriculum Accelerated Math - Grade 6 Unit 7: Geometry - Triangles

### ESTABLISHED GOALS:

Students will continue their study of mathematics in the area of geometry. In this unit, students will gain a deeper understanding of angles and triangles and will solve real-world problems involving geometric figures.

### Content Standards:

- CCSS.7.G.2. Draw (freehand, with ruler and protractor, and with technology) geometric shapes with given conditions. Focus on constructing triangles from three measures of angles or sides, noticing when the conditions determine a unique triangle, more than one triangle, or no triangle.
- CCSS.MATH.CONTENT.7.G.B.5: Use facts about supplementary, complementary, vertical, and adjacent angles in a multi-step problem to write and solve simple equations for an unknown angle in a figure.
- CCSS.MP4 Model with mathematics.
- CCSS.MP5 Use appropriate tools strategically.
- CCSS.MP6 Attend to precision.

### **Stage 1 Desired Results**

### Transfer

### Students will be able to independently use their learning to...

use their knowledge of triangles to solve real-world problems involving geometric figures.

### Meaning

### **ENDURING UNDERSTANDINGS**

- Drawings and constructions help to see the relationships and differences between geometrical figures.
- Analyzing geometric relationships develops reasoning and justification skills.
- Angle relationships can be used to determine missing angle measures in diagrams.

### **ESSENTIAL QUESTIONS**

- How do geometric models describe spatial relationships?
- How are geometric shapes and objects classified?
- What are the major classifications and relationships of angles, polygons and solids?

### **Acquisition**

### Students will understand...

- the requirements for three segments to form a triangle.
- there are 180 degrees in every triangle.
- the classifications of triangles for both sides and angles: acute, obtuse, right, scalene, isosceles, equilateral
- Facts about supplementary, complementary, vertical, and adjacent angles
- Angle pair relationships: adjacent, vertical, complementary, supplementary, linear pair
- conditions needed to construct a unique triangle, more than one triangle, or no triangle.

- creating triangles given specific sides and/or angles.
- finding missing angles in a triangle.
- classifying a triangle by both its sides and its angles.
- Identifying values of angles in complementary and supplementary relationships
- Using vertical, complementary, and supplementary angle relationships to find missing angles
- Solving for unknown angles using equations

| Used in Content Area Standards | 21 <sup>st</sup> Century Skills   |
|--------------------------------|-----------------------------------|
|                                | Communication                     |
|                                | Critical Thinking                 |
|                                | <ul> <li>Collaboration</li> </ul> |
|                                |                                   |

| Stage 2 - Evidence   |  |  |  |
|--|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |  |

### Windham School District Curriculum Accelerated Math - Grade 6 Unit 8: Geometry & Data - Volume

|  | Stage 1 Desired Results  |  |  |
|--|--|--|--|
| ESTABLISHED GOALS:   | Tro  | ansfer   |  |
| Students will continue their study of mathematics in the area of | Students will be able to independently use the                 | eir learning to  |  |
| Geometry. In this unit, students will continue their             | <ul> <li>apply volume formulas in the context of so</li> </ul> | olving real-world problems                                     |  |
| understanding of volume.   | • explain the difference between surface are                   | ea and volume of objects.                                      |  |
|  | Meaning  |  |  |
| Content Standards:   | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS  |  |
| CCSS.6.G.2. Find the volume of a right rectangular prism         | <ul> <li>Area, surface area and volume have</li> </ul>         | <ul><li>What does volume mean?</li></ul>                       |  |
| with fractional edge lengths by packing it with unit cubes       | applications in real world situations.                         | <ul> <li>How are the volumes of rectangular prism</li> </ul>   |  |
| of the appropriate unit fraction edge lengths, and show          | • Dimension is a measure of the width,                         | and triangular prism related?                                  |  |
| that the volume is the same as would be found by                 | height, or length of a figure.                                 | What is the difference between volume and                      |  |
| multiplying the edge lengths of the prism. Apply the             | Different 3-dimensional figures can have                       | surface area?  |  |
| formulas V = I w h and V = b h to find volumes of right          | the same volume even if the dimensions                         |  |  |
| rectangular prisms with fractional edge lengths in the           | are not all the same.  |  |  |
| context of solving real-world and mathematical problems.         | Acqu   | uisition   |  |
| CCSS. 7.G.6 Solve real-world and mathematical problems           | Students will understand                                       | Students will be skilled at                                    |  |
| involving area, volume and surface area of two- and three-       | - 101/8011   | <ul> <li>Calculating volume using models</li> </ul>            |  |
| dimensional objects composed of triangles, quadrilaterals,       | Polyhedron   | <ul> <li>Fluently calculating volume using formulas</li> </ul> |  |
| polygons, cubes, and right prisms.                               | ● Edge   | <ul> <li>Applying the formulas for volume of three-</li> </ul> |  |
| CCSS.MP1 Make sense of problems and persevere in                 | Vertex   | dimensional figures  |  |
| solving them.  | Length   | <ul> <li>Differentiating between volume and the</li> </ul>     |  |
| CCSS.MP6 Attend to precision.                                    | Width  | surface area to solve problem for three-                       |  |
| CCSS.MP8 Look for and express regularity in repeated             | Depth  | dimensional figures  |  |
| reasoning.   | Cubic Units  | <ul> <li>Calculating and explaining how to find the</li> </ul> |  |
|  | <ul> <li>Formulas for prism: V=LWH or V=Bh</li> </ul>          | area, volume, and surface area for two- and                    |  |
|  | Irregular Figures  | three- dimensional objects from real-world                     |  |
|  | Prism  | situations   |  |

| volume as the space inside a solid. |   |
|-------------------------------------|---|
| Used in Content Area Standards      | 21 <sup>st</sup> Century Skills   |
|                                     | <ul><li>Collaboration</li><li>Critical Thinking</li><li>Communication</li></ul> |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |

## Windham School District Curriculum Accelerated Math - Grade 6 Unit 9: Geometry & Data - Statistics & Probability

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Students will continue their study of mathematics in the area of Geometry and Data. In this unit, students will continue their understanding of data analysis and statistical graphs.

### Content Standards:

- CCSS.6.SP.1. Recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. CCSS.6.SP.2. Understand that a set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.
- CCSS.6.SP.3. Recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.
- CCSS.6.SP.4. Display numerical data in plots on a number line, including dot plots, histograms, and box plots.
- CCSS.6.SP.5. Summarize numerical data sets in relation to their context, such as by:
- CCSS.6.SP.5. a. Reporting the number observations.

### **Stage 1 Desired Results**

### Transfer

### Students will be able to independently use their learning to...

- analyze graphs found in multiple sources
- describe data using graphs and measures of central tendency

### Meaning

### ENDURING UNDERSTANDINGS

- A statistical question anticipates variability in the data related to the question and accounts for it in the answers.
- A set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.
- A measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.

### **ESSENTIAL QUESTIONS**

- How are statistics used to collect, analyze, and draw conclusions in today's society?
- Why are statistics important in the world?
- What are the ways that data can be represented visually?
- Why is it better to use different graphs and diagrams to understand data?
- What are the different ways in which we can summarize data sets?

### Acquisition

### Students will understand...

- line plots, histograms, bar graphs, and scatter plots as visual representations of data.
- measures of central tendency: mean, median, and the mode.
- data can be misleading
- statistical questioning
- Sampling

- Determining measures of central tendency and variation
- Choosing which measure of central tendency is appropriate for a given set of points
- Analyzing data from a given dot plot, histogram, and box plots
- Reporting observations about data using

| <ul> <li>CCSS.6.SP.5. b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.</li> <li>CCSS.6.SP.5. c. Giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.</li> <li>CCSS.6.SP.5. d. Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP6 Attend to precision</li> </ul> | <ul> <li>Frequency</li> <li>Distribution</li> <li>Symmetric</li> <li>Outliers</li> <li>balance point</li> <li>measures of variation: range, quartile, interquartile range (IQR), absolute deviation, mean absolute deviation</li> <li>Box-and-whisker plot</li> </ul> | • | mathematical vocabulary Summarize and describe distributions using both measures of central tendency as well as variation data Make predictions from graphs |
|---|---|---|---|
| Used in Content Area Standards  |   |   | 21 <sup>st</sup> Century Skills   |
|   |   | • | Communication Critical Thinking   |
|   |   | • | Technology Literacy   |

| Stage 2 - Evidence   |   |  |  |  |
|--|---|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |   |  |  |  |
|  | ASSESSMENT: Written Assessments or Projects |  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |   |  |  |  |

Title of Curriculum: 7th Grade Math Curriculum

| Unit Name                                    | What (content, vocab)   | Why (enduring understandings)   | How (skills)  |
|--|---|---|---|
| Unit 1: Ratio and Proportional Relationships | <ul> <li>Ratio, rate, unit rate</li> <li>Equivalent ratios</li> <li>Proportional relationship</li> <li>Percent Proportion and Equation</li> <li>Constant rate of change</li> <li>Complex fractions</li> <li>Markups, discounts, sales tax, commission, simple interest</li> </ul> | <ul> <li>A proportion is an equality of ratios.</li> <li>Proportional relationships guide many aspects of life: nature, drawings, and financial scenarios.</li> <li>The connections between percents, decimals, and fractions are critical to help order, analyze, construct, and make predictions in everyday real-world and mathematical situations.</li> </ul> | <ul> <li>Calculate complex unit rates</li> <li>Solve percent equations using proportions</li> <li>Calculate discount or sale price of an item</li> <li>Calculate sales tax</li> <li>Solve percent word problems including percent change and percent error</li> <li>Express proportions in tables and graphs</li> <li>Express a proportional relationship in an equation</li> <li>Graph proportional relationship</li> <li>Interpret a point on a graph in context</li> </ul> |
| Unit 2: The Number System                    | <ul> <li>Absolute value</li> <li>Zero pairs</li> <li>Additive inverse</li> <li>Operations with integers</li> <li>Order of Operations</li> <li>Rational Numbers</li> <li>Terminating and repeating decimals</li> </ul>   | <ul> <li>The properties of operations for whole numbers hold true for rational numbers.</li> <li>Rational numbers are all numbers that can be written as a fraction including natural numbers, whole numbers and integers.</li> </ul>   | <ul> <li>Model addition and subtraction of signed<br/>numbers on a number line</li> <li>Add, subtract, multiply, and divide with</li> </ul>   |
| Unit 3: Expressions and Equations            | <ul><li>Distributive Property</li><li>Algebraic Properties</li><li>Inequalities</li></ul>   | Real world situations can be represented symbolically   | Simplify algebraic expressions with rational numbers  |

|                                 | <ul> <li>Variables, constants, and coefficients</li> <li>Like terms</li> <li>Equivalent expressions and equations</li> </ul> | with expressions and equations.  An equation is formed by two equivalent expressions.  Equivalent equations represent the same value in unique forms.  | <ul> <li>Create algebraic expressions from verbal expressions</li> <li>Define a variable and create an equation from a word problem</li> <li>Create and solve one-step equations with integers by balancing the equation</li> <li>Solve two-step equations by using equivalent equations</li> <li>Create and solve one- and two- step inequalities</li> <li>Graph inequalities on a number line</li> <li>Rewrite expressions in different forms</li> <li>Solve problems with fractional coefficients</li> <li>Check for reasonableness of solutions</li> <li>Finding the Greatest Common Factor for monomials</li> <li>Factor linear expressions using the distributive property</li> </ul> |
|---------------------------------|--|--|---|
| Geometry - Circle/Scale         | <ul> <li>Circumference and area</li> <li>Composite figures</li> <li>Scale drawings</li> <li>Scale factor</li> </ul>          | <ul> <li>Scale drawings are proportional to one another by a measure called the scale factor.</li> <li>Proportional relationships can be used to draw geometric figures at differing scales.</li> <li>A circle is a closed shape that is defined by the set of points that are the same distance from the center of the circle.</li> </ul> | Explain the change in area and volume when applying scale factor  |
| Geometry – Angles and Triangles | <ul><li>Properties of triangles</li><li>Classification of triangles:<br/>acute, obtuse, right</li></ul>                      | Drawings and constructions<br>help to see the relationships  | <ul> <li>Create triangles given specific sides and/or angles</li> <li>Determine the missing angles in triangles</li> </ul>  |

|             |  | <ul> <li>and differences between geometrical figures.</li> <li>Analyzing geometric relationships develops reasoning and justification skills.</li> <li>Angle relationships can be used to determine missing angle measures in diagrams.</li> </ul>  | <ul> <li>Classify triangles by their sides and angles</li> <li>determine the missing angles in polygons.</li> <li>break polygons into triangles and computing the sum of interior angles.</li> <li>classify angle pair relationships.</li> <li>create algebraic equations using angle pair relationships.</li> </ul> |
|-------------|--|---|--|
| Statistics  | <ul> <li>Measures of Central Tendency</li> <li>Dispersion of data</li> <li>Variation</li> <li>Sampling Techniques</li> <li>Bias</li> <li>Valid and Invalid inferences</li> <li>Comparing data sets</li> </ul>  | <ul> <li>A statistical question anticipates variability in the data related to the question and accounts for it in the answers.</li> <li>A set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.</li> </ul> | · · · · · · · · · · · · · · · · · · ·  |
| Probability | <ul> <li>Probability is between and includes 0 and 1</li> <li>Experimental probability</li> <li>Theoretical Probability</li> <li>Tree diagrams</li> <li>Dependent and independent events</li> <li>Compound probability</li> <li>possible and favorable outcomes</li> </ul> | <ul> <li>Probability is used to predict<br/>the likelihood of an event<br/>and make decisions.</li> <li>Key to valuable experimenta<br/>probability is good data.</li> </ul>  | <ul><li>calculate experimental probability.</li><li>Compare different experimental</li></ul>   |

|  | <ul> <li>Calculate compound probability of both</li> </ul> |
|--|--|
|  | dependent and independent events.                          |

## Windham School District Curriculum Mathematics - Grade 7 Unit 1: Ratio & Proportional Relationships

**Stage 1 Desired Results** 

### ESTABLISHED GOALS:

Students will continue their study of mathematics in the area of algebra. In this unit, students will gain a deeper understanding of ratio and proportional relationships and apply to real world applications.

### Content Standards:

- CCSS.7.RP.1. Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units.
- CCSS.7.RP.2. Recognize and represent proportional relationships between quantities.
- CCSS.7.RP.3. Use proportional relationships to solve multistep ratio and percent problems.
   Examples: simple interest, tax, markups and markdowns, gratuities and commissions, fees, percent increase and decrease, percent error.
- CCSS.MP1 Make sense of problems and persevere in solving them.
- CCSS.MP2 Reason abstractly and quantitatively.
- CCSS.MP6 Attend to precision.

### Transfer

### Students will be able to independently use their learning to...

- solve real-world problem using proportional relationships and percent relationships
- connect proportional relationships to linear relationships
- apply proportional reasoning to solve problems involving scale factor

### Meaning

### ENDURING UNDERSTANDINGS

- A proportion is an equality of ratios.
- Proportional relationships guide many aspects of life: nature, drawings, and financial scenarios.
- The connections between percents, decimals, and fractions are critical to help order, analyze, construct, and make predictions in everyday real-world and mathematical situations.

### ESSENTIAL QUESTIONS

- What is the better deal?
- How can proportions be used to solve a variety of problems?

### **Acquisition**

### Students will understand...

- unit rate is the rate of change based on one.
- a proportion is two ratios that are equivalent.
- a complex fraction is a comparison of decimals or fractions and may be expressed as a simple fraction.
- constant of proportionality is the rate of change.

- calculating complex unit rates.
- solving a percent equation using proportions.
- calculating the discount and the sale price of an item.
- calculating sales tax.
- solving percent word problems involving percent change and percent error.

| <ul> <li>CCSS.MP7 Look for and make use of structure.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul> | <ul> <li>the graph of a proportional relationship is a straight line that goes through the origin.</li> <li>the concept of interest.</li> <li>commission is money earned based on sales.</li> <li>markups, markdowns, and sales tax are related to sales.</li> </ul> | <ul> <li>expressing proportions in tables and graphs.</li> <li>expressing a proportional relationship in an equation.</li> <li>graphing proportional relationships.</li> <li>interpreting a point in the graph in the context of a word problem.</li> </ul> |
|---|--|---|
| Used in Content Area Standards  |  | 21st Century Skills   |
|   |  | Critical Thinking   |
|   |  | Communication   |
|   |  |   |

| Stage 2 - Evidence                          |  |  |  |  |
|---|--|--|--|--|
| Evaluative Criteria Assessment Evidence     |  |  |  |  |
| ASSESSMENT: Written Assessments or Projects |  |  |  |  |
|   | Other Evidence: independent practice, classroom observations and discussions |  |  |  |

## Windham School District Curriculum Mathematics - Grade 7 Unit 2: The Number System

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Students will continue their study of mathematics in the area of numbers and operations. In this unit, students will gain a deeper understanding of the number system, and will operate with rational numbers.

### Content Standards:

- CCSS.7.NS.1. Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram.
- CCSS.7.NS.2. Apply and extend previous understandings of multiplication and division and of fractions to multiply and divide rational numbers.
- CCSS.7.NS.3. Solve real-world and mathematical problems involving the four operations with rational numbers.
- CCSS.MP1 Make sense of problems and persevere in solving them.
- CCSS.MP2 Reason abstractly and quantitatively.
- CCSS.MP4 Model with mathematics.

### **Stage 1 Desired Results**

### Transfer

### Students will be able to independently use their learning to...

- recognize rational numbers, especially signed numbers, as they relate to real world scenarios
- fluently add, subtract, multiply and divide rational numbers.
- solve equations and inequalities with rational numbers.

### Meaning

### ENDURING UNDERSTANDINGS

- The properties of operations for whole numbers hold true for rational numbers.
- Rational numbers are all numbers that can be written as a fraction including natural numbers, whole numbers and integers.

### **ESSENTIAL QUESTIONS**

- How are integers related to science, social studies and language arts?
- How do you represent rational numbers?

### **Acquisition**

### Students will understand...

- additive inverses as zero pairs.
- addition and subtraction are inverse operations where subtraction is adding the inverse.
- rules for addition, subtraction, multiplication and division of integers.
- zero cannot be a divisor.
- a fraction must be equivalent to either a terminating or a repeating decimal.

- ordering and comparing rational numbers.
- modeling addition and subtraction of signed numbers on a number line.
- Adding, subtracting, multiplying, and dividing integers.
- adding, subtracting, multiplying and dividing rational numbers.
- using the order of operations with rational numbers.
- evaluating algebraic expressions with integers values.

|                                |  | • | converting common fractions to decimals without a calculator. solving real world problems involving rational numbers. |
|--------------------------------|--|---|---|
| Used in Content Area Standards | ed in Content Area Standards 21st Century Skills |   | 21st Century Skills   |
|                                |  | • | Critical Thinking   |
|                                |  | • | Problem solving   |
|                                |  | • | Communication   |
|                                |  |   |   |

| Stage 2 - Evidence   |  |  |  |  |
|--|--|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |  |  |

## Windham School District Curriculum Mathematics - Grade 7 Unit 3: Expressions & Equations

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Students will continue their study of mathematics in the area of algebra. In this unit, students will gain a deeper understanding of solving real-world problems involving expressions and equations.

### Content Standards:

- CCSS.7.EE.1. Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients.
- CCSS.7.EE.2. Understand that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related.
- CCSS.7.EE.3. Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.
- CCSS.7.EE.4. Use variables to represent quantities in a real-world or mathematical problem, and construct simple equations and inequalities to

### **Stage 1 Desired Results**

### Transfer

### Students will be able to independently use their learning to...

- represent scenarios using expressions and equations.
- use equations as a method to solve real-world problems.

### Meaning

### ENDURING UNDERSTANDINGS

- Real world situations can be represented symbolically with expressions and equations.
- An equation is formed by two equivalent expressions.
- Equivalent equations represent the same value in unique forms.

### **ESSENTIAL QUESTIONS**

- How do you compare algebraic solutions to arithmetic solutions?
- How do you translate real world problems to algebraic expressions?
- Does my answer make sense?

### **Acquisition**

### Students will understand...

- the difference between a constant and a coefficient, including coefficients of one.
- like terms are terms with the same variable.
- equivalent expressions have the same value.
- an algebraic equation may have a solution.
- an inequality states two values are not the same.
- commutative, associative, identity, distributive, and inverse properties.
- a monomial is a single term.

- simplifying algebraic expressions with rational numbers.
- creating algebraic expressions from verbal expressions.
- defining a variable and creating an equation from a word problem.
- creating and solving one-step equations with integers by balancing the equation.
- solving two-step equations by using equivalent equations.
- graphing inequalities on a number line.

| solve problems by reasoning about the quantities.  CCSS.MP1 Make sense of problems and persevere in solving them.  CCSS.MP3 Construct viable arguments and critique the reasoning of others.  CCSS.MP7 Look for and make use of structure. | • | creating and solving one and two-step inequalities.  rewriting expressions in a different form; example $\frac{1}{2}$ of $x = .5x = x/2$ solving problems with fractional coefficients. checking for the reasonableness of the solution. finding the Greatest Common Factor for monomials. factoring linear expressions using distributive property. |
|--|---|--|
| Used in Content Area Standards   |   | 21st Century Skills  |
|  | • | Critical Thinking  |
|  | • | Collaboration  |
|  | • | Communication  |

| Stage 2 - Evidence   |                     |  |
|--|---------------------|--|
| Evaluative Criteria  | Assessment Evidence |  |
| ASSESSMENT: Written Assessments or Projects                                  |                     |  |
| Other Evidence: independent practice, classroom observations and discussions |                     |  |

## Windham School District Curriculum Mathematics - Grade 7 Unit 4: Geometry - Circles/Scale

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Students will continue their study of mathematics in the area of geometry. In this unit, students will gain a deeper understanding of finding area and circumference of a circle, as well as using scale to produce new figures.

### Content Standards:

- CCSS.7.G.A.1 Solve problems involving scale drawings of geometric figures, including computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale.
- CCSS.7.G.B.4 Know the formulas for the area and circumference of a circle and use them to solve problems; give an informal derivation of the relationship between the circumference and area of a circle.
- CCSS.MP1 Make sense of problems and persevere in solving them.
- CCSS.MP2 Reason abstractly and quantitatively.
- CCSS.MP5 Use appropriate tools strategically.
- CCSS.MP6 Attend to precision.

### **Stage 1 Desired Results**

### Students will be able to independently use their learning to...

 apply areas and circumferences of circles when finding surface area and volume as well as solving real-life problems.

Transfer

apply proportional reasoning to solve problems involving scale factor

### Meaning

### ENDURING UNDERSTANDINGS

- Scale drawings are proportional to one another by a measure called the scale factor.
- Proportional relationships can be used to draw geometric figures at differing scales.
- A circle is a closed shape that is defined by the set of points that are the same distance from the center of the circle.

### **ESSENTIAL QUESTIONS**

- How can we determine area, given circumference?
- Can we determine diameter or radius, given area or circumference?
- What kinds of problems can you solve using circumference and area formulas?
- How can you use proportions to investigate real-world and mathematical objects at different scales?

### **Acquisition**

### Students will understand...

- circumference of a circle is the distance around the circle.
- formula for calculating the circumference of a circle is  $C = d\pi$  or  $C = 2\pi r$  where C is the circumference of a circle, d is the length of the diameter of the circle, r is the length of the radius of the circle, and d is represented using the approximation 3.14.

- Calculating circumference and area of circles
- Drawing similar figures using scale factor
- Finding missing lengths given similar figures
- Explaining the change in area and volume when applying scale factor

|                                | <ul> <li>formula for calculating the area of a circle is A = πr²</li> <li>Scale drawings are representations of real objects or places that are in proportion to the real objects or places they represent.</li> <li>scale of a drawing is the ratio drawing length : actual length</li> <li>scale of a map is the ratio map distance : actual distance.</li> <li>When calculating the area of a scaled figure, the scale must be applied to all dimensions of the figure.</li> </ul> |   |
|--------------------------------|---|---|
| Used in Content Area Standards |   | 21 <sup>st</sup> Century Skills   |
| •                              |   | <ul><li>Technology Literacy</li><li>Critical Thinking</li><li>Collaboration</li></ul> |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | Other Evidence: independent practice, classroom observations and discussions |  |

## Windham School District Curriculum Mathematics - Grade 7 Unit 5: Geometry - Angles & Triangles

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Students will continue their study of mathematics in the area of geometry. In this unit, students will gain a deeper understanding of angles and triangles, and will solve real-world problems involving geometric figures.

### Content Standards:

- CCSS.7.G.2. Draw (freehand, with ruler and protractor, and with technology) geometric shapes with given conditions. Focus on constructing triangles from three measures of angles or sides, noticing when the conditions determine a unique triangle, more than one triangle, or no triangle.
- CCSS.7.G.5. Use facts about supplementary, complementary, vertical, and adjacent angles in a multi-step problem to write and solve simple equations for an unknown angle in a figure.
- CCSS.MP4 Model with mathematics.
- CCSS.MP5 Use appropriate tools strategically.
- CCSS.MP6 Attend to precision.

### **Stage 1 Desired Results**

### Students will be able to independently use their learning to...

- use angles and triangles to solve real-world problems involving geometric figures.
- use vocabulary and properties in future studies of Geometry.

### Meaning

Transfer

### ENDURING UNDERSTANDINGS

- Drawings and constructions help to see the relationships and differences between geometrical figures.
- Analyzing geometric relationships develops reasoning and justification skills.
- Angle relationships can be used to determine missing angle measures in diagrams.

### **ESSENTIAL QUESTIONS**

- How do geometric models describe spatial relationships?
- What are the major classifications and relationships of angles and triangles?

### Acquisition

### Students will understand...

- the requirements for three segments to form a triangle.
- there are 180 degrees in every triangle.
- the classifications of triangles for both sides and angles.
- the characteristics of a regular polygon.
- the different angle pair relationships: adjacent, vertical, complementary, supplementary, and linear pair.
- congruent angles are angles with the same measure.

- creating triangles given specific sides and/or angles.
- finding missing angles in a triangle.
- classifying a triangle by both its sides and its angles.
- determining the missing angles in polygons.
- breaking polygons into triangles and computing the sum of interior angles.
- classifying angle pair relationships.
- creating algebraic equations using angle pair relationships.

| Used in Content Area Standards | 21 <sup>st</sup> Century Skills |
|--------------------------------|---------------------------------|
|                                | Critical Thinking               |
|                                | Communication                   |
|                                |                                 |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |  |

### Windham School District Curriculum Mathematics - Grade 7 Unit 6: Statistics

| CTARI | ICHED | GOALS |  |
|-------|-------|-------|--|

Students will continue their study of mathematics in the area of data and problem solving. In this unit, students will gain a deeper understanding of statistics, by analyzing and interpreting data from real-world problems.

### Content Standards:

- CCSS.7.SP.1 Understand that statistics can be used to gain information about a population by examining a sample of the population; generalizations about a population from a sample are valid only if the sample is representative of that population. Understand that random sampling tends to produce representative samples and support valid inferences.
- CCSS.7.SP.2. Use data from a random sample to draw inferences about a population with an unknown characteristic of interest. Generate multiple samples (or simulated samples) of the same size to gauge the variation in estimates or predictions.
- CCSS.7.SP.3. Informally assess the degree of visual overlap of two numerical data distributions with similar variabilities, measuring the difference

### **Stage 1 Desired Results**

### Transfer

Students will be able to independently use their learning to...

analyze and interpret data from real-world situations.

### Meaning

### ENDURING UNDERSTANDINGS

- A statistical question anticipates variability in the data related to the question and accounts for it in the answers.
- A set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.

### ESSENTIAL QUESTIONS

How do you interpret data from statistical representations?

### Acquisition

### Students will understand...

- characteristics of each measure of central tendency.
- dispersion of data is the way it is spread out.
- the less variation a set has, the closer the numbers are to each other.
- random sampling gives unbiased data.
- a valid inference is a prediction based on a random sample.

- creating data with a specific mode, median and mean.
- identifying when a measure of central tendency would not be an accurate reflection of the data.
- using data from a random sample to draw inferences about a population.
- analyzing data to make a prediction.
- displaying two samples of data in a box plot to illustrate variability.
- creating a line plot to compare two samples.

| <ul> <li>between the centers by expressing it as a multiple of a measure of variability.</li> <li>CCSS.7.SP.4. Use measures of center and measures of variability for numerical data from random samples to draw informal comparative inferences about two populations.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> </ul> |                                     |
|--|-------------------------------------|
| Used in Content Area Standards   | 21 <sup>st</sup> Century Skills     |
|  | Communication     Critical Thinking |
|  | Critical Thinking                   |

| Stage 2 - Evidence                      |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence |  |  |
|   | ASSESSMENT: Written Assessments or Projects                                  |  |
|   | Other Evidence: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 7 Unit 7: Probability

| <ul> <li>CCSS.7.SP.C.8 Find probabilities of compound events using organized lists, tables, tree diagrams, and simulation.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP4 Model with mathematics.</li> </ul> | probability is either independent or dependent. | <ul> <li>identifying an event that would have a probability of one.</li> <li>calculating compound probability of both dependent and independent events.</li> </ul> |
|---|---|--|
| Used in Content Area Standards  |   | 21 <sup>st</sup> Century Skills  |
|   |   | <ul><li>Communication</li><li>Critical Thinking</li></ul>  |

| Stage 2 - Evidence                          |  |  |
|---|--|--|
| Evaluative Criteria                         | Assessment Evidence  |  |
| ASSESSMENT: Written Assessments or Projects |  |  |
|   | Other Evidence: independent practice, classroom observations and discussions |  |

Title of Curriculum: 7th Grade Accelerated Math

| Unit Name                                    | What (content, vocab)   | Why (enduring understandings)  | How (skills)  |
|--|---|--|---|
| Unit 1: Ratio and Proportional Relationships | <ul> <li>Ratio, rate, unit rate</li> <li>Equivalent ratios</li> <li>Proportional relationship</li> <li>Percent Proportion and Equation</li> <li>Constant rate of change</li> <li>Complex fractions</li> <li>Markups, discounts, sales tax, commission, simple interest</li> </ul> | <ul> <li>A proportion is an equality of ratios.</li> <li>Proportional relationships guide many aspects of life: nature, drawings, and financial scenarios.</li> <li>The connection between percents, decimals, and fractions is essential to help order, analyze, construct, and make predictions in everyday real-world and mathematical situations.</li> </ul> | <ul> <li>Calculate complex unit rates</li> <li>Solve a percent equation</li> <li>Calculate discount or sale price of an item</li> <li>Calculate sales tax</li> <li>Solve percent word problems including percent change and percent error</li> <li>Express proportions in tables and graphs</li> <li>Express a proportional relationship in an equation</li> <li>Interpret a point on a graph in context</li> </ul> |
| Unit 2: The Number System                    | <ul> <li>Absolute value</li> <li>Zero pairs</li> <li>Additive inverse</li> <li>Operations with integers</li> <li>Order of Operations</li> <li>Rational Numbers</li> <li>terminating and repeating decimals</li> </ul>   | <ul> <li>The properties of operations for whole numbers hold true for rational numbers.</li> <li>Rational numbers are all numbers that can be written as a fraction including natural numbers, whole numbers and integers.</li> </ul>  | <ul> <li>Order and compare rational numbers</li> <li>Determine if a number is rational or irrational</li> <li>Model addition and subtraction of signed numbers on a number line</li> </ul>  |

| Unit 3: Expressions and Equations  | <ul> <li>Distributive Property</li> <li>Monomials</li> <li>Binomials</li> <li>Algebraic Properties</li> <li>Inequalities</li> <li>Variables, constants, and coefficients</li> <li>Like terms</li> <li>Equivalent expressions and equations</li> </ul> | <ul> <li>Real world situations can be represented symbolically with expressions and equations.</li> <li>An equation is formed by two equivalent expressions.</li> <li>Equivalent equations represent the same value in unique forms.</li> </ul> | <ul> <li>Estimate, to the nearest whole number, non-perfect square roots</li> <li>Simplify algebraic expressions with rational numbers</li> <li>Create algebraic expressions from verbal expressions</li> <li>Define a variable and create an equation from a word problem</li> <li>Solve one-step equations with integers by balancing the equation</li> <li>Solve two-step equations by using equivalent equations</li> <li>Create and solve one- and two- step inequalities</li> <li>Rewrite expressions in different forms</li> <li>Solve problems with fractional coefficients</li> <li>Check for reasonableness of solutions</li> <li>Find GCF for monomials</li> <li>Factor linear expressions using the distributive property</li> </ul> |
|------------------------------------|---|---|--|
| Unit 4: Transformations            | <ul><li>Transformations</li><li>Congruence</li><li>Similarity</li></ul>   | <ul> <li>Congruent objects can be transformed on top of each other.</li> <li>Similar objects are a combination of rigid motions and dilation.</li> </ul>  | <ul> <li>Transform polygons using dilations, translations, reflections, and rotations.</li> <li>Identify coordinates of transformed figures.</li> <li>Describe sequence of transformations that result in congruent or similar figures.</li> </ul>   |
| Unit 5: Angles and<br>Transversals | <ul> <li>Triangle angle relationships</li> <li>Angles formed by parallel lines cut by a transversal</li> <li>Interior, exterior, and corresponding angles</li> </ul>  | <ul> <li>Analyzing geometric relationships<br/>develops reasoning and<br/>justification skills.</li> <li>Angle relationships can be used to<br/>determine missing angle<br/>measures in diagrams.</li> </ul>                                    | <ul> <li>classify angle pair relationships.</li> <li>create algebraic equations using angle pair relationships.</li> <li>find angle measurements using properties of similar figures, exterior</li> </ul>  |

| Unit 6: Pythagorean Theorem | <ul> <li>Pythagorean Theorem</li> <li>Right Triangles</li> <li>Area of squares</li> <li>Radicals</li> </ul>   | Right triangles have a special relationship among the side lengths which can be represented by a model and a formula.  | <ul> <li>and interior angles, and parallel lines cut by a transversal.</li> <li>Informally prove the Pythagorean Theorem</li> <li>Determine if a triangle is a right triangle using its converse.</li> <li>Apply the Pythagorean Theorem to find missing triangle side lengths.</li> <li>Apply the Pythagorean Theorem to solve problems</li> </ul>   |
|-----------------------------|---|--|---|
| Unit 7: Geometry - Volume   | <ul><li>Cylinder</li><li>Cones</li><li>Spheres</li></ul>  | <ul> <li>Everyday objects have a variety of attributes, each of which can be measured in many ways.</li> <li>Area, surface area and volume have applications in real world situations.</li> <li>Different 3-dimensional figures can have the same volume even if the dimensions are not all the same.</li> </ul> | <ul> <li>and spheres using appropriate formulas and units.</li> <li>Use volume formulas to solve real world problems.</li> </ul>  |
| Unit 8: Statistics          | <ul> <li>Measures of Central Tendency</li> <li>Dispersion of data</li> <li>Variation</li> <li>Sampling Techniques</li> <li>Bias</li> <li>Valid and Invalid inferences</li> <li>Comparing data sets</li> </ul> | <ul> <li>A statistical question anticipates variability in the data related to the question and accounts for it in the answers.</li> <li>A set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.</li> </ul>                | <ul> <li>Create data with specific mode, median, and mean</li> <li>Identify when a measure of center is not an accurate reflection of data</li> <li>Use data from a random sample to draw inferences about a population.</li> <li>Analyze data to make predictions</li> <li>Display two samples of data on a box plot to illustrate variability</li> <li>Create a line plot to compare two samples</li> </ul> |
| Unit 9: Probability         | <ul> <li>Probability is between and includes 0 and 1</li> <li>Experimental probability</li> </ul>   | Probability is used to predict the likelihood of an event and make decisions.  | Perform an activity, record results and calculate experimental probability.   |

| <ul> <li>Theoretical Probability</li> <li>Tree diagrams</li> <li>Dependent and independent events</li> <li>Compound probability</li> <li>possible and favorable outcomes</li> </ul> | Key to valuable experimental probability is good data. | <ul> <li>Compare different experimental probabilities for the same activity and explain the differences.</li> <li>Make predictions based on probability.</li> <li>Create tree diagrams to find total possible outcomes.</li> <li>Express probability as fractions and percents.</li> <li>Identify an event that would have a probability of zero and one.</li> <li>Calculate compound probability of both dependent and independent events.</li> </ul> |
|---|--|--|
|---|--|--|

## Windham School District Curriculum Accelerated Mathematics - Grade 7 Unit 1: Ratio & Proportional Relationships

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Students will continue their study of mathematics in the area of algebra. In this unit, students will gain a deeper understanding of ratio and proportional relationships and apply these concepts to real world applications.

### Content Standards:

- CCSS.7.RP.1. Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units.
- CCSS.7.RP.2. Recognize and represent proportional relationships between quantities.
- CCSS.7.RP.3. Use proportional relationships to solve multistep ratio and percent problems.
   Examples: simple interest, tax, markups and markdowns, gratuities and commissions, fees, percent increase and decrease, percent error.
- CCSS.MP1 Make sense of problems and persevere in solving them.
- CCSS.MP2 Reason abstractly and quantitatively.
- CCSS.MP6 Attend to precision.
- CCSS.MP7 Look for and make use of structure.
- CCSS.MP8 Look for and express regularity in repeated reasoning.

### **Stage 1 Desired Results**

### Transfer

### Students will be able to independently use their learning to...

- solve real-world problem using proportional relationships and percent relationships
- connect proportional relationships to linear relationships
- apply proportional reasoning to solve problems involving scale factor

### Meaning

### ENDURING UNDERSTANDINGS

- A proportion is an equality of ratios.
- Proportional relationships guide many aspects of life: nature, drawings, and financial scenarios.
- The connection between percents, decimals, and fractionsis critical to help order, analyze, construct, and make predictions in everyday real-world and mathematical situations.

### ESSENTIAL QUESTIONS

- What is the better deal?
- How can proportions be used to solve a variety of problems?

### **Acquisition**

### Students will understand...

- unit rate is the rate of change based on one.
- a proportion is two ratios that are equivalent.
- a complex fraction is a comparison of decimals or fractions and may be expressed as a simple fraction.
- constant of proportionality is the rate of change.
- linear equation will graph as a line due to constant rate of change.

- calculating complex unit rates.
- solving a percent equation using proportions.
- calculating the discount and the sale price of an item.
- calculating sales tax.
- solving percent word problems involving percent change and percent error.
- expressing proportions in tables and graphs.

| Used in Content Area Standards 21 <sup>st</sup> Century Skills |  |
|--|--|
| 21 Century Skins   |  |
| Critical Thinking  |  |
| Communication  |  |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | Other Evidence: independent practice, classroom observations and discussions |  |

### Windham School District Curriculum Accelerated Mathematics - Grade 7 Unit 2: The Number System

| CCTA | DI | ISHFI | $\sim c \alpha$ | VIC. |
|------|----|-------|-----------------|------|
|      |    |       |                 |      |

Students will continue their study of mathematics in the area of numbers and operations. In this unit, students will gain a deeper understanding of the number system and will calculate with rational numbers.

### Content Standards:

- CCSS.7.NS.1. Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram.
- CCSS.7.NS.2. Apply and extend previous understandings of multiplication and division and of fractions to multiply and divide rational numbers.
- CCSS.7.NS.3. Solve real-world and mathematical problems involving the four operations with rational numbers.
- CCSS.MP1 Make sense of problems and persevere in solving them.
- CCSS.MP2 Reason abstractly and quantitatively.
- CCSS.MP4 Model with mathematics.

### **Stage 1 Desired Results**

### Transfer

### Students will be able to independently use their learning to...

- fluently add, subtract, multiply and divide rational numbers.
- solve equations and inequalities with rational numbers.

### Meaning

### ENDURING UNDERSTANDINGS

- The properties of operations for whole numbers hold true for rational numbers.
- Rational numbers are all numbers that can be written as a fraction including natural numbers, whole numbers and integers.

### **ESSENTIAL QUESTIONS**

- How are integers related to science, social studies and language arts?
- How do you represent rational numbers?

### **Acquisition**

### Students will understand...

- additive inverses as zero pairs.
- that addition and subtraction are inverse operations and that subtraction problems can be changed to addition problems by adding the inverse.
- adding the additive inverse.
- the rules for addition, subtraction, multiplication and division of integers.
- exponents, square roots, and cube roots.
- that zero cannot be a divisor.
- that a fraction must be equivalent to either a terminating or a repeating decimal.

- ordering and comparing rational numbers.
- determining if a number is rational or irrational.
- modeling addition and subtraction of signed numbers on a number line.
- adding, subtracting, multiplying and dividing rational numbers.
- using the order of operations with rational numbers.
- evaluating algebraic expressions with integers values.
- converting common fractions to decimals without a calculator.

|                                | the difference between a rational and irrational number. | • | Solve real-world problems involving rational numbers. finding square roots of perfect squares and cube roots of perfect cubes. interpreting sums of rational numbers in a real-world context. solving real world problems involving rational numbers. |
|--------------------------------|--|---|---|
| Used in Content Area Standards |  |   | 21 <sup>st</sup> Century Skills   |
|                                |  | • | Critical Thinking   |
|                                |  | • | Perseverance  |
|                                |  | • | Communication   |
|                                |  |   |   |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | Other Evidence: independent practice, classroom observations and discussions |  |

### Windham School District Curriculum **Accelerated Mathematics - Grade 7 Unit 3: Expressions & Equations**

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Students will continue their study of mathematics in the area of algebra. In this unit, students will gain a deeper understanding of solving real-world problems involving expressions and equations.

### Content Standards:

- CCSS.7.EE.1. Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients.
- CCSS.7.EE.2. Understand that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related.
- CCSS.7.EE.3. Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.
- CCSS.7.EE.4. Use variables to represent quantities in a real-world or mathematical problem, and

### **Stage 1 Desired Results**

### Students will be able to independently use their learning to...

- solve real-world problems using numerical and algebraic expressions and equations.
- use linear equations to solve more advanced mathematical equations

### Meaning

Transfer

### ENDURING UNDERSTANDINGS

- Real world situations can be represented symbolically with expressions and equations.
- An equation is formed by two equivalent expressions.
- Equivalent equations represent the same value in unique forms.

### **ESSENTIAL QUESTIONS**

- How do you compare algebraic solutions to arithmetic solutions?
- How do you translate real world problems to algebraic expressions?
- Does my answer make sense?

### **Acquisition**

### Students will understand...

- difference between a constant and a coefficient, including coefficients of one.
- like terms are terms with the same variable.
- equivalent expressions have the same value.
- an algebraic equation may have a solution.
- an inequality states two values are not the same.
- commutative, associative, identity, distributive, and inverse properties.
- a monomial is a single term.

- simplifying algebraic expressions with rational numbers.
- creating algebraic expressions from verbal expressions.
- defining a variable and creating an equation from a word problem.
- solving one-step equations with integers by balancing the equation.
- solving two-step equations by using equivalent equations.
- solving equations with variables on both sides of the equation.

| oscu iii content Arca Standards   | Critical Thinking     Communication  |
|---|--|
| Used in Content Area Standards  | 21st Century Skills  |
| CCSS.MP7 Look for and make use of structure.  | <ul> <li>checking for the reasonableness of the solution.</li> <li>finding the Greatest Common Factor for monomials.</li> <li>factoring linear expressions using distributive property.</li> </ul>   |
| <ul> <li>construct simple equations and inequalities to solve problems by reasoning about the quantities.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> </ul> | <ul> <li>graphing inequalities on a number line.</li> <li>creating and solving one-step inequalities.</li> <li>creating and solving two-step inequalities.</li> <li>rewriting expressions in a different form; example ½ of x = .5x = x/2</li> <li>solving problems with fractional coefficients.</li> </ul> |

| Stage 2 - Evidence   |  |
|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |
| Other Evidence: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Accelerated Mathematics - Grade 7 Unit 4: Geometry - Transformations

**Stage 1 Desired Results** 

| CTADI | ICHEU | CUVIC |  |
|-------|-------|-------|--|

Students will continue their study of mathematics in the area of geometry. In this unit, students will gain a deeper understanding of transformations, and will be able to determine whether a transformation creates a congruent or similar figure.

### Content Standards:

- CCSS.8.G.1. Verify experimentally the properties of rotations, reflections, and translations.
- CCSS.8.G.2. Understand that a two-dimensional figure is congruent to another if the second can be obtained from the first by a sequence of rotations, reflections, and translations; given two congruent figures, describe a sequence that exhibits the congruence between them.
- CCSS.8.G.3. Describe the effect of dilations, translations, rotations, and reflections on two-dimensional figures using coordinates.
- CCSS.8.G.4. Understand that a two-dimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations; given two similar two-dimensional figures, describe a sequence that exhibits the similarity between them.
- CCSS.MP1 Make sense of problems and persevere in solving them.
- CCSS.MP6 Attend to precision
- CCSS.MP7 Look for and make use of structure.

# Transfer

# Students will be able to independently use their learning to...

- translate, reflect, rotate and dilate figures on a coordinate plane.
- determine whether the new figure is congruent or similar to the original figure.

# Meaning

# **ENDURING UNDERSTANDINGS**

- Congruent objects can be transformed on top of each other.
- Similar objects are a combination of rigid motions and dilation.

# **ESSENTIAL QUESTIONS**

What movements preserve or change shapes?

# Acquisition

# Students will understand...

- Transformations: dilations, translations, reflections, and rotations
- transformations preserve congruence of polygons, lines, and angle measurements.
- dilations create similar figures.

- transforming polygons using dilations, translations, reflections, and rotations.
- identifying coordinates of transformed figures.
- describing a sequence of transformations that result in congruent or similar figures.

| Used in Content Area Standards | 21 <sup>st</sup> Century Skills         |
|--------------------------------|---|
|                                | <ul> <li>Technology Literacy</li> </ul> |
|                                | Critical thinking                       |
|                                |   |

| Stage 2 - Evidence   |  |
|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum **Accelerated Mathematics - Grade 7 Unit 5: Geometry - Angles & Transversals**

| ECT | $\Gamma \Lambda DI$ | ICHED | GOALS |
|-----|---------------------|-------|-------|

Students will continue their study of mathematics in the area of Students will be able to independently use their learning to... geometry. In this unit, students will gain a deeper understanding of angles, angle relationships, and transversals and will solve real-world problems involving geometric figures.

### Content Standards:

- CCSS.7.G.5. Use facts about supplementary, complementary, vertical, and adjacent angles in a multistep problem to write and solve simple equations for an unknown angle in a figure.
- CCSS.8.G.1 Verify experimentally the properties of rotations, reflections, and translations.
- CCSS.8.G.2 Understand that a two-dimensional figure is congruent to another if the second can be obtained from the first by a sequence of rotations, reflections, and translations; given two congruent figures, describe a sequence that exhibits the congruence between them.
- CCSS.8.G.3 Describe the effect of dilations, translations, rotations, and reflections on two-dimensional figures using coordinates.
- CCSS.8.G.4 Understand that a two-dimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations; given two similar two-dimensional figures,

# **Stage 1 Desired Results**

- use angles and triangles to solve real-world problems involving geometric figures.
- use vocabulary and properties in future studies of Geometry.

# Meanina

Transfer

# ENDURING UNDERSTANDINGS

- Analyzing geometric relationships develops reasoning and justification skills.
- Angle relationships can be used to determine missing angle measures in diagrams.

# **ESSENTIAL QUESTIONS**

- Who needs to use angles and how do they use them?
- What special relationships exist between angles and lines?
- How many pairs of congruent angles are created when two parallel lines are cut by a transversal?

# **Acquisition**

# Students will understand...

- different angle pair relationships: adjacent, vertical, complementary, supplementary, and linear pair.
- congruent angles are angles with the same measure.
- intersecting lines are lines with one point in common.
- angle relationships between exterior and interior triangle angles, similar triangles, and parallel lines cut by a transversal.

- classifying angle pair relationships.
- creating algebraic equations using angle pair relationships.
- finding angle measurements using properties of similar figures, exterior and interior angles, and parallel lines cut by a transversal.

| <ul> <li>describe a sequence that exhibits the similarity between them.</li> <li>CCSS.8.G.5 Use informal arguments to establish facts about the angle sum and exterior angle of triangles, about the angles created when parallel lines are cut by a transversal, and the angle-angle criterion for similarity of triangles.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> </ul> |                                 |
|--|---------------------------------|
| CCSS.MP6 Attend to precision.  |                                 |
| Used in Content Area Standards   | 21 <sup>st</sup> Century Skills |
|  | Technology Literacy             |

| Stage 2 - Evidence                      |  |
|---|--|
| Evaluative Criteria Assessment Evidence |  |
|   | ASSESSMENT: Written Assessments or Projects                                  |
|   | OTHER EVIDENCE: independent practice, classroom observations and discussions |

# Windham School District Curriculum Accelerated Mathematics - Grade 7 Unit 6: Geometry - The Pythagorean Theorem

| , , ,   |   |   |  |
|---|---|---|--|
|   | Stage 1 Desired Results   |   |  |
| ESTABLISHED GOALS:  | Transfer  |   |  |
| Students will continue their study of mathematics in                | Students will be able to independently use their lea                | rning to  |  |
| the area of geometry. In this unit, students will gain a            | <ul> <li>apply pythagorean theorem to future geometric</li> </ul>   | c concepts  |  |
| deeper understanding of the pythagorean theorem and                 | <ul> <li>use pythagorean theorem and its converse to see</li> </ul> | olve real-world problems.   |  |
| its converse.   | Med   | aning   |  |
|   | ENDURING UNDERSTANDINGS   | ESSENTIAL QUESTIONS   |  |
| Content Standards:  | Right triangles have a special relationship                         | How can right triangle relationships model real                         |  |
| CCSS.8.G.6. Explain a proof of the Pythagorean                      | among the side lengths which can be                                 | world phenomena?  |  |
| Theorem and its converse.   | represented by a model and a formula.                               | How can you use the Pythagorean Theorem to                              |  |
| <ul> <li>CCSS.8.G.7. Apply the Pythagorean Theorem to</li> </ul>    |   | solve everyday problems?  |  |
| determine unknown side lengths in right triangles                   |   |   |  |
| in real-world and mathematical problems in two                      | Acquisition   |   |  |
| and three dimensions.   | Students will understand  | Students will be skilled at   |  |
| <ul> <li>CCSS8.G.8. Apply the Pythagorean Theorem to</li> </ul>     | Pythagorean Theorem equates the sum of the                          | <ul> <li>Informally proving the Pythagorean Theorem</li> </ul>          |  |
| find the distance between two points in a                           | squares of the legs to the square of the                            | $(a^2 + b^2 = c^2)$   |  |
| coordinate system.  | hypotenuse.   | <ul> <li>Determining if a triangle is a right triangle using</li> </ul> |  |
| <ul> <li>CCSS.MP.2 Reason abstractly and quantitatively.</li> </ul> | • converse of the Pythagorean Theorem can be                        | its converse.   |  |
| <ul> <li>CCSS.MP.4 Model with mathematics.</li> </ul>               | used to determine whether a given triangle is a                     | <ul> <li>Applying the Pythagorean Theorem to find</li> </ul>            |  |
| <ul> <li>CCSS.MP.6 Attend to precision.</li> </ul>                  | right triangle.   | missing triangle side lengths.  |  |
|   |   | <ul> <li>Applying the Pythagorean Theorem to solve</li> </ul>           |  |
|   |   | problems  |  |
| Used in Content Area Standards                                      |   | 21 <sup>st</sup> Century Skills   |  |
|   |   | Technology Literacy   |  |
|   |   | Critical Thinking   |  |

| Stage 2 - Evidence   |  |
|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Accelerated Mathematics - Grade 7 Unit 7: Geometry: Volume

|   | Stage 1 Desired Results   |   |
|---|---|---|
| ESTABLISHED GOALS:  | Transfer  | •   |
| Students will continue their study of mathematics in  | Students will be able to independently use their learning t   | to  |
| the area of geometry. In this unit, students will gain  | • solve real-world problems including the volume of cyli  | inders, cones and spheres.  |
| a deeper understanding of the volume of three-  | Meaning   | 1   |
| dimensional figures; such as cylinders, cones and   | ENDURING UNDERSTANDINGS   | ESSENTIAL QUESTIONS   |
| spheres.  | • Everyday objects have a variety of attributes, each of which can be measured in many ways.  | <ul> <li>Will the size of a container indicate its contents?</li> </ul>   |
| <ul><li>Content Standards:</li><li>CCSS.8.G.9. Know the formulas for the volumes</li></ul>  | <ul> <li>Area, surface area and volume have applications in<br/>real world situations.</li> </ul>   | <ul> <li>How will the volume change if one<br/>dimension is changed?</li> </ul>   |
| of cones, cylinders, and spheres and use them to solve real-world and mathematical problems.  | <ul> <li>Different 3-dimensional figures can have the same<br/>volume even if the dimensions are not all the same.</li> </ul>   | <ul> <li>How does understanding two-dimensional<br/>figures help find the volume of three-<br/>dimensional figures?</li> </ul>  |
| <ul> <li>CCSS.MP1 Make sense of problems and</li> </ul>   | Acquisitio  | n   |
| <ul> <li>persevere in solving them.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP6 Attend to precision</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul> | <ul> <li>Students will understand</li> <li>volume of some solid figures is calculated using the area of the base and its height.</li> <li>connection between finding volume of one base vs. two base figures.</li> <li>formulas for finding volume of cones, cylinders, and spheres.</li> </ul> | <ul> <li>Students will be skilled at</li> <li>calculating volume of cones, cylinders, and spheres using appropriate formulas and units.</li> <li>using volume formulas to solve real-world problems.</li> </ul> |
| Used in Content Area Standards 21st Century Skills  |   | 21 <sup>st</sup> Century Skills   |
|   |   | Technology Literacy   |
|   |   | Critical Thinking   |

| Stage 2 - Evidence   |  |
|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Accelerated Mathematics - Grade 7 Unit 8: Statistics

# ESTABLISHED GOALS:

Students will continue their study of mathematics in the area of data and problem solving. In this unit, students will gain a deeper understanding of statistics, by analyzing and interpreting data from real-world problems.

### Content Standards:

- CCSS.7.SP.1 Understand that statistics can be used to gain information about a population by examining a sample of the population; generalizations about a population from a sample are valid only if the sample is representative of that population. Understand that random sampling tends to produce representative samples and support valid inferences.
- CCSS.7.SP.2. Use data from a random sample to draw inferences about a population with an unknown characteristic of interest. Generate multiple samples (or simulated samples) of the same size to gauge the variation in estimates or predictions.
- CCSS.7.SP.3. Informally assess the degree of visual overlap of two numerical data distributions with similar variabilities, measuring the difference between the centers by expressing it as a multiple of a measure of variability.

# **Stage 1 Desired Results**

# Students will be able to independently use their learning to...

- analyze and interpret data from real-world situations.
- understand when real-life data is misleading

# Meaning

Transfer

# **ENDURING UNDERSTANDINGS**

- A statistical question anticipates variability in the data related to the question and accounts for it in the answers.
- A set of data collected to answer a statistical question has a distribution, which can be described by its center, spread, and overall shape.

# ESSENTIAL QUESTIONS

 How do you interpret data from statistical representations?

# Acquisition

## Students will understand...

- measure of central tendency: mean, median, mode
- dispersion of data is the spread of data
- the less variation a set has the closer the numbers are to each other.
- random sampling gives unbiased data.
- a valid inference is a prediction based on a random sample.

- creating data with a specific mode, median and mean.
- identifying when a measure of central tendency would not be an accurate reflection of the data.
- using data from a random sample to draw inferences about a population.
- analyzing data to make a prediction.
- displaying two samples of data in a box plot to illustrate variability.

| CCSS.7.SP.4. Use measures of center and measures of        | <ul> <li>creating a line plot to compare two</li> </ul> |
|--|---|
| variability for numerical data from random samples to draw | samples.  |
| informal comparative inferences about two populations.     |   |
| CCSS.MP3 Construct viable arguments and critique the       |   |
| reasoning of others.                                       |   |
| CCSS.MP4 Model with mathematics.                           |   |
| CCSS.MP5 Use appropriate tools strategically.              |   |
| Used in Content Area Standards                             | 21 <sup>st</sup> Century Skills                         |
|  | <ul> <li>Communication</li> </ul>                       |
|  | <ul> <li>Critical Thinking</li> </ul>                   |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Accelerated Mathematics - Grade 7 Unit 9: Probability

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|--------|-------|-------------------|-------------|-----|
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Students will continue their study of mathematics in the area of data and problem solving. In this unit, students will gain a deeper understanding of probability to solve real-world problems involving chance.

### Content Standards:

- CCSS.7.SP.C.5 Understand that the probability of a chance event is a number between 0 and 1 that expresses the likelihood of the event occurring.
   Larger numbers indicate greater likelihood. A probability near 0 indicates an unlikely event, a probability around 1/2 indicates an event that is neither unlikely nor likely, and a probability near 1 indicates a likely event.
- CCSS.7.SP.C.6 Approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency, and predict the approximate relative frequency given the probability.
- CCSS.7.SP. C.7 Develop a probability model and use it to find probabilities of events. Compare probabilities from a model to observed frequencies; if the agreement is not good, explain possible sources of the discrepancy.

# **Stage 1 Desired Results**

# Transfer

Students will be able to independently use their learning to...

solve real-world problems involving chance.

# Meaning

# ENDURING UNDERSTANDINGS

- Probability is used to predict the likelihood of an event and make decisions.
- Key to valuable experimental probability is good data.

# **ESSENTIAL QUESTIONS**

- What makes a game fair?
- How are probabilities used to make everyday decisions?

## **Acauisition**

## Students will understand...

- probability is the likelihood that something will happen.
- experimental probability is based on someone's results.
- theoretical probability is based on what exists.
- possible outcomes and favorable outcomes.
- equally likely outcomes are results that have the same probability of happening.
- tree diagrams as a method for finding all possible outcomes.
- probability of an outcome ranges between 0 (never happening) and 1 (always happening).
- compound probability is used when more than one event is happening.

- performing an activity, recording results and calculating experimental probability.
- comparing different experimental probabilities for the same activity and explaining the difference.
- making predictions based on probability.
- creating tree diagrams to find total possible outcomes.
- expressing probability as fractions and percents.
- identifying an event that would have a probability of zero.
- identifying an event that would have a probability of one.

| <ul> <li>CCSS.7.SP.C.8 Find probabilities of compound events using organized lists, tables, tree diagrams, and simulation.</li> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> <li>CCSS.MP4 Model with mathematics.</li> </ul> | <ul> <li>probability is either independent or<br/>dependent.</li> </ul> | calculating compound probability of both dependent and independent events. |
|---|---|--|
| Used in Content Area Standards  |   | 21 <sup>st</sup> Century Skills  |
|   |   | Communication  |
|   |   | Critical Thinking  |
|   |   |  |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

Title of Curriculum: 8th Grade Math

| Unit Name   | What (content, vocab)  | Why (enduring understandings)   | How (skills)  |
|---|--|---|---|
| Unit 1: Numbers & Operations:<br>The Real Number System | <ul> <li>Rational numbers</li> <li>Irrational numbers</li> <li>Radicals (square and cube roots)</li> <li>Exponents</li> <li>Scientific notation</li> <li>Compare real numbers</li> </ul> | <ul> <li>Real numbers include rational<br/>and irrational numbers which can<br/>be approximated using rational<br/>numbers.</li> <li>Real numbers can be represented<br/>using mathematical symbols.</li> </ul> | <ul><li>Approximate rational numbers</li><li>Compare and order rational and</li></ul>   |
| Unit 2: Algebraic Thinking: Solving Equations           | <ul> <li>Equivalent expressions</li> <li>Equations</li> <li>Inverse operations</li> <li>Rational number coefficients</li> </ul>  | Mathematical properties and inverse operations can be applied to efficiently solve equations and interpret solutions.   | <ul> <li>Solve two-step equations, with integers using inverse operations</li> <li>Solve multi-step equations with variables on both sides</li> <li>Simplify expressions</li> <li>Solve equations with rational number coefficients</li> <li>Apply mathematics to problem solving situations</li> </ul>   |
| Unit 3: Algebraic Thinking: Linear Functions            | <ul> <li>Linear and nonlinear functions</li> <li>Slope</li> <li>y-intercept</li> <li>Proportional relationships</li> <li>Tables, graphs, equations</li> </ul>                            |   | <ul> <li>Determine if a relationship is linear or nonlinear</li> <li>Write and interpret linear equations in slope intercept (y=mx+b) form</li> <li>Analyze and translate information for linear relationships between tables, graphs and equations</li> <li>Find and interpret the rate of change (slope, m) using table, graph, and equation</li> </ul> |

| Unit 4: Algebraic Thinking: Linear            | Graphs of Linear systems   | <ul> <li>Solutions to linear systems can be</li> </ul>  | <ul> <li>Find and interpret the initial value (y-intercept, b) using table, graph, and equation</li> <li>Represent and compare proportional relationships from different representations</li> <li>Solve linear systems using graphing</li> </ul>   |
|---|--|---|--|
| Systems Chinking: Linear                      | <ul> <li>Solutions (intersection point, infinite, none)</li> </ul>   | used to represent real world phenomena.   | <ul> <li>Solve linear systems using graphing methods</li> <li>Determine whether lines will be parallel or intersecting</li> <li>Interpret the solution to a linear system in real world situations</li> </ul>  |
| Unit 5: Algebraic Thinking:<br>Bivariate Data | <ul> <li>Scatterplots</li> <li>Association (Correlation)</li> <li>Best fit line</li> <li>Qualitative graphs and descriptions</li> </ul>              | <ul> <li>Bivariate data can be graphed to show correlation.</li> <li>Linear data can be modeled with an equation to answer questions and make predictions</li> <li>Functions can model relationships between quantities.</li> </ul> | <ul> <li>Construct and interpret scatter plots to investigate patterns of association between two quantities</li> <li>Describe patterns of association for two quantities. (positive, negative, no association)</li> <li>Create and use lines of best fit to make and evaluate predictions</li> <li>Interpret the relationships between two variables on qualitative graphs</li> </ul> |
| Unit 6: Geometry:<br>Transformations          | <ul> <li>Transformations:         dilations, translations,         reflections, rotations</li> <li>Congruence</li> <li>Similarity</li> </ul>         | Transformations can result in congruent or similar figures.   | <ul> <li>Transform polygons using dilations, translations, reflections, and rotations</li> <li>Identify coordinates of transformed figures</li> <li>Describe sequence of transformations that result in congruent or similar figures</li> </ul>  |
| Unit 7: Geometry: Angles                      | <ul> <li>Triangle angle relationships</li> <li>Angles formed by parallel lines cut by a transversal</li> <li>Interior and exterior angles</li> </ul> | <ul> <li>Special angle relationships are formed by triangles and parallel lines cut by a transversal.</li> <li>Angle relationships can be used to determine missing angle measures in diagrams.</li> </ul>                          | Find angle measurements using properties of similar figures, exterior and interior angles, and parallel lines cut by a transversal   |

| Unit 8: Geometry: Pythagorean<br>Theorem | <ul> <li>Pythagorean Theorem</li> <li>Converse of the         Pythagorean Theorem     </li> <li>Squares and square roots</li> <li>Distance on the         coordinate plane     </li> </ul> | Right triangles have a special relationship among the side lengths which can be represented by a model and a formula.  | <ul> <li>Informally prove the Pythagorean Theorem</li> <li>Determine if a triangle is a right triangle using its converse</li> <li>Apply the Pythagorean Theorem to find missing triangle side lengths</li> <li>Apply the Pythagorean Theorem to solve problems</li> <li>Apply the Pythagorean Theorem to find distance between two points on the coordinate plane</li> </ul> |
|--|--|--|---|
| Unit 9: Geometry: Volume                 | <ul> <li>Volume and Surface area of right prisms and pyramids</li> <li>Nets</li> <li>Volume of Cylinder, Cones and Spheres</li> </ul>  | <ul> <li>Everyday objects have a variety of attributes, each of which can be measured in many ways.</li> <li>Area, surface area and volume have applications in real world situations.</li> <li>Different 3-dimensional figures can have the same volume even if the dimensions are not all the same.</li> </ul> | <ul> <li>Calculate volume of triangular prisms and pyramids using appropriate formulas and units</li> <li>Calculate surface area of triangular prisms and pyramids</li> <li>Calculate volumes of cones, cylinders, and spheres using appropriate formulas and units</li> <li>Use volume formulas to solve real world problems</li> <li>Draw nets of solid figures</li> </ul>  |

# Windham School District Curriculum Mathematics - Grade 8

# **Unit 1: Numbers & Operations - The Real Number System**

| Stage 1 Desired Results  |  |                  |  |
|--|--|------------------|--|
| ESTABLISHED GOALS:   | Transfer   |                  |  |
| Students will continue their study of mathematics in the area of the | dents will be able to independently use their learning to              |                  |  |
| real number system. In this unit, students will gain a deeper        | understand the different types of numbers within the real number syste | :ms              |  |
| understanding of rational and irrational numbers.                    | connect those understandings to numbers they see in their daily life.  |                  |  |
|  | Meaning  |                  |  |
| Content Standards:   | OURING UNDERSTANDINGS ESSENTIAL QUESTIONS                              |                  |  |
| • CCSS.8.NS.1. Know that numbers that are not rational are           | Real numbers include rational and irrational • When are numbers        | exact?           |  |
| called irrational. Understand informally that every number has       | numbers which can be approximated using   • How can mathematic         | cs make really   |  |
| a decimal expansion; for rational numbers show that the              | rational numbers. large or really small r                              | numbers          |  |
| decimal expansion repeats eventually, and convert a decimal          | Real numbers can be represented using understandable?                  |                  |  |
| expansion that repeats eventually into a rational number.            | mathematical symbols.  |                  |  |
| CCSS.8.NS.2. Use rational approximations of irrational               | Acquisition  |                  |  |
| numbers to compare the size of irrational numbers, locate            | dents will understand Students will be skilled at.                     |                  |  |
| them approximately on a number line diagram, and estimate            | real numbers are made up of rational and • determining whethe          | r a number is    |  |
| the value of expressions (e.g., $\pi 2$ )                            | irrational numbers irrational or rational.                             |                  |  |
| CCSS.8.EE.1. Know and apply the properties of integer                | different subsets of the real number system • approximating irration   | onal numbers.    |  |
| exponents to generate equivalent numerical expressions.              | are comparable. • comparing and order                                  | ing rational and |  |
| CCSS.8.EE.2. Use square root and cube root symbols to                | finding perfect square roots help to estimate irrational numbers.      |                  |  |
| represent solutions to equations of the form x 2 = p and x 3 =       | the values of square roots that are not   • finding perfect square     | e and cube       |  |
| p, where p is a positive rational number. Evaluate square roots      | perfect. roots.  |                  |  |
| of small perfect squares and cube roots of small perfect cubes       | radical symbols indicate square or cube roots. • writing equivalent ex | pressions using  |  |
| Know that √2 is irrational.  | equivalent expressions can be written using integer exponents.         |                  |  |
| • CCSS.8.EE.3. Use numbers expressed in the form of a single         | integer exponents.  • investigating number                             | rs written in    |  |
| digit times a whole-number power of 10 to estimate very              | very large or very small numbers can be scientific notation            |                  |  |
| large or very small quantities.                                      | written using scientific notation.                                     |                  |  |
| CCSS.MP2 Reason abstractly and quantitatively.                       |  |                  |  |

| <ul> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP6 Attend to precision.</li> </ul>      |   |            |
|---|---|------------|
| <ul> <li>CCSS.MP7 Look for and make use of structure.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul> |   |            |
| Used in Content Area Standards  | 21st Centu  | ıry Skills |
|   | <ul><li>Communication</li><li>Technology Litera</li></ul> | асу        |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

# Windham School District Curriculum Mathematics - Grade 8

# **Unit 2: Algebraic Thinking - Solving Equations**

| Stage 1 Desired Results                        |  |  |  |
|--|--|--|--|
| ESTABLISHED GOALS:                             | Transfer   |  |  |
| Students will continue their study of          | Students will be able to independently use their lear              | ning to  |  |
| mathematics in the area of algebraic thinking. | <ul> <li>understand how mathematical operations are in</li> </ul>  | versely connected  |  |
| In this unit, students will gain a deeper      | <ul> <li>use equations to solve real world problems.</li> </ul>    |  |  |
| understanding of solving equations.            |  | Meaning  |  |
|  | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS  |  |
| Content Standards:                             | <ul> <li>Mathematical properties and inverse operations</li> </ul> | Are all things created equal?  |  |
| • CCSS.8.EE.7. Solve linear equations in       | can be applied to efficiently solve equations and                  | What situations can be modeled using equations?                                |  |
| one variable.                                  | interpret solutions.   | How can two equations look different but be the same?                          |  |
| CCSS.MP2 Reason abstractly and                 | A  | Acquisition  |  |
|  | Students will understand   | Students will be skilled at  |  |
| CCSS.MP3 Construct viable arguments            | <ul> <li>an equation involves inverse operations and</li> </ul>    | solving two-step equations with integers using inverse                         |  |
| and critique the reasoning of others.          | maintaining balance.   | operations.  |  |
| CCSS.MP4 Model with mathematics.               | <ul> <li>equivalent expressions are created by</li> </ul>          | <ul> <li>solving multi-step equations with variables on both sides.</li> </ul> |  |
| CCSS.MP7 Look for and make use of              | properties of mathematics.   | simplifying expressions  |  |
| structure.                                     | <ul> <li>rational number coefficients</li> </ul>                   | <ul> <li>solving equations with rational number coefficients.</li> </ul>       |  |
|  |  | <ul> <li>applying mathematics to problem solving situations.</li> </ul>        |  |
| Used in Content Area Standards                 |  | 21 <sup>st</sup> Century Skills  |  |
|  |  | Critical Thinking  |  |
|  |  | Communication  |  |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 8 Unit 3: Algebraic Thinking - Linear Functions

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|-----|-----|------|------|------|----|
|     |     |      |      |      |    |

Students will continue their study of mathematics in the area of algebraic thinking. In this unit, students will gain a deeper understanding of linear relationships between two variables.

### Content Standards:

- CCSS.8.EE.5. Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways.
- CCSS.8.EE.6. Use similar triangles to explain why
  the slope m is the same between any two distinct
  points on a nonvertical line in the coordinate
  plane; derive the equation y = mx for a line
  through the origin and the equation y = mx + b
  for a line intercepting the vertical axis at b.
- CCSS.8.F.1. Understand that a function is a rule that assigns to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and corresponding output.
- CCSS.8.F.2. Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).

# **Stage 1 Desired Results**

# Students will be able to independently use their learning to...

- model real world situations using graphs, tables, and equations.
- connect linear functions to future algebraic function understandings.

# Meaning

Transfer

## ENDURING UNDERSTANDINGS

- Proportional relationships can be represented as a linear equation that passes through the origin.
- Linear relationships can be represented using tables, graphs and equations.
- Linear functions model relationships between quantities.

# **ESSENTIAL QUESTIONS**

- How can functions represent real world phenomena?
- When do two variables represent a linear relationship?

# **Acquisition**

# Students will understand...

- linear and nonlinear functions can be shown using different representations.
- proportional and nonproportional relationships.
- connections between verbal descriptions and graphical representations of linear functions.
- slope and y-intercept of linear functions.

- determining if a relationship is linear or nonlinear.
- writing and interpreting linear equations in slope intercept (y = mx + b) form.
- analyzing and translating information for linear relationships between tables, graphs and equations.
- finding and interpreting the rate of change (slope, m) using tables, graphs, and equations.

|   | <ul><li>Technology Literacy</li><li>Critical Thinking</li></ul>   |
|---|---|
| Used in Content Area Standards  | 21st Century Skills   |
| <ul> <li>CCSS.8.F.4. Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two (x, y) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values.</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically.</li> <li>CCSS.MP7 Look for and make use of structure.</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning</li> <li>Used in Content Area Standards</li> </ul> | ,   |
| <ul> <li>CCSS.8.F.3. Interpret the equation y = mx + b as a<br/>defining a linear function, whose graph is a<br/>straight line; give examples of functions that are<br/>not linear.</li> </ul>  | <ul> <li>finding and interpreting the initial value (y-intercept, b) using tables, graphs, and equations.</li> <li>representing and comparing proportional</li> </ul> |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | Other Evidence: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 8 Unit: Algebraic Thinking - Linear Systems

| Stage 1 Desired Results                                     |  |   |  |
|---|--|---|--|
| ESTABLISHED GOALS:  | Transfer   |   |  |
| Students will continue their study of mathematics in        | Students will be able to independently use their le                  | earning to  |  |
| the area of algebraic thinking. In this unit, students will | <ul> <li>model multiple linear relationships and interpre</li> </ul> | et their intersection point.  |  |
| gain a deeper understanding of the relationships            | Med  | aning   |  |
| between different linear scenarios.                         | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS   |  |
|   | <ul> <li>Solutions to linear systems can be used to</li> </ul>       | What can happen when you have two lines?                            |  |
| Content Standards:  | represent real world phenomena.                                      | How does the intersection of a linear system                        |  |
| CCSS.8.EE.8. Analyze and solve pairs of                     |  | model real world phenomena?   |  |
| simultaneous linear equations.                              |  | Acquisition   |  |
| CCSS.MP1 Make sense of problems and persevere               | Students will understand   | Students will be skilled at   |  |
| in solving them.  | <ul> <li>lines may or may not intersect.</li> </ul>                  | • solving linear systems using graphing methods.                    |  |
| CCSS.MP4 Model with mathematics.                            | <ul> <li>graphs of Linear systems</li> </ul>                         | <ul> <li>determining whether lines will be parallel or</li> </ul>   |  |
| CCSS.MP5 Use appropriate tools strategically                | <ul> <li>solutions (intersection point, infinite, none)</li> </ul>   | intersecting.   |  |
|   |  | <ul> <li>interpreting the solution to a linear system in</li> </ul> |  |
|   |  | real world situations.  |  |
| Used in Content Area Standards                              |  | 21st Century Skills   |  |
|   |  | Technology Literacy   |  |
|   |  | Critical thinking   |  |
|   |  |   |  |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 8 Unit 5: Algebraic Thinking - Bivariate Data

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|-----|-----|-------|------|--|
|     |     |       |      |  |

Students will continue their study of mathematics in the area of algebraic thinking. In this unit, students will gain a deeper understanding of how data can be represented using scatterplots.

## Content Standards:

- CCSS.8.SP.1. Construct and interpret scatter plots for bivariate measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering, outliers, positive or negative association, linear association, and nonlinear association. CCSS.8.SP.2. Know that straight lines are widely used to model relationships between two quantitative variables. For scatter plots that suggest a linear association, informally fit a straight line, and informally assess the model fit by judging the closeness of the data points to the line.
- CCSS.8.SP.3. Use the equation of a linear model to solve problems in the context of bivariate measurement of data, interpreting the slope and interpret.
- CCSS.8.SP.4. Understand that patterns of association can also be seen in bivariate categorical data by displaying frequencies and relative frequencies in a two-way table. Construct and interpret a two-way table summarizing data on two categorical variables collected from the same subjects. Use relative frequencies calculated for rows or columns to describe possible association between the two variables.

# **Stage 1 Desired Results**

# Students will be able to independently use their learning to...

interpret and model data using scatterplots.

# Meaning

Transfer

# ENDURING UNDERSTANDINGS

- Bivariate data can be graphed to show correlation.
- Linear data can be modeled with an equation to answer questions and make predictions
- Functions can model relationships between quantities.

## ESSENTIAL QUESTIONS

 How can mathematics be used to model and make predictions for real world phenomena?

# **Acquisition**

# Students will understand...

- scatter plots show relationships between two variables.
- some data can be modeled using a linear equation.
- linear models can be used to make predictions about data.
- qualitative graphs tell a story.

- constructing and interpreting scatter plots to investigate patterns of association between two quantities.
- describing patterns of association for two quantities.
- creating and using lines of best fit to make and evaluate predictions.
- interpreting the relationships between two variables on qualitative graphs

| <ul> <li>CCSS.MP 3 Construct viable arguments and critique the<br/>reasoning of others.</li> </ul> |   |
|--|---|
| CCSS.MP 4 Model with mathematics.  |   |
| Used in Content Area Standards   | 21 <sup>st</sup> Century Skills         |
|  | Communication                           |
|  | <ul> <li>Technology Literacy</li> </ul> |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 8 Unit 6: Geometry - Transformations

| Stage   | 1 Desired Results   |   |
|---|---|---|
| ESTABLISHED GOALS:  |   | Transfer  |
| Students will continue their study of mathematics in the area of geometry   | Students will be able to independentl   | y use their learning to   |
| In this unit, students will gain a deeper understanding of congruence and   | <ul> <li>determine if figures are congruer</li> </ul>   | nt or similar using the coordinate plane.   |
| similarity on the coordinate plane.   |   | Meaning   |
|   | ENDURING UNDERSTANDINGS   | ESSENTIAL QUESTIONS   |
| Content Standards:  | <ul> <li>Transformations can result in</li> </ul>   | <ul> <li>What movements preserve or change</li> </ul>   |
| • CCSS.8.G.1. Verify experimentally the properties of rotations,  | congruent or similar figures.   | shapes?   |
| reflections, and translations.  |   | • How can a house fit on a piece of paper?  |
| • CCSS.8.G.2. Understand that a two-dimensional figure is congruent to  |   | Acquisition   |
| <ul> <li>another if the second can be obtained from the first by a sequence or rotations, reflections, and translations; given two congruent figures, describe a sequence that exhibits the congruence between them.</li> <li>CCSS.8.G.3. Describe the effect of dilations, translations, rotations, and reflections on two-dimensional figures using coordinates.</li> <li>CCSS.8.G.4. Understand that a two-dimensional figure is similar to another if the second can be obtained from the first by a sequence or rotations, reflections, translations, and dilations; given two similar two-dimensional figures, describe a sequence that exhibits the similarity between them</li> <li>CCSS.MP1 Make sense of problems and persevere in solving them.</li> <li>CCSS.MP6 Attend to precision</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul> | <ul> <li>transformations as dilations,<br/>translations, reflections, and<br/>rotations</li> <li>transformations preserve<br/>congruence of polygons, lines,</li> </ul> | <ul> <li>transforming polygons using dilations, translations, reflections, and rotations.</li> <li>identifying coordinates of transformed figures.</li> <li>describing sequences of transformations that result in congruent or similar figures.</li> </ul> |
| Osea in Content Area Standards  |   | 21st Century Skills  ■ Critical Thinking  |
|   |   | - 5531  |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 8 Unit 7: Geometry - Angles

| Stage 1 Desired Results  |  |  |  |
|--|--|--|--|
| ESTABLISHED GOALS:   | Transfer   |  |  |
| Students will continue their study of mathematics in             | Students will be able to independently use their lea               | arning to  |  |
| the area of geometry. In this unit, students will gain a         | <ul> <li>use angle relationships in more advanced study</li> </ul> | of Geometry.   |  |
| deeper understanding of angle relationships.                     | • use the relationships between angles and lines                   | to solve real life problems.                                       |  |
|  | Med  | aning  |  |
| Content Standards:   | ENDURING UNDERSTANDINGS  | ESSENTIAL QUESTIONS  |  |
| • CCSS.8.G.5. Use informal arguments to establish                | <ul> <li>Special angle relationships are formed by</li> </ul>      | How do intersecting lines create angle                             |  |
| facts about the angle sum and exterior angle of                  | triangles and parallel lines cut by a transversal.                 | relationships?   |  |
| triangles, about the angles created when parallel                | Angle relationships can be used to determine                       |  |  |
| lines are cut by a transversal, and the angle-angle              | missing angle measures in diagrams.                                |  |  |
| criterion for similarity of triangles.                           |  | isition  |  |
| CCSS.MP1 Make sense of problems and persevere                    | Students will understand   | Students will be skilled at  |  |
| in solving them.   | <ul> <li>angle relationships between exterior and</li> </ul>       | <ul> <li>finding angle measurements using properties of</li> </ul> |  |
| CCSS.MP6 Attend to precision                                     | interior triangle angles, similar triangles, and                   | similar figures, exterior angles, interior angles,                 |  |
| <ul> <li>CCSS.MP7 Look for and make use of structure.</li> </ul> | parallel lines cut by a transversal.                               | and parallel lines cut by a transversal.                           |  |
|  |  |  |  |
| Used in Content Area Standards                                   |  | 21 <sup>st</sup> Century Skills                                    |  |
|  |  | Critical thinking  |  |
|  |  | Communication  |  |

| Stage 2 - Evidence                          |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence     |  |  |
| ASSESSMENT: Written Assessments or Projects |  |  |
|   | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 8 Unit 8: Geometry - Pythagorean Theorem

|   | , , ,   |   |  |
|---|---|---|--|
|   | Stage 1 Desired Results                                     |   |  |
| ESTABLISHED GOALS:  |   | Transfer  |  |
| Students will continue their study of mathematics in Students will be able to independently use the |   | eir learning to   |  |
| the area of geometry . In this unit, students will gain a   | <ul> <li>apply pythagorean theorem to future geo</li> </ul> | metric concepts   |  |
| deeper understanding of problem solving using the   | <ul> <li>use pythagorean theorem and its convers</li> </ul> | e to solve real-world problems.   |  |
| Pythagorean Theorem.  |   | Meaning   |  |
|   | ENDURING UNDERSTANDINGS                                     | ESSENTIAL QUESTIONS   |  |
| Content Standards:  | Right triangles have a special relationship                 | How can right triangle relationships model real world                         |  |
| • CCSS.8.G.6. Explain a proof of the Pythagorean  | among the side lengths which can be                         | phenomena?  |  |
| Theorem and its converse.   | represented by a model and a formula.                       | How can you use the Pythagorean Theorem to solve                              |  |
| • CCSS.8.G.7. Apply the Pythagorean Theorem to  |   | everyday problems?  |  |
| determine unknown side lengths in right triangles   | Acquisition   |   |  |
| in real-world and mathematical problems in two  | Students will understand                                    | Students will be skilled at   |  |
| and three dimensions.   | Pythagorean Theorem equates the sum                         | • informally proving the Pythagorean Theorem (a <sup>2</sup> + b <sup>2</sup> |  |
| CCSS.8.G.8. Apply the Pythagorean Theorem to  | of the squares of the legs to the square of                 |   |  |
| find the distance between two points in a   | the hypotenuse in right triangles.                          | <ul> <li>determining if a triangle is a right triangle using its</li> </ul>   |  |
| coordinate system.  | converse of the Pythagorean Theorem                         | converse.   |  |
| CCSS.MP2 Reason abstractly and quantitatively.  | can be used to determine whether a                          | applying the Pythagorean Theorem to find missing                              |  |
| <ul> <li>CCSS.MP4 Model with mathematics.</li> </ul>  | given triangle is a right triangle.                         | triangle side lengths.  |  |
| CCSS.MP6 Attend to precision.   |   | applying the Pythagorean Theorem to solve                                     |  |
|   |   | problems.   |  |
|   |   | applying the Pythagorean Theorem to find distance                             |  |
|   |   | between two points on the coordinate plane.                                   |  |
| Used in Content Area Standards  |   | 21st Century Skills   |  |
|   |   | Critical Thinking   |  |
|   |   | Communication   |  |

| Stage 2 - Evidence                          |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence     |  |  |
| ASSESSMENT: Written Assessments or Projects |  |  |
|   | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Mathematics - Grade 8 Unit 9: Geometry - Volume

| Stage 1 Desired Results  |   |   |
|--|---|---|
| ESTABLISHED GOALS:   | Transfe   | er  |
| Students will continue their study of mathematics  | Students will be able to independently use their learning   | to  |
| in the area of geometry. In this unit, students will   | <ul> <li>solve real world problems involving volume and surfa</li> </ul>                          | ice area.   |
| gain a deeper understanding of solving real world  | Meanin  | ng  |
| problems involving geometric solids.   | ENDURING UNDERSTANDINGS   | ESSENTIAL QUESTIONS   |
|  | <ul> <li>Everyday objects have a variety of attributes, each of</li> </ul>                        | Will the size of a container indicate its   |
| Content Standards:   | which can be measured in many ways.   | contents?   |
| <ul> <li>CCSS.7.G.6. Solve real-world and<br/>mathematical problems involving area,</li> </ul> | <ul> <li>Area, surface area and volume have applications in<br/>real world situations.</li> </ul> | <ul> <li>How will the volume change if one dimension<br/>is changed?</li> </ul>     |
| volume and surface area of two- and three  | Different 3-dimensional figures can have the same   | How does understanding two-dimensional  |
| dimensional objects composed of triangles,   | volume even if the dimensions are not all the same.   | figures help find the volume of three-  |
| quadrilaterals, polygons, cubes, and right   |   | dimensional figures?  |
| prisms.  | Acquisit  | ion   |
| CCSS.8.G.9. Know the formulas for the  |   | Students will be skilled at   |
| volumes of cones, cylinders, and spheres and   | <ul> <li>volume of some solid figures is calculated using the</li> </ul>                          | <ul> <li>calculating volume of triangular prisms and</li> </ul>                     |
| use them to solve real-world and   | area of the base and its height.  | pyramids using appropriate formulas and units.                                      |
| <ul><li>mathematical problems.</li><li>CCSS.MP1 Make sense of problems and</li></ul>           | <ul> <li>connection between finding volume of one base vs.</li> <li>two base figures.</li> </ul>  | <ul> <li>calculating surface area of triangular prisms<br/>and pyramids.</li> </ul> |
| persevere in solving them.   | <ul> <li>formulas for finding volume of cones, cylinders, and</li> </ul>                          | <ul> <li>calculating volumes of cones, cylinders, and</li> </ul>                    |
| <ul> <li>CCSS.MP4 Model with mathematics.</li> </ul>   | spheres.  | spheres using appropriate formulas and units  |
| <ul> <li>CCSS.MP6 Attend to precision</li> </ul>   | <ul> <li>a net is a two-dimensional drawing of a three-</li> </ul>                                | <ul> <li>using volume formulas to solve real world</li> </ul>                       |
| <ul> <li>CCSS.MP8 Look for and express regularity in</li> </ul>                                | dimensional figure.   | problems.   |
| repeated reasoning.  | <ul> <li>characteristics of right prisms and pyramids.</li> </ul>                                 | <ul> <li>drawing nets of solid figures.</li> </ul>                                  |
|  | <ul> <li>surface area is the sum of the areas of the faces and</li> </ul>                         |   |
|  | bases in a three dimensional figure.  |   |

| Used in Content Area Standards | 21st Century Skills |
|--------------------------------|---------------------|
|                                | Critical Thinking   |
|                                | Communication       |
|                                |                     |

| Stage 2 - Evidence                          |  |  |
|---|--|--|
| Evaluative Criteria Assessment Evidence     |  |  |
| ASSESSMENT: Written Assessments or Projects |  |  |
|   | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# <u>Title of Curriculum:</u> 8th grade Algebra 1

| Unit Name   | What (content, vocab)  | Why (enduring understandings)  | How (skills)   |
|---|--|--|--|
| Unit 1: Algebraic Expressions and Functions: Foundations of Functions and Expressions | <ul> <li>Functions</li> <li>Representations of relations</li> <li>Function notation</li> <li>Translations between verbal and algebraic expressions</li> <li>Mathematical properties</li> <li>Order of operations</li> <li>Domain and range of functions</li> </ul> | <ul> <li>Relations and functions can represent real world phenomena</li> <li>Variables represent unknown numbers or values that can change</li> </ul>  | <ul> <li>Translate between verbal and algebraic expressions</li> <li>Perform order of operations</li> <li>Determine whether a relation is a function</li> <li>Evaluate a function in function notation</li> <li>Apply mathematical properties to simplify expressions</li> <li>Recognize and evaluate functions</li> <li>Identify and use the algebraic properties</li> <li>Write function rules from tables and word problems</li> <li>Determine domain and range of various functions</li> </ul> |
| Unit 2: Algebraic Expressions and Functions: Exponential Expressions and Functions    | <ul> <li>Properties of exponents</li> <li>Scientific notation</li> <li>Geometry applications</li> <li>Exponential Functions</li> </ul>   | <ul> <li>Very large and small numbers can be represented efficiently using scientific notation</li> <li>Exponent properties can be proven through expansion</li> <li>Exponential functions model real world phenomena.</li> </ul>        | <ul> <li>Use the rules of exponents to simplify monomials</li> <li>Apply geometric formulas to problems involving monomials</li> <li>Write large or small numbers in scientific notation</li> <li>Perform operations on numbers expressed in scientific notation</li> <li>Graph exponential functions</li> </ul>   |
| Unit 3: Algebraic Equations:<br>Solving Equations and Inequalities                    | <ul> <li>Literal and algebraic equations</li> <li>Absolute value</li> <li>Percents</li> <li>Proportions</li> <li>Inequalities</li> <li>Compound inequalities</li> <li>Absolute value inequalities</li> </ul>   | <ul> <li>Operations performed on one side of an equation must be performed on the other side(s) in order to preserve the equality.</li> <li>Solutions to inequalities represent a range of values rather than a single value.</li> </ul> | Write and solve multi-step equations with rational coefficients  |

| Unit 4: Functions:<br>Linear Relationships       | <ul> <li>Slope</li> <li>Forms of linear equations</li> <li>Arithmetic sequences</li> <li>Direct variation</li> <li>Linear representations</li> <li>Parallel and perpendicular lines</li> <li>Properties of horizontal and vertical lines</li> </ul> | <ul> <li>Linear relationships have a constant rate of change.</li> <li>Tables, graphs, and equations are all ways of representing functions and real world phenomena.</li> <li>Slope can be referenced in many different ways.</li> </ul> | <ul> <li>Solve literal equations</li> <li>Write and solve proportions, including with binomials in numerator and denominator</li> <li>Write and Solve application percent problems</li> <li>Solve absolute value inequalities</li> <li>Calculate slope between two points</li> <li>Determine the slope of a line, given an equation, table, or graph</li> <li>Find and determine intercepts</li> <li>Graph linear equations</li> <li>Determine whether lines are parallel, perpendicular, or neither</li> <li>Write linear equations in slope-intercept, standard and point-slope form</li> <li>Create and interpret linear equations from real world data</li> <li>Write a rule given an arithmetic sequence</li> </ul> |
|--|---|---|--|
| Unit 5: Functions: Bivariate Data (Scatterplots) | <ul> <li>Scatterplots</li> <li>Line of best fit</li> <li>Correlation</li> </ul>   | Scatter plots can model data,<br>and be used to make<br>predictions   | <ul> <li>Represent bivariate data with scatterplots</li> <li>Interpret scatterplots</li> <li>Calculate the line of best fit</li> <li>Use the line of best fit to find starting point represented by the y-intercept; to describe what the slope means; and to fin the values at a particular point including outside the given graph</li> <li>Determine if there is a correlation between bivariate data</li> <li>Make predictions based on the line of best fit</li> </ul>  |
| Unit 6: Algebraic Equations:<br>Linear Systems   | <ul><li>Systems of equations</li><li>Systems of inequalities</li><li>Linear inequalities</li></ul>  | <ul> <li>There is more than one way to<br/>solve a system of equations<br/>and students should</li> </ul>   | <ul> <li>Write and solve linear systems using multiple methods</li> <li>Distinguish if a system of equations has</li> </ul>  |

|  |  | determine the most efficient method.  Systems of equations with two unknowns can be used to solve real world problems. | <ul> <li>one solution, no solution, or infinitely many solutions</li> <li>Graph linear inequalities on a coordinate plane</li> <li>Graph systems of linear inequalities on a coordinate plane</li> <li>Create and interpret linear inequalities</li> <li>Model real world situations with systems of equations</li> </ul> |
|--|--|--|---|
| Unit 7: Algebraic Expressions and Equations: Polynomials and Quadratics        | <ul> <li>Standard form and degree</li> <li>Operations with polynomials</li> <li>Factoring polynomials</li> <li>Quadratic equations</li> <li>Geometry applications</li> </ul> | Mathematical properties<br>extend to simplify<br>polynomials.  | <ul> <li>Simplify polynomial expressions</li> <li>Solve quadratic equations by factoring</li> <li>Solve geometric problems involving polynomials</li> <li>Factor quadratics (leading coefficient is 1)</li> <li>Factor polynomials</li> </ul>   |
| Unit 8: Algebraic Expressions and Equations: Radical Expressions and Equations | <ul> <li>Operations with radicals</li> <li>Pythagorean theorem</li> <li>Representations of radicals</li> <li>Radical Equations</li> <li>Extraneous solutions</li> </ul>      | <ul> <li>Radicals represent numbers.</li> <li>In some operations, radicals mimic variables.</li> </ul>                 | <ul> <li>Simplify radicals</li> <li>Add, subtract, multiply, and divide radicals</li> <li>Solve problems involving the Pythagorean theorem</li> <li>Solve radical equations</li> <li>Determine extraneous solutions when solving radical equations</li> </ul>   |

# Windham School District Curriculum Algebra 1 - Grade 8

# **Unit 1: Algebraic Expressions & Function Foundations of Functions and Expressions**

**Stage 1 Desired Results** 

## ESTABLISHED GOALS:

Students will continue their study of mathematics in the areas of algebraic expressions and functions. In this unit, students will gain a deeper understanding of function foundations for algebra.

## Content Standards:

- CCSS.HSF.IF.A.1: Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range.
   If f is a function and x is an element of its domain, then f(x) denotes the output of f corresponding to the input x. The graph of f is the graph of the equation y = f(x).
- CCSS.HSF.IF.A.2: Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.
- CCSS.HSF.IF.B.6: Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.
- CCSS.HSF.IF.C.8: Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.
- CCSS.HSF.IF.B.5: Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.

# Transfer

Students will be able to independently use their learning to...

• connect basic knowledge of functions in the study of advanced functions.

# Meaning

# ENDURING UNDERSTANDINGS

- Relations and functions can represent real world phenomena.
- Variables represent unknown numbers or values that can change.

# **ESSENTIAL QUESTIONS**

- How can relations and functions relate to real world problems?
- How do you use variables, expressions, and equations to model real world problems?

# **Acquisition**

## Students will understand...

- verbal and algebraic expressions.
- order of operations.
- that mathematical properties simplify expressions.
- representations of relations and graphs of relations.
- functions and function notation.
- the domain and range of a function.

- translating between verbal and algebraic expressions.
- performing order of operations.
- determining whether a relation is a function.
- evaluating a function in function notation.
- applying mathematical properties to simplify expressions.
- recognizing and evaluating functions.

| • CCSS.HSF.BF.A.1: Write a function that describes a relationship  | <ul> <li>identifying and using the algebraic</li> </ul>   |
|--|---|
| between two quantities.  | properties.   |
| <ul> <li>CCSS.HSA.SSE.A.1: Interpret expressions that represent a quantity in terms of its context.</li> <li>CCSS.HSA.SSE.A.1.A: Interpret parts of an expression, such as terms, factors, and coefficients.</li> <li>CCSS.HSA.SSE.A.2: Use the structure of an expression to identify ways to rewrite it.</li> </ul>  | <ul> <li>writing function rules from tables and word problems.</li> <li>determining the domain and range of various functions.</li> </ul> |
| <ul> <li>CCSS.HSA.SSE.B.3: Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.</li> <li>CCSS.HSF.BF.A.1.C: (+) Compose functions.</li> <li>CCSS.MP3 Construct viable arguments and critique the reasoning of others.</li> <li>CCSS.MP7 Look for and make use of structure.</li> </ul> |   |
| Used in Content Area Standards   | 21 <sup>st</sup> Century Skills   |
|  | <ul><li>Technology Literacy</li><li>Communication</li></ul>   |

| Stage 2 - Evidence   |  |  |
|--|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |  |

# **Unit 2: Algebraic Expressions & Functions Exponential Expressions & Functions**

**Stage 1 Desired Results** 

| ESTABLISHED GOALS: |
|--------------------|
|--------------------|

Students will continue their study of mathematics in the areas of algebraic expressions and functions. In this unit, students will gain a deeper understanding of exponential expressions and functions.

#### Content Standards:

- CCSS.HSA.SSE.A.2: Use the structure of an expression to identify ways to rewrite it.
- CCSS.HSA.SSE.B.3: Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.
- CCSS.HSA.APR.A.1: Understand that polynomials form a system analogous to the integers; namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.
- CCSS.8A.IF.08.b: Use the properties of exponents to interpret expressions for exponential functions
- CCSS.MP1 Make sense of problems and persevere in solving them.
- CCSS.MP2 Reason abstractly and quantitatively.
- CCSS.MP7 Look for and make use of structure.

#### Transfer

#### Students will be able to independently use their learning to...

- recognize the key characteristics of exponential functions and its real-life applications
- use knowledge of exponential function in future studies of logarithmic functions

#### Meaning

#### ENDURING UNDERSTANDINGS

- Very large and small numbers can be represented efficiently using scientific notation
- Exponent properties can be proven through expansion.
- Exponential functions model real world phenomena.

#### **ESSENTIAL QUESTIONS**

- What are the rules of exponents and how are they applied to simplify expressions?
- How can exponents model real world data?

#### **Acquisition**

#### Students will understand...

- properties of exponents can simplify monomial expressions.
- scientific notation can be used to write really large or small numbers.
- geometric applications of monomial expressions.
- negative exponents have a reciprocal relationship.
- exponential functions model real world phenomena.

- using the rules of exponents to simplify monomials.
- applying geometric formulas to problems involving monomials.
- writing large or small numbers in scientific notation.
- performing operations on numbers expressed in scientific notation.
- graphing exponential functions.

| Used in Content Area Standards | 21st Century Skills |
|--------------------------------|---------------------|
|                                | Critical thinking   |
|                                | Technology Literacy |

| Stage 2 - Evidence  |  |
|---------------------|--|
| Evaluative Criteria | Assessment Evidence  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |

### Windham School District Curriculum Algebra 1 - Grade 8 **Unit 3: Algebraic Equations Solving Equations & Inequalities**

#### ESTABLISHED GOALS:

Students will continue their study of mathematics in the areas of Students will be able to independently use their learning to... algebraic equations. In this unit, students will gain a deeper understanding of solving equations and inequalities.

#### Content Standards:.

- CCSS.HSA.CED.1. Create equations and inequalities in one variable and use them to solve problems.
- CCSS.HSF.A.REI.1. Understand solving equations as a process of reasoning and explain the reasoning. Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.
- CCSS.HSA.REI.3. Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.
- CCSS.HSA.CED.A.4: Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. For example, rearrange Ohm's law V = IR to highlight resistance R
- CCSS.MP1 Make sense of problems and persevere in solving them.

#### **Stage 1 Desired Results**

use their skills of writing and solving equations as an effective problem solving technique.

Transfer

explain when an inequality should be written rather than an equation.

#### Meaning

#### ENDURING UNDERSTANDINGS

- Operations performed on one side of an equation must be performed on the other side(s) in order to preserve the equality
- Solutions to inequalities represent a range of values rather than a single value.

#### **ESSENTIAL QUESTIONS**

- How do you use expressions and equations to model real world problems?
- How can an equation or inequality be manipulated to isolate a variable while preserving the value of the original equation/inequality?

#### **Acquisition**

#### Students will understand...

- literal equations
- absolute value equations can have multiple solutions.
- percentages and proportions.
- connections between solving equations and solving inequalities.

- writing and solving multi-step equations with rational coefficients.
- writing and solving multi-step one-variable inequalities and graphing them on a number line.
- solving and graphing compound inequalities.
- graphing inequalities on a number line.
- solving absolute value equations.
- solving literal equations.

| CCSS.MP3 Construct viable arguments and critique the reasoning of others. | <ul> <li>writing and solving proportions, including proportions with binomials in the</li> </ul> |
|---|--|
| CCSS.MP4 Model with mathematics.  | numerator or denominator.  |
| CCSS.MP7 Look for and make use of structure.                              | <ul> <li>writing and solving application percent</li> </ul>                                      |
| CCSS.MP8 Look for and express regularity in repeated                      | problems.  |
| reasoning.  | <ul> <li>solving absolute value inequalities.</li> </ul>   |
| Used in Content Area Standards  | 21st Century Skills  |
|   | <ul> <li>Communication</li> </ul>  |
|   | Critical thinking  |

| Stage 2 - Evidence  |  |
|---------------------|--|
| Evaluative Criteria | Assessment Evidence  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |

# Windham School District Curriculum Algebra 1 - Grade 8 Unit 4: Functions - Linear Functions

#### **Stage 1 Desired Results**

#### **ESTABLISHED GOALS:**

Students will continue their study of mathematics in the area of functions. In this unit, students will gain a deeper understanding of linear relationships.

#### Content Standards:

- CCSS.HSF.IF.B.4: For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship.
- CCSS.HSF.IF.B.6: Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.
- CCSS.HSF.IF.C.7.A: Graph linear and quadratic functions and show intercepts, maxima, and minima.
- CCSS.HSF.IF.C.8: Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.
- CCSS.HSF.IF.C.9: Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).
- CCSS.HSA.CED.A.1: Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.

#### Transfer

#### Students will be able to independently use their learning to...

- make connections between linear functions and real-life scenarios
- use knowledge of linear functions as they learn other more advanced functions.

#### Meaning

#### ENDURING UNDERSTANDINGS

- Linear relationships have a constant rate of change
- Tables, graphs, and equations are all ways of representing functions and real world phenomena
- Slope can be referenced in many different forms.

#### ESSENTIAL QUESTIONS

- How can graphs be used to solve linear equations?
- How do you determine the appropriate form of an equation for a line when given specific characteristics?
- What is the relationship between slope and rate of change and how can each be used to solve real world problems?

#### Acquisition

#### Students will understand...

- the concept of slope and rate of change
- direct variation equations
- arithmetic sequences.
- equations of lines in slope-intercept form, point slope form, and standard form.
- properties of horizontal and vertical lines.

- calculating slope between two points
- determining the slope of a line, given an equation, table, or graph
- finding and determining intercepts.
- determining whether lines are parallel, perpendicular or neither.
- graphing linear equations.
- writing linear equations in slopeintercept, standard and point-slope form.

| Stage 2 - Evidence   |  |
|--|--|
| Evaluative Criteria Assessment Evidence                                      |  |
| ASSESSMENT: Written Assessments or Projects                                  |  |
| OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

**Unit 5: Functions - Bivariate Data (Scatterplots)** 

| Stage 1 Desired Results   |   |  |
|---|---|--|
| ESTABLISHED GOALS:  | Tra   | nsfer  |
| Students will continue their study of mathematics in  | Students will be able to independently use their lea  | arning to  |
| the area of functions. In this unit, students will gain a   | • use their ability to analyze data in scatterplots   | to analyze real-life data sets   |
| deeper understanding of bivariate data.   | <ul> <li>use their knowledge of scatterplots in future st</li> </ul>  | udies of statistical data  |
|   | ·   | aning  |
| Content Standards:  | ENDURING UNDERSTANDINGS   | ESSENTIAL QUESTIONS  |
| <ul> <li>CCSS.HSS.ID.B.6: Represent data on two</li> </ul>  | Scatter plots can model data and be used to   | How can mathematics be used to model and   |
| quantitative variables on a scatter plot, and   | make predictions.   | make predictions for real world phenomena?   |
| describe how the variables are related.   | Acqu  | isition  |
| <ul> <li>CCSS.HSS.ID.B.6.c: Fit a linear function for a scatter plot that suggests a linear association.</li> <li>CCSS.HSF.S.ID.8 Interpreting linear models-Compute (using technology) and interpret the correlation coefficient of a linear fit.</li> <li>CCSS.MP4 Model with mathematics.</li> <li>CCSS.MP5 Use appropriate tools strategically</li> </ul> | <ul> <li>Students will understand</li> <li>scatter plots show relationships between two variables.</li> <li>some data can be modeled using a linear equation.</li> <li>equations of a line of best fit.</li> <li>Correlation of two variables</li> <li>not all data is linear.</li> </ul> | <ul> <li>representing bivariate data with scatterplots.</li> <li>interpreting scatterplots.</li> <li>calculating the line of best fit.</li> <li>using the line of best fit to find the starting point represented by the y-intercept; to describe what the slope means; and to find the values at a particular point including outside the given graph.</li> <li>determining if there is a correlation between bivariate data.</li> <li>making predictions based on the line of best fit.</li> </ul> |
| Used in Content Area Standards  |   | 21st Century Skills  |
|   |   | Technology Literacy  |
|   |   | Critical thinking  |
|   |   |  |

| Stage 2 - Evidence  |  |
|---------------------|--|
| Evaluative Criteria | Assessment Evidence  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |

### **Unit 6: Algebraic Equations - Linear Systems**

|  | Stage 1 Desired Results                   |
|--|---|
| ESTABLISHED GOALS:   |   |
| Students will continue their study of mathematics in the area of | Students will be able to in               |
| algebraic equations. In this unit, students will gain a deeper   | <ul> <li>extend their knowledg</li> </ul> |
| understanding of linear systems.                                 | <ul> <li>Recognize systems of</li> </ul>  |
|  |   |

#### Content Standards:

- CCSS.HSF.A.CED.2: Create equations that describe numbers or relationships- Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
   CCSS.HSA.CED.A.3: Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.
- CCSS.HSA.REI.C.5: Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions. CCSS.HSA.REI.C.6: Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.
- CCSS.HSA.REI.10. Represent and solve equations and inequalities graphically. Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane often forming a curve (which could be a line).

#### Transfer

#### Students will be able to independently use their learning to...

- extend their knowledge of linear systems to solve nonlinear systems
- Recognize systems of linear equations as a valuable problem solving tool

#### Meaning

#### ENDURING UNDERSTANDINGS

- There is more than one way to solve a system of equations, and students can determine the most efficient method for solving.
- Systems of equations with two unknowns can be used to solve real world problems.

#### **ESSENTIAL QUESTIONS**

- How do you solve real world problems using systems of equations?
- Which method is best and why?
- How can systems of equations be used to represent situations and solve problems?
- What does the number of solutions (none, one or infinite) of a system of linear equations represent?

#### Acquisition

#### Students will understand...

- linear systems as a model
- Graphical and algebraic representations of linear systems
- linear inequalities and their graphical representation.

- writing and solving linear systems by graphing, elimination, and substitution.
- distinguishing if a system of equations has one solution, no solution, or infinitely many solutions.
- graphing linear inequalities on a coordinate plane.

|  | <ul> <li>Critical thinking</li> <li>Technology Literacy</li> </ul> |
|--|--|
| Used in Content Area Standards                                     | 21 <sup>st</sup> Century Skills                                    |
| reasoning.   |  |
| CCSS.MP8 Look for and express regularity in repeated               |  |
| CCSS.MP7 Look for and make use of structure.                       |  |
| CCSS.MP6 Attend to precision.                                      |  |
| CCSS.MP5 Use appropriate tools strategically.                      |  |
| them.  |  |
| CCSS.MP1 Make sense of problems and persevere in solving           | situations with systems of equations.                              |
| of the corresponding half-planes.                                  | <ul> <li>modeling and solving real world</li> </ul>                |
| system of linear inequalities in two variables as the intersection | inequalities in one variable.                                      |
| case of a strict inequality), and graph the solution set to a      | <ul> <li>creating and interpreting linear</li> </ul>               |
| two variables as a half-plane (excluding the boundary in the       | on a coordinate plane.   |
| • CCSS.HSA.REI.D.12: Graph the solutions to a linear inequality in | <ul> <li>graphing systems of linear inequalities</li> </ul>        |

| Stage 2 - Evidence                      |  |
|---|--|
| Evaluative Criteria Assessment Evidence |  |
|   | ASSESSMENT: Written Assessments or Projects                                  |
|   | OTHER EVIDENCE: independent practice, classroom observations and discussions |

# Unit 7: Algebraic Expressions & Equations Polynomials & Quadratics

| Stage 1 Desired Results  |   |   |
|--|---|---|
| ESTABLISHED GOALS:   | Trai  | nsfer   |
| Students will continue their study of mathematics in               | Students will be able to independently use their lea                | rning to  |
| the area of algebraic expressions and equations. In this           | <ul> <li>connect their understanding of properties of po</li> </ul> | lynomials to simplify complex numbers and radical                   |
| unit, students will gain a deeper understanding of                 | expressions   |   |
| simplifying polynomials and factoring and solving                  | <ul> <li>use their understanding of solving quadratic eq</li> </ul> | uations when solving higher order equations                         |
| quadratics.  | Meaning   |   |
|  | ENDURING UNDERSTANDINGS   | ESSENTIAL QUESTIONS   |
| Content Standards:   | <ul> <li>Mathematical properties extend to simplify</li> </ul>      | What characteristics of a polynomial determine                      |
| CCSS.HSA.SSE.B.3: Choose and produce an                            | polynomials.  | how to factor it completely?  |
| equivalent form of an expression to reveal and                     | Acqu  | isition   |
| explain properties of the quantity represented by                  | Students will understand  | Students will be skilled at   |
| the expression.  | • the degree and standard form of a polynomial                      | <ul> <li>simplifying polynomial expressions.</li> </ul>             |
| CCSS.HSA.SSE.B.3.a: Factor a quadratic expression                  | <ul> <li>factoring polynomials: greatest common factor,</li> </ul>  | <ul> <li>solving quadratic equations by factoring.</li> </ul>       |
| to reveal the zeros of the function it defines.                    | difference of squares, trinomial factoring                          | <ul> <li>solving geometric problems involving</li> </ul>            |
| CCSS.HSA.APR.A.1: Understand that polynomials                      | quadratic equations.  | polynomials.  |
| form a system analogous to the integers; namely,                   |   | <ul> <li>factoring quadratics (leading coefficient is 1)</li> </ul> |
| they are closed under the operations of addition,                  |   | and other polynomials.  |
| subtraction, and multiplication; add, subtract, and                |   | <ul> <li>factoring polynomials</li> </ul>                           |
| multiply polynomials.  |   |   |
| CCSS.HSA.REI.B.4: Solve quadratic equations in                     |   |   |
| one variable   |   |   |
| CCSS.MP1 Make sense of problems and persevere                      |   |   |
| in solving them.   |   |   |
| <ul> <li>CCSS.MP2 Reason abstractly and quantitatively.</li> </ul> |   |   |

| CCSS.MP7 Look for and make use of structure. |                     |
|--|---------------------|
| Used in Content Area Standards               | 21st Century Skills |
|  | Communication       |
|  | Critical thinking   |

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

# Windham School District Curriculum Algebra 1 - Grade 8 Unit 8: Algebraic Expressions & Equations Radical Expressions & Equations

|   | tage 1 Desired Results  |  |
|---|---|--|
| ESTABLISHED GOALS:  | Tro   | ansfer   |
| Students will continue their study of mathematics in the area of algebraic expressions and equations. In this unit, students will gain a deeper understanding of radical expressions and equations.  Content Standards:  CCSS.HSA.SSE.A.2: Use the structure of an expression to identify ways to rewrite it.  CCSS.HSA.SSE.B.3: Choose and produce an equivalent form of   | roots.  • use their knowledge of solving radical ed  Me  ENDURING UNDERSTANDINGS  • Radicals represent numbers.   | essions to simplify expressions with rational  |
| an expression to reveal and explain properties of the quantity represented by the expression.   | variables.  | uisition   |
| <ul> <li>CCSS.HSG.SRT.C.8: Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.</li> <li>CCSS.HSN.RN.A.2: Rewrite expressions involving radicals and rational exponents using the properties of exponents.</li> <li>CCSS.HSA.REI.A.2: Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.</li> <li>CCSS.MP7 Look for and make use of structure</li> <li>CCSS.MP8 Look for and express regularity in repeated reasoning.</li> </ul> | <ul> <li>Students will understand</li> <li>radical expressions.</li> <li>Pythagorean theorem</li> <li>equivalent representations of radical expressions.</li> <li>radical equations.</li> <li>extraneous solutions in radical equations.</li> </ul> | <ul> <li>Students will be skilled at</li> <li>simplifying radical expressions.</li> <li>adding, subtracting, multiplying, and dividing radicals.</li> <li>solving problems involving the Pythagorean theorem.</li> <li>solving radical equations.</li> <li>determining extraneous solutions when solving radical equations.</li> </ul> |
| Used in Content Area Standards  |   | 21 <sup>st</sup> Century Skills  |

|  | Communication |
|--|---------------|
|--|---------------|

| Stage 2 - Evidence  |  |  |
|---------------------|--|--|
| Evaluative Criteria | Assessment Evidence  |  |
|                     | ASSESSMENT: Written Assessments or Projects                                  |  |
|                     | OTHER EVIDENCE: independent practice, classroom observations and discussions |  |

#### ADDENDUM: MASTERY TOPICS - MATHEMATICS - GRADES K to 12

note: All curriculum topics will be discussed. The topics listed below will be emphasized, revisited, and assessed multiple times.

#### Kindergarten

- Count to 100 by 1's and 10's. (K.CC.A.1, K.CC. A. 2)
- Identify, read, write, and represent a number of objects with a written number 0 to 20 (K.CC.A. 3 K.CC. B 4)
- Count to answer "how many" up to 20 in various arrangements. (K.CC.B.5)
- Compare numbers represented in objects and numerals. (K.CC. 6, K.CC.7)
- Use strategies to represent and solve addition and subtraction problems within 10. (K.OA.A1 K.OA.A.2, K.OA.A.3)
- For any number from 1 to 9, find the number that makes 10 when added to the given number. (K.OA.A.4)
- Fluently adds and subtracts within 5. (K.OA.A.5)
- Work with numbers 11 to 19 to gain foundations for place value. (K.NBT.A.1)

#### 1st Grade:

- Count, read, and write numbers from 1 to 120. (1.NBT.A.1)
- Identify, organize, and represent tens and ones. (1.NBT.A.2)
- Compare numbers using symbols (<, >, =). (1 NBT.B.3)
- Use strategies to represent and solve addition and subtraction problems within 20. (1.OA.A.1)
- Fluently add and subtract within 10. (1.OA.C.6)
- Define and compose shapes (2-D and 3-D) by their attributes. (1.G.A.1, 1G.A.2)
- Divide wholes into equal shares (halves and fourths). (1.G.A.3)
- Measure with non-standard units and compare lengths of objects. (1.MD.A.1, 1.MD.A.2)
- Create graphs and interpret data. (1.MD.C.4)
- Tell and write time to the hour and half-hour. (1.MD.B.3)

#### 2nd Grade:

- Solve one- and two- step problems using addition and subtraction (2.OA.A.1).
- Fluently add and subtract within 20 (2.OA.B.2).
- Partition circles and rectangles into halves, thirds, and fourths (2.G.A.3).
- Identify and understand the value of digits in the hundreds, tens, and ones places (2.NBT.A.1).
- Compare the value of two 3-digit numbers (2.NBT.A.4).
- Use concrete models, drawings, or strategies to add and subtract 2- digit numbers (2.NBT.B.5, 2.NBT.B.6, 2.NBT.B.7).
- Measure objects and compare lengths using standard units, selecting appropriate tools. (2.MD.A.1, 2.MD.A.2, 2. MD. A.4)

- Recognize and draw 2-D and 3-D shapes and their attributes. (2.G.A.1)
- Collect data, draw picture, bar, and line plot graphs, and solve problems related to graphs. (2.MD.D.9, 2.MD.D.10)

#### 3rd Grade:

Operations and Algebraic Thinking

- Know the multiplication facts to 100 (3.OA.C.7)
- Know and be able to use the multiplication properties (commutative, associative, distributive)(3.OA.B.5)

Number and Operations in Base Ten

Round to nearest 10 and 100 (3.NBT.A.1)

Number and Operations - Fractions

- Understand fractions (as equal parts to whole, what numerator and denominator represent) (3.NF.A.1)
- Fractions on a number line (3.NF.A.2)
- Compare fractions with same numerator or denominator (3.NF.A.3.D)

Measurement and Data

- Tell time to the nearest minute. (3.MD.A.1)
- Time intervals in minutes on a number line(3.MD.A.1)
- Create and interpret picture and bar graphs. (3.MD.B.4)
- Measure to nearest quarter inch. (3.MD.B.4)
- Understand area can be found using multiplication or addition. (3.MD.C.7)
- Find the perimeter of a polygon given the side lengths. (3.MD.D.8)

#### Geometry

Classify quadrilaterals by their attributes.(3.G.A.1)

#### 4th Grade:

Operations and Algebraic Thinking

- Know the division facts to 100. (3.OA.C.7)
- Find factors and multiples of given numbers. (4.OA.B.4)

Number and Operations in Base Ten

- Recognize that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. (4.NBT.A.1)
- Read, write, and compare multi-digit whole numbers in standard, word, and expanded form. (4.NBT.A.2)
- Round whole numbers up to 1,000,000. (4.NBT.A.3)
- Add and subtract multi-digit whole numbers up to 1,000,000. (4.NBT.B.4)
- Multiply numbers (4 digits by one digit and 2 digits by 2 digits). (4.NBT.B.5)
- Divide by 1-digit divisors. (4.NBT.B.6)

**Number and Operations - Fractions** 

- Recognize and find equivalent fractions. (4.NF.A.1)
- Add and subtract fractions with like denominators. (4.NF.B.3)

#### Measurement and Data

- Measure angles with a protractor (already lined up). (4.MD.C.6)
- Know relative size of measurement units and compare within a system. (4.MD.A.1)

#### Geometry

• Know and recognize points, lines, line segments, rays, types of angles, parallel, perpendicular. (4.G.A.1)

#### 5th Grade:

Operations and Algebraic Thinking

• Evaluate expressions with parentheses, brackets, and braces. (all four operations, excluding exponents) (5.OA.A.1)

#### Numbers and Operations in Base Ten

- Read, write, and compare decimals in standard, expanded, and word form. (5.NBT.A.3)
- Round decimals. (to hundredths) (5.NBT.A.4)
- Multiply whole numbers. (multi-digit) (5.NBT.B.5)
- Divide by 2-digit divisors. (5.NBT.B.6)
- Add, subtract, and multiply decimals. (5.NBT.B.7)

#### **Numbers and Operations - Fractions**

- Add and subtract fractions with unlike denominators. (5.NF.A.1)
- Multiply fractions and whole numbers. (5.NF.B.4)
- Divide fractions (whole number by a unit fraction and a unit fraction by a whole number.) (5.NF.B.7.B)

#### Measurement and Data

- Find the volume of right rectangular prisms. (whole numbers) (5.MD.C.3)
- Convert measurements within a system. (metric & US customary) (5.MD.A.1)

#### Geometry

- Classify two-dimensional figures. (triangles & quadrilaterals) (5.G.B.4)
- Graph points on the coordinate plane to solve real-world and mathematical problems. (quadrant I only) (5.G.A.1)

#### 6th Grade

#### **Numbers and Operations**

- GCF, LCM in application (6.NS.4)
- Decimal Division (other operations should be review) (6.NS.3)
- Fraction Division (other operations should be review) (6.NS.1/2)
- Mixed Number Operations (5.NF.1)
- Conversions of fractions, decimals and percents to the hundredths (6.NS.7)
- Ordering integers on a number line (6.NS.7)
- Graph points on coordinate plane in all four quadrants(6.NS.8)

#### Algebra

• Use proportional reasoning to set up rates and ratios. (6.RP.1/3)

- Solve one step equations with inverse operations and positive rational coefficients (6.EE.5/6)
- Order of Operations with whole numbers and exponents (6.EE.A3)

#### Geometry

- Volume and surface area of rectangular prisms with whole, fractions, and decimals (6.G.2)
- Area of regular polygons and composite figures (6.G.1)

#### **Probability and Statistics**

- Describe variations of data center vs. variability (6.SP.3)
- Interpret box plots (identify 5 number summary) (6.SP.4)

#### 6th Grade Accelerated Math

#### **Numbers and Operations**

- GCF, LCM in application (6.NS.4)
- Decimal Division (other operations should be review) (6.NS.3)
- Fraction Division (other operations should be review) (6.NS.1/2)
- Mixed Number Operations (5.NF.1)
- Conversions of fractions, decimals and percents to the hundredths (6.NS.7)
- Ordering integers on a number line (6.NS.7)
- Graph points on coordinate plane in all four quadrants(6.NS.8)
- Converting rational numbers to decimals: terminating and repeating decimals (7.NS.2)
- Operations with integers (7.NS.1/7.NS.2)
- Operations with Rational Numbers (7.NS.1/7.NS.2)

#### Algebra

- Use proportional reasoning to set up rates and ratios. (6.RP.1/3)
- Solve one step equations with inverse operations and positive rational coefficients (6.EE.5/6)
- Order of Operations with whole numbers and exponents (6.EE.A3)

#### Geometry

- Volume and surface area of rectangular prisms with whole, fractions, and decimals (6.G.2)
- Area of regular polygons and composite figures (6.G.1)
- Area and circumference of circles and composite figures (7.G.4)

#### **Probability and Statistics**

- Describe variations of data center vs. variability (6.SP.3)
- Interpret box plots (identify 5 number summary) (6.SP.4)

#### 7th Grade:

#### **Numbers and Operations**

Converting rational numbers to decimals: terminating and repeating decimals (7.NS.2)

- Operations with integers (7.NS.1/7.NS.2)
- Operations with Rational Numbers (7.NS.1/7.NS.2)

#### Algebra

- Use properties of operations to add, subtract, expand and factor linear expressions with rational numbers in any form (7.EE.1/7.EE.2)
- Find unit rate/constant of proportionality in tables, graphs, situations and equations (7.RP.2)
- Use proportions to solve ratio and percent problems, including percent proportion and equations (7.RP.3)
- Solve one-step equations and equations in the form px + q = r with all rational numbers (7.EE.3/7.EE.4)
- Solve and graph one-step inequalities on a number line with all rational numbers (7.EE.3)

#### Geometry

- Area and circumference of circles and composite figures (7.G.4)
- Use proportions to compute actual lengths from a scale drawing and reproduce an image with a new scale (7.G.1)

#### **Probability and Statistics**

• Calculate and compare experimental and theoretical probabilities (7.SP.6)

#### 7th Grade Accelerated Math

#### **Numbers and Operations**

- Converting rational numbers to decimals: terminating and repeating decimals (7.NS.2)
- Operations with integers (7.NS.1/7.NS.2)
- Operations with Rational Numbers (7.NS.1/7.NS.2)
- Decide whether a number is rational or irrational(8.NS.1)
- Compare rational and irrational numbers(8.NS.2)

#### Algebra

- Use properties of operations to add, subtract, expand and factor linear expressions with rational numbers in any form (7.EE.1/7.EE.2)
- Find unit rate/constant of proportionality in tables, graphs, situations and equations (7.RP.2)
- Use proportions to solve ratio and percent problems, including percent proportion and equations (7.RP.3)
- Solve one-step equations and equations in the form px + q = r with all rational numbers (7.EE.3/7.EE.4)
- Solve 2-step linear equations to find the value of a variable with integers (8.EE.7)
- Solve and graph one-step inequalities on a number line with all rational numbers (7.EE.3)

#### Geometry

- Area and circumference of circles and composite figures (7.G.4)
- Use proportions to compute actual lengths from a scale drawing and reproduce an image with a new scale (7.G.1)
- Verify experimentally the properties of reflections and translations (8.G.1)

- Describe the effect of translations and reflections on two-dimensional figures using coordinates (8.G.3)
- Know the formula for volume of a cylinder (8.G.9)
- Volume and Surface Area Triangular Prisms (7.G.6)

#### **Probability and Statistics**

• Calculate and compare experimental and theoretical probabilities (7.SP.6)

#### 8th Grade:

#### **Numbers and Operations:**

- Decide whether a number is rational or irrational(8.NS.1)
- Compare rational and irrational numbers(8.NS.2)

#### Algebra:

- Identify linear functions (8.F.3)
- Derive slope-intercept form equation y = mx for a line through the origin and the equation y = mx + b for a line intercepting the vertical axis at b (8.EE.6)
- Compare two different proportional relationships represented in different ways (8.EE.5)
- Solve 2-step linear equations to find the value of a variable with integers (8.EE.7)

#### Geometry

- Verify experimentally the properties of reflections and translations (8.G.1)
- Describe the effect of translations and reflections on two-dimensional figures using coordinates (8.G.3)
- Apply the Pythagorean Theorem to determine unknown side lengths in right triangles. (8.G.7)
- Know the formula for volume of a cylinder (8.G.9)
- Volume and Surface Area Triangular Prisms (7.G.6)

#### **Probability and Statistics**

Construct and interpret scatter plots (8.SP.1)

#### 8th Grade Algebra 1:

- Solve multistep equations (including with fractions) with applications and explanations
- Solve absolute value equations
- Graph functions using input/output tables
- Solve proportions
- Solve percent problems
- Solve and graph one-variable inequalities including multi-step, fractional, and compound inequalities
- Find the slope of a line using the formula, given an equation or graph
- Graph linear equations in slope-intercept form and standard form
- Graph linear inequalities in 2 variables on a coordinate plane
- Write equations in slope-intercept and point-slope form

- Solve system of linear equations using graphing, substitution and linear combinations
- Solve systems of linear inequalities by graphing.
- Understand a function: what is it?; basic notation; evaluate functions
- Add, subtract, multiply polynomials
- Using lines of best fit to answer questions (such as starting point as y-intercept; describing what the slope means; finding values at a particular point including beyond what the graph shows you
- Simplify monomial expressions
- Simplify radicals (numerical and variables)
- Use the slopes to determine if lines are parallel, perpendicular or neither
- Factor simple quadratics (coefficient =1)

#### Algebra 1:

- Solve multistep equations (including with fractions) with applications and explanations
- Solve absolute value equations
- Graph functions using input/output tables
- Solve proportions
- Solve percent problems
- Solve and graph one-variable inequalities including multi-step, fractional, and compound inequalities
- Find the slope of a line using the formula, given an equation or graph
- Graph linear equations in slope-intercept form and standard form
- Graph linear inequalities in 2 variables on a coordinate plane
- Write equations in slope-intercept and point-slope form
- Solve system of linear equations using graphing, substitution and linear combinations
- Solve systems of linear inequalities by graphing.
- Understand a function: what is it?; basic notation; evaluate functions
- Add, subtract, multiply polynomials
- Using lines of best fit to answer questions (such as starting point as y-intercept; describing what the slope means; finding values at a particular point including beyond what the graph shows you

#### CP Algebra 1:

- Solve multistep equations (including with fractions) with applications and explanations
- Solve absolute value equations
- Graph functions using input/output tables
- Solve proportions
- Solve percent problems
- Solve and graph one-variable inequalities including multi-step, fractional, and compound inequalities
- Find the slope of a line using the formula, given an equation or graph

- Graph linear equations in slope-intercept form and standard form
- Graph linear inequalities in 2 variables on a coordinate plane
- Write equations in slope-intercept and point-slope form
- Solve system of linear equations using graphing, substitution and linear combinations
- Solve systems of linear inequalities by graphing.
- Understand a function: what is it?; basic notation; evaluate functions
- Add, subtract, multiply polynomials
- Using lines of best fit to answer questions (such as starting point as y-intercept; describing what the slope means; finding values at a particular point including beyond what the graph shows you

#### **Geometry:**

- On a coordinate plane, find the distance between 2 points, the length of a segment, and the midpoint of a segment. Also apply the segment addition postulate.
- Use all angle relationships including: pairs of angles formed by parallel lines; complementary and supplementary angles; linear pair; and vertical angles.
- Apply the angle addition postulate.
- Understand the characteristics of parallel and perpendicular lines
- Solve problems using similarity of triangles and other polygons (including ratio of areas) and solids (including ratio of volumes) and dilations.
- Justify one's reasoning, throughout the school year, by use of informal proofs, justifications, logical reasoning and proof of evidence.
- Using different units of measure and converting in one, two and three dimensions.
- Know and use all facts of triangles and quadrilaterals.
- Apply the pythagorean theorem to solve problems.
- Know and use the facts of right triangles (special rights & trigonometry) to solve triangles and their applications.
- Know and use facts of circles
- Solve problems using congruence (triangles and other polygons)
- Apply prior knowledge 2-D (area to solve applications) & 3D (surface area of prisms and pyramids and volumes for all solids) shapes to solve applications (note: On surface area, emphasize breaking the shape into its parts rather than using the formula).

#### **CP Geometry:**

- On a coordinate plane, find the distance between 2 points, the length of a segment, and the midpoint of a segment. Also apply the segment addition postulate.
- Use all angle relationships including: pairs of angles formed by parallel lines; complementary and supplementary angles; linear pair; and vertical angles.
- Apply the angle addition postulate.
- Understand the characteristics of parallel and perpendicular lines
- Solve problems using similarity of triangles and other polygons (including ratio of areas) and solids (including ratio of volumes) and dilations.
- Justify one's reasoning, throughout the school year, by use of informal proofs, justifications, logical reasoning and proof of evidence.

- Using different units of measure and converting in one, two and three dimensions.
- Know and use all facts of triangles and quadrilaterals.
- Apply the pythagorean theorem to solve problems.
- Know and use the facts of right triangles (special rights & trigonometry) to solve triangles and their applications.
- Know and use facts of circles
- Solve problems using congruence (triangles and other polygons)
- Apply prior knowledge 2-D (area to solve applications) & 3D (surface area of prisms and pyramids and volumes for all solids) shapes to solve applications (note: On surface area, emphasize breaking the shape into its parts rather than using the formula).

#### **Honors Geometry:**

- On a coordinate plane, find the distance between 2 points, the length of a segment, and the midpoint of a segment. Also apply the segment addition postulate.
- Use all angle relationships including: pairs of angles formed by parallel lines; complementary and supplementary angles; linear pair; and vertical angles.
- Apply the angle addition postulate.
- Understand the characteristics of parallel and perpendicular lines
- Solve problems using similarity of triangles and other polygons (including ratio of areas) and solids (including ratio of volumes) and dilations.
- Justify one's reasoning, throughout the school year, by use of informal proofs, justifications, logical reasoning and proof of evidence.
- Using different units of measure and converting in one, two and three dimensions.
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- Solve problems using congruence (triangles and other polygons)
- Apply prior knowledge 2-D (area to solve applications) & 3D (surface area of prisms and pyramids and volumes for all solids) shapes to solve applications (note: On surface area, emphasize breaking the shape into its parts rather than using the formula).
- Use the Law of sines and cosines to solve problems

#### Algebra 2 Part A:

- Solve compound inequalities and applications
- Solve absolute value equations
- Graph absolute value equations and inequalities using a table of values and using basic transformations. Find domain and range.
- Graph quadratics using a table of values and basic transformations
- Find domain and range of quadratic functions
- Find vertex, zeros, y-intercept, direction of opening, and axis of symmetry of quadratic functions.
- Understand the difference between vertex and standard form of quadratic functions

- Solve application problems for quadratic functions
- Factor polynomials using greatest common factor, difference of squares, and trinomials to find zeros
- Graph systems of linear inequalities
- Use function notation for evaluating and graphing functions.

#### CP Algebra 2:

Factoring (trinomials with coefficient = 1; trinomials with coefficient not = 1; difference of squares; GCF; grouping;)

- Division of polynomials
- Graph Quadratic functions including basic transformations in both vertex form and standard form
- Find domain and range of functions
- Analyze quadratic functions (given graph or equation) for max, min, zeros, y-intercept, direction of opening, axis of symmetry
- Solve quadratic equations by factoring and using the quadratic formula
- Graph absolute value equations with transformations
- Evaluate and analyze functions given their graph
- Solving systems of a quadratic function and a linear function graphically and algebraically
- Composition of functions
- Operations with complex numbers
- Simplify expressions with integer and rational exponents
- Simplify numeric and algebraic radical expressions (to 3rd degree)

#### **Honors Algebra 2:**

- Factoring (trinomials with coefficient = 1; trinomials with coefficient not = 1; difference of squares; GCF; grouping;)
- Division of polynomials
- Graph Quadratic functions including basic transformations in both vertex form and standard form
- Find domain and range of quadratic functions
- Analyze quadratic functions (given graph or equation) for max, min, zeros, y-intercept, direction of opening, axis of symmetry
- Solve quadratic equations by factoring, completing the square, and using the quadratic formula
- Graph absolute value equations with transformations
- Evaluate and analyze functions given their graph
- Composition of functions
- Solving systems of a quadratic function and a linear function graphically and algebraically
- Operations with complex numbers
- Simplify expressions with integer and rational exponents
- Solve equations with integer and rational exponents
- Simplify numeric and algebraic radical expressions
- Solve radical equations

- Solve exponential functions  $(2^x = 8)$
- Perform operations with rational expressions

#### Precalculus:

- Trigonometry (unit circle, evaluate, applications, laws, graphs)
- Exponential/logarithmic functions (properties, solving, graphs, applications)
- Higher degree polynomials (graphs, transformations, analyze, properties)
- Inverse Functions
- Rational functions (properties, graphs, applications, analyze)

#### **Precalculus:**

- Trigonometry (unit circle, evaluate, applications, laws, graphs)
- Exponential/logarithmic functions (properties, solving, graphs, applications)
- Higher degree polynomials (graphs, transformations, analyze, properties)
- Inverse Functions
- Rational functions (properties, graphs, applications, analyze)
- Trigonometry (Identities, Formulas)
- Conics (graph, properties, analyze)
- Limits